



Predictive routing and multi-objective fleet sizing for shared mobility-on-demand

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Cognitive Robotics

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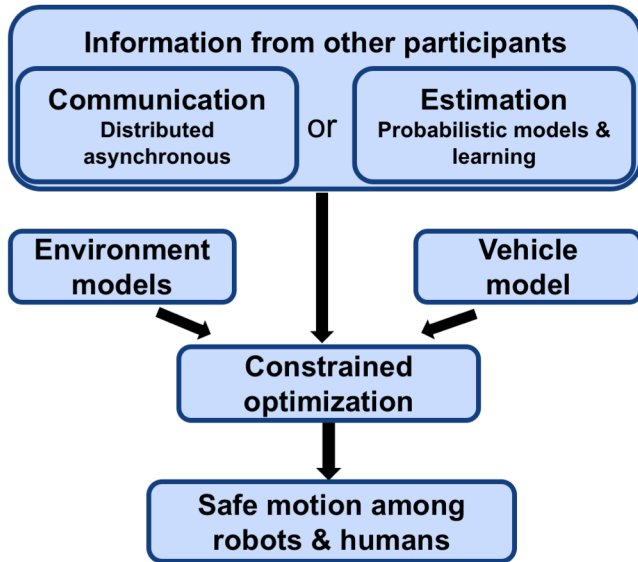
**AUTONOMOUS
MULTI-ROBOTS LAB**






**Autonomous cars will
make transport
reliable, safe, efficient,
comfortable and clean**

Motion planning for autonomous vehicles



- W. Schwarting et al., "Safe Nonlinear Trajectory Generation for Parallel Autonomy With a Dynamic Vehicle Model", T-ITS 2017
B. Zhou et al., "Joint Multi-Policy Behavior Estimation and Receding-Horizon Trajectory Planning for Automated Urban Driving", ICRA 2018
L. Ferranti et al., "SafeVRU: A Research Platform for the Interaction of Self-Driving Vehicles with Vulnerable Road Users", IV 2019



**Autonomous cars will
solve all our problems!
Reliable, safe, efficient,
comfortable and clean**





+40 %

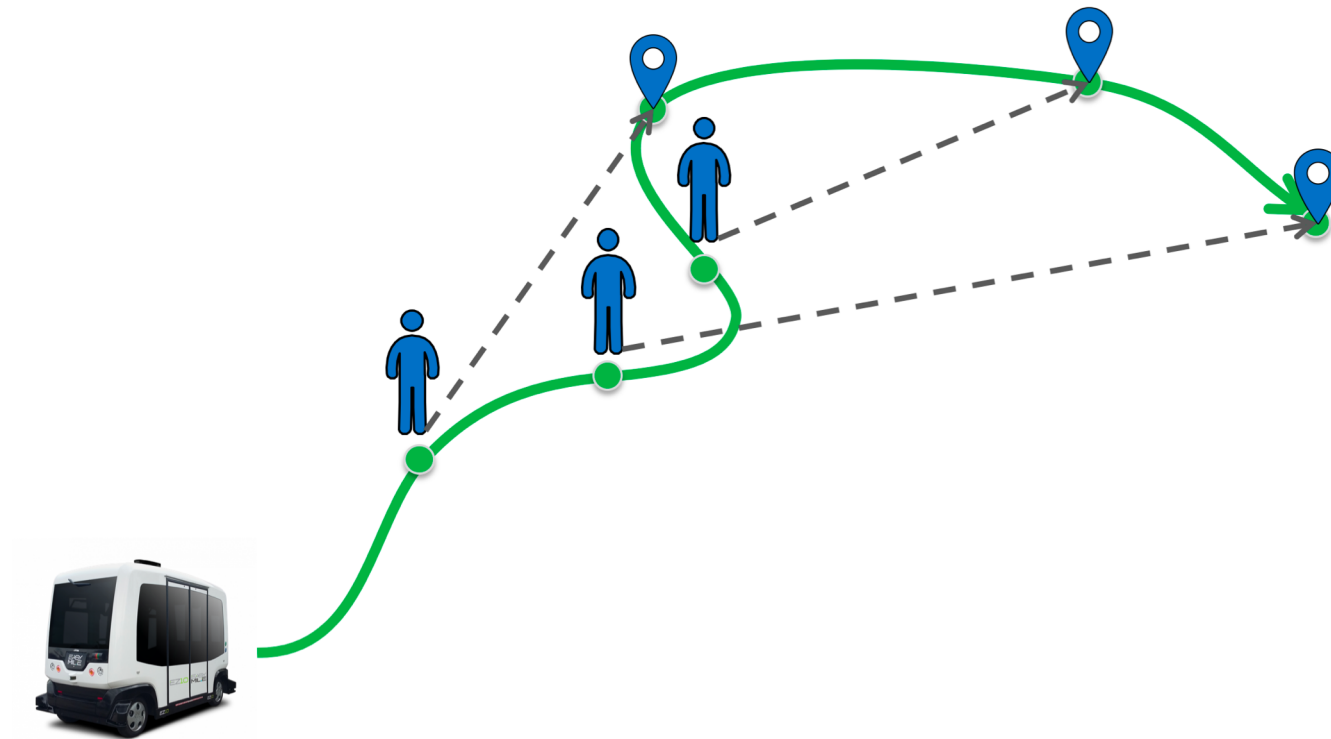


Ridesharing

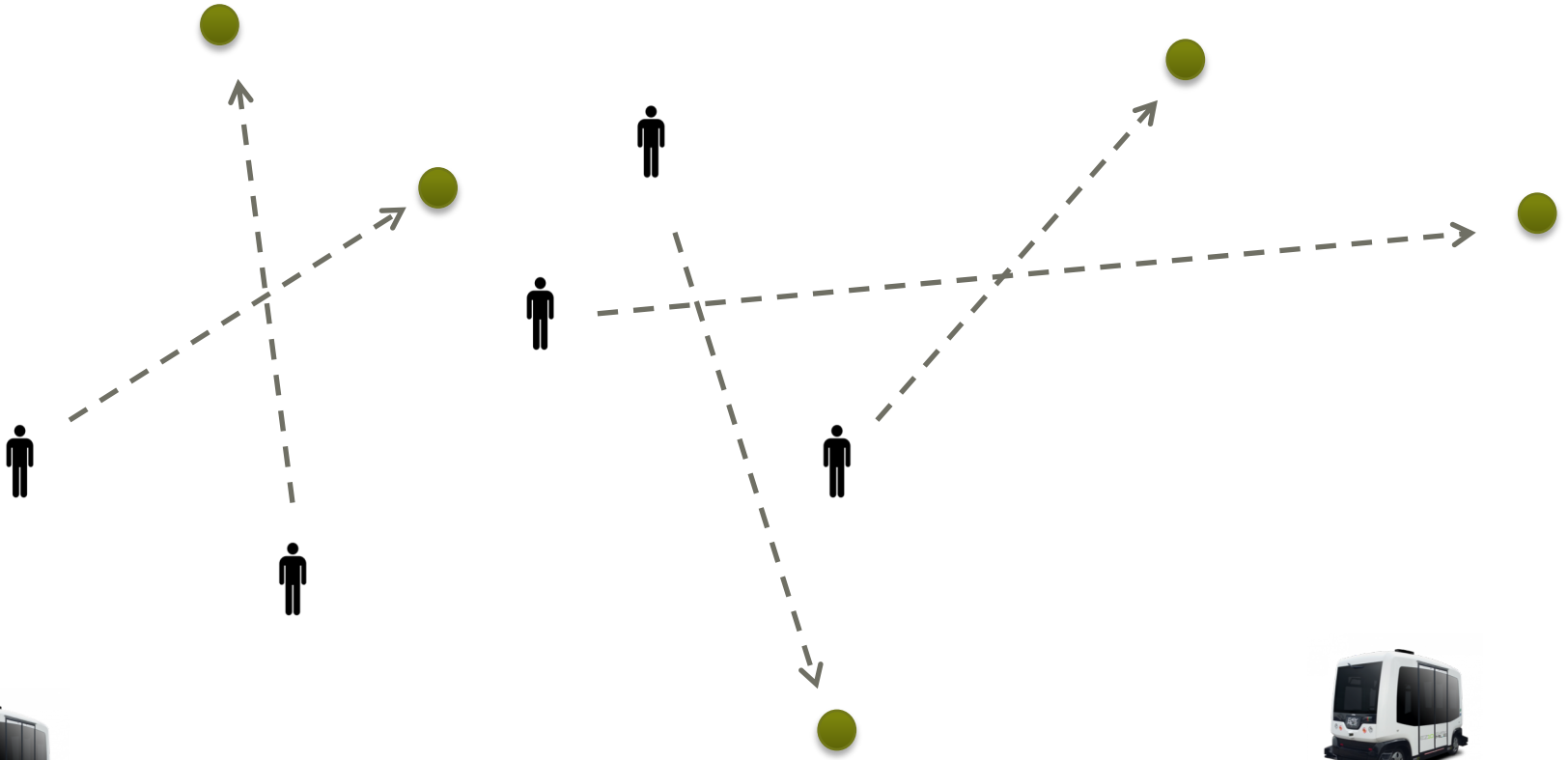
Ride sharing/pooling

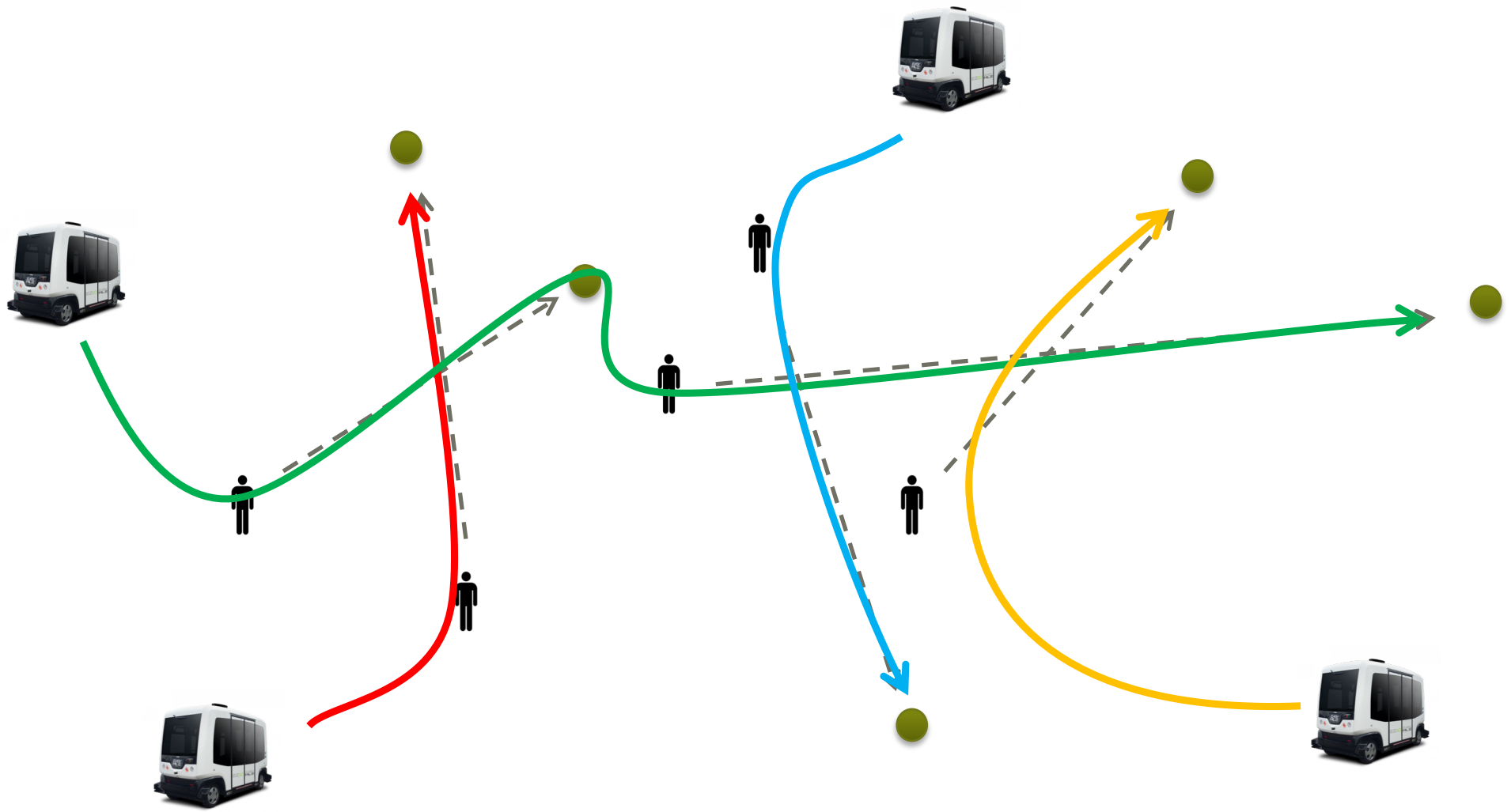
Instead of one passenger per vehicle, we can have **shared rides**

- Several passengers in the same vehicle
- Higher efficiency
- Less cars on the roads



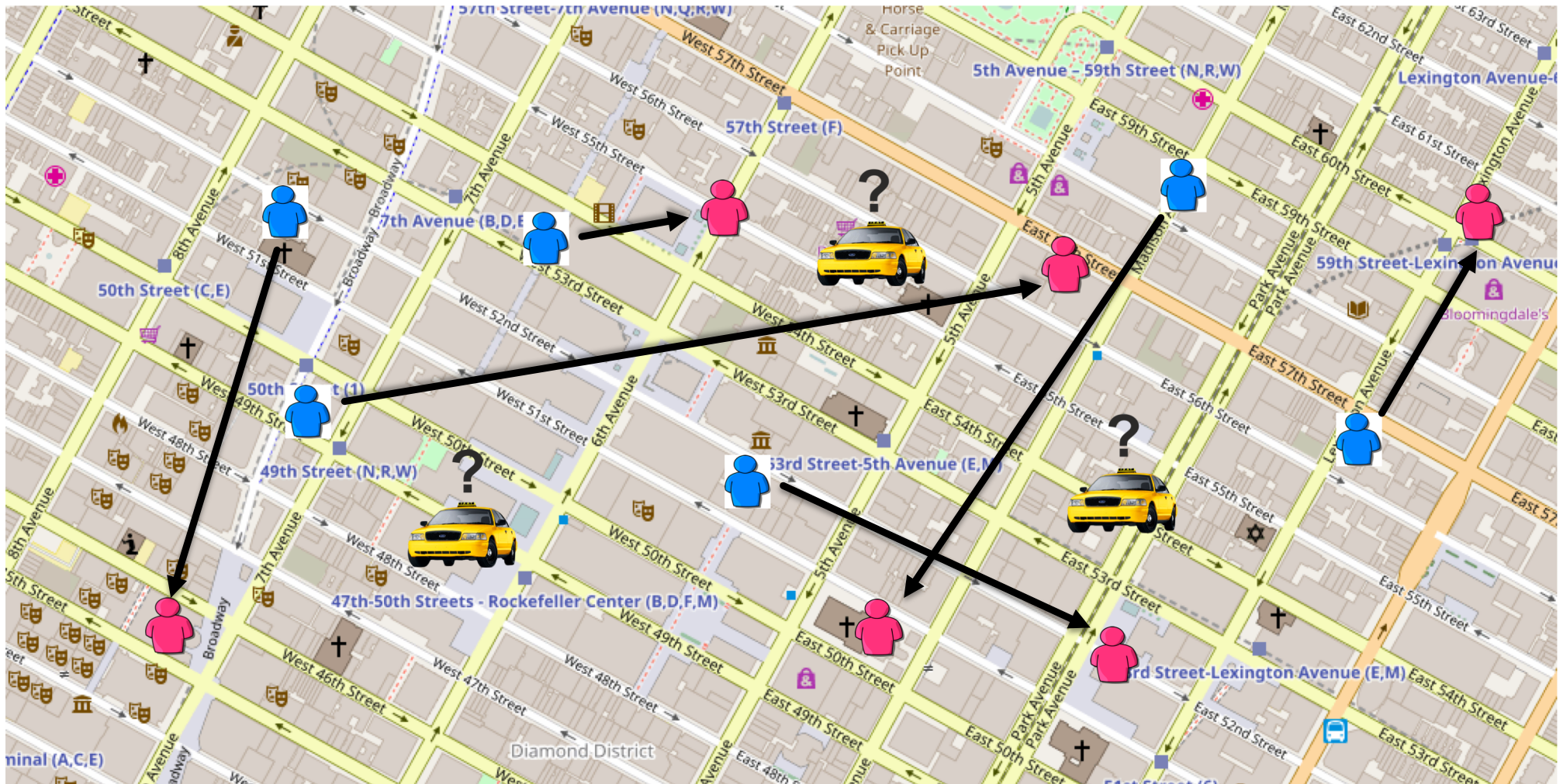






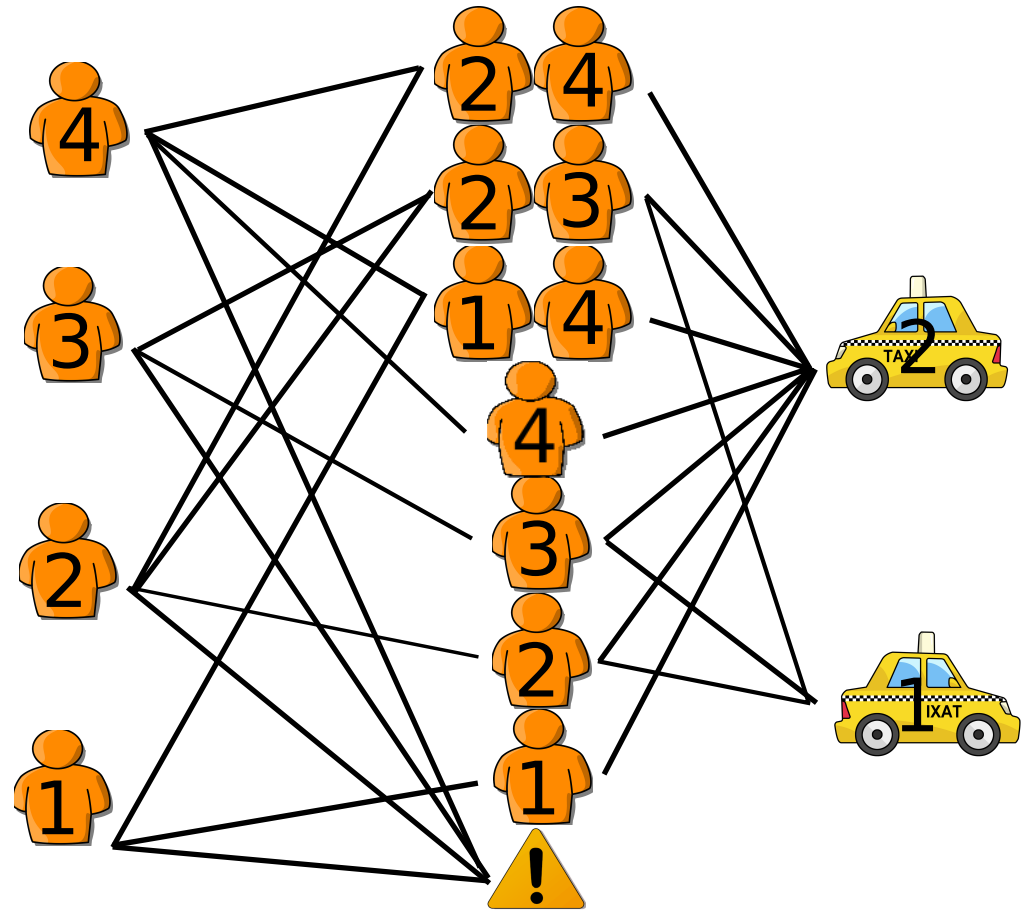
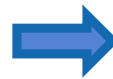
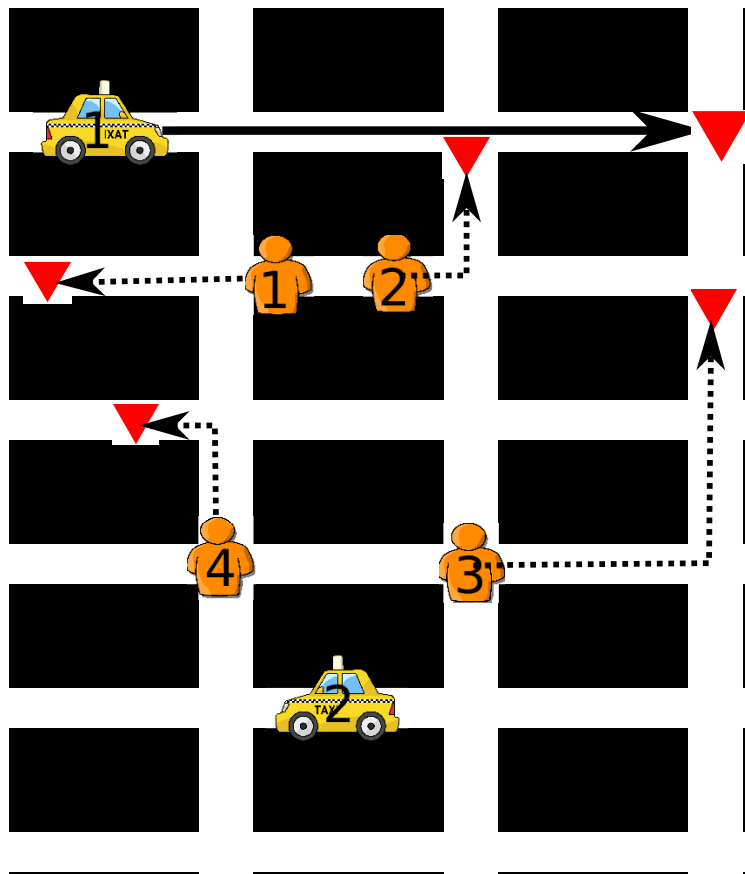
On-demand high-capacity ride-sharing

Large combinatorial complexity → Algorithm that is **scalable, online and anytime optimal**



Step 1: Compute feasible trips

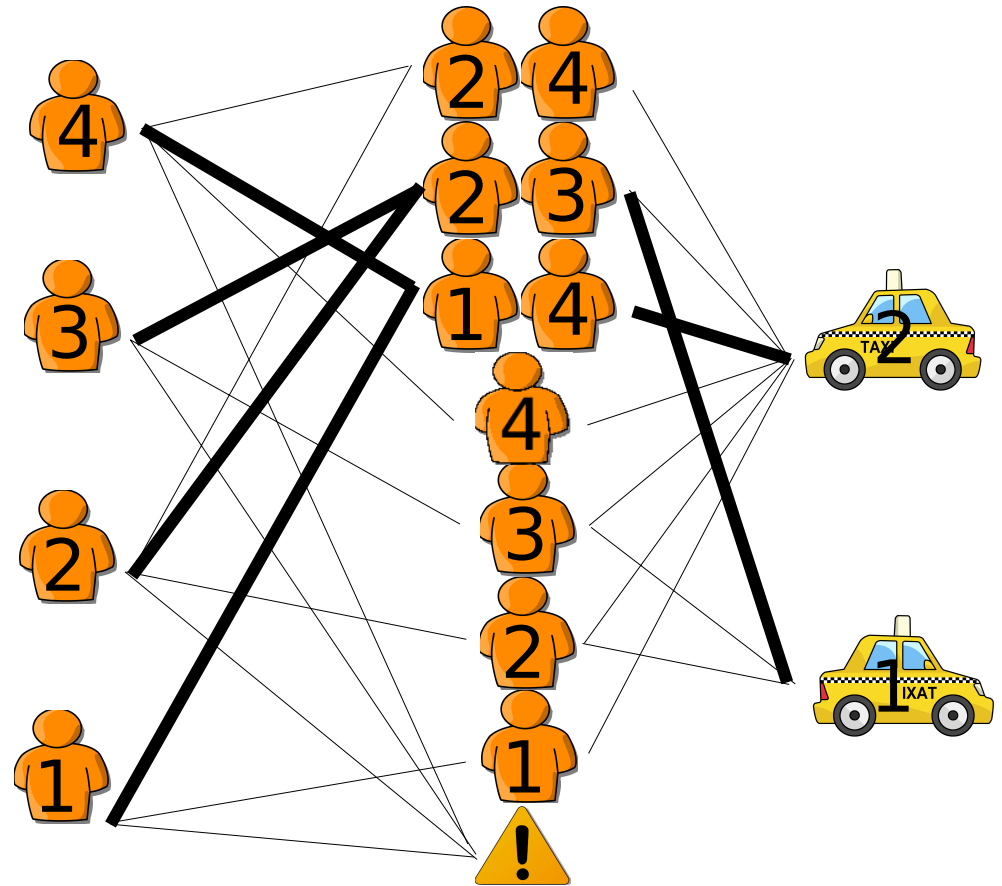
Incremental search of feasible routes/schedules



Step 2: Assignment of vehicles to trips

Formulated as an Integer Linear Program

- Initialized from greedy assignment
- Optimized over time
- Minimize sum of delays



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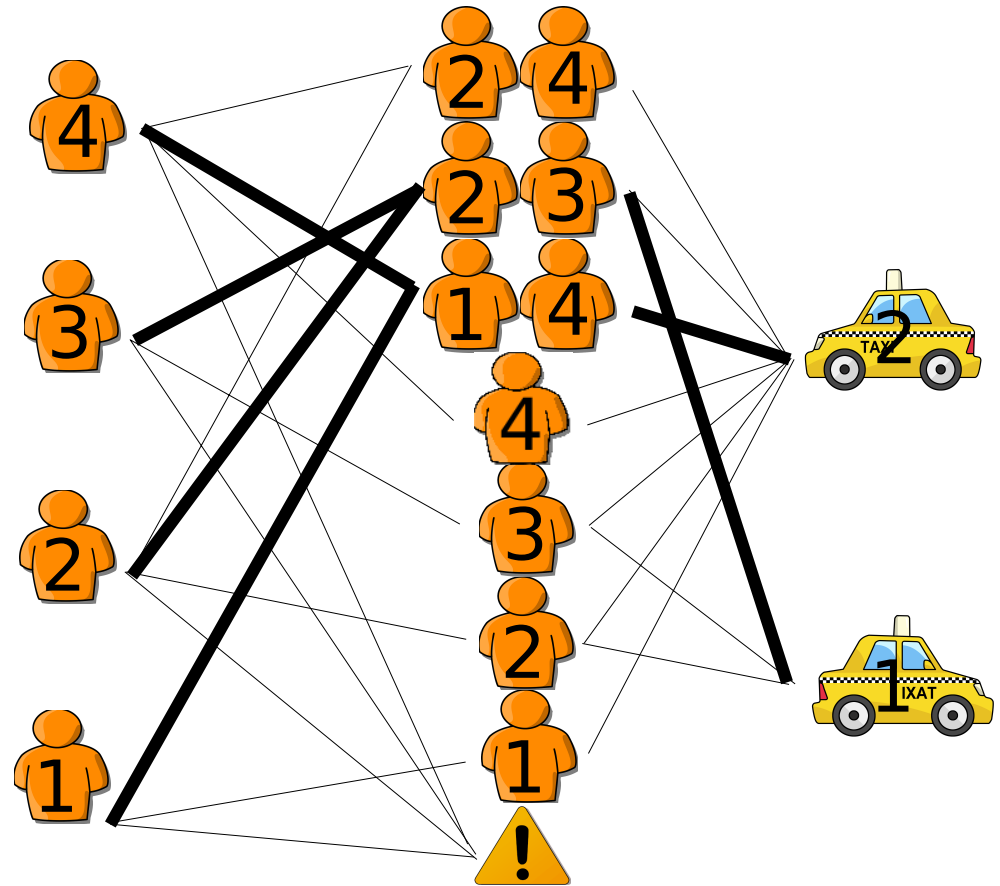
Algorithm 1. Optimal assignment

1: Initial guess: Σ_{greedy}

2: $\Sigma_{optim} := \arg \min_{\mathcal{X}} \sum_{i,j \in \mathcal{E}_{TV}} c_{i,j} \epsilon_{i,j} + \sum_{k \in \{1, \dots, n\}} c_{ko} \chi_k$

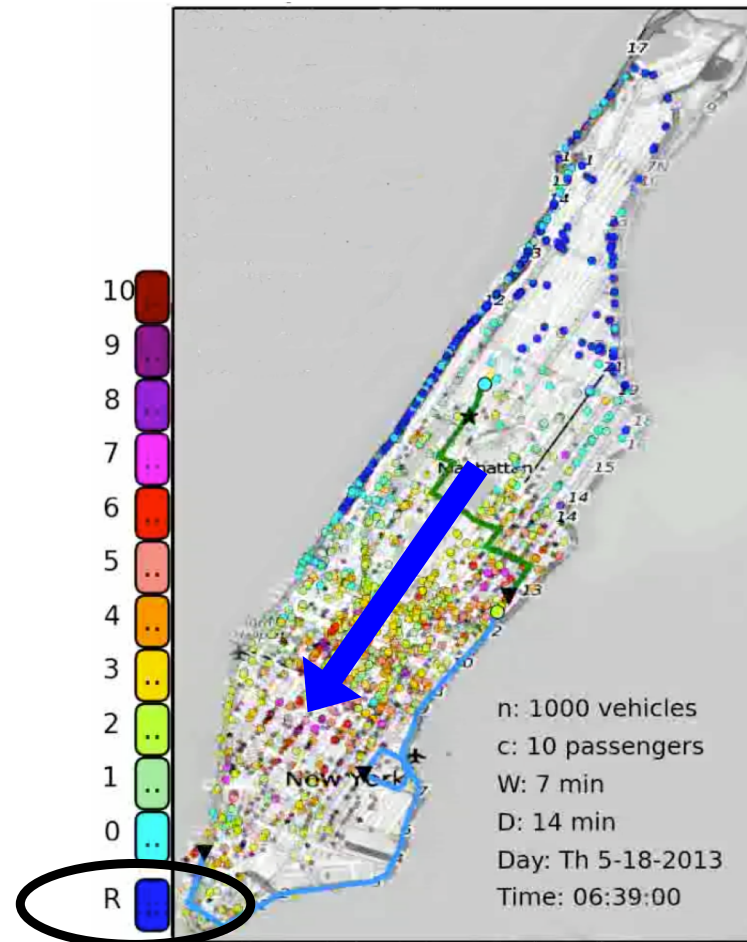
3: s.t. $\sum_{i \in \mathcal{I}_{V=j}^T} \epsilon_{i,j} \leq 1 \quad \forall v_j \in \mathcal{V}$

4: $\sum_{i \in \mathcal{I}_{R=k}^T} \sum_{j \in \mathcal{I}_{T=i}^V} \epsilon_{i,j} + \chi_k = 1 \quad \forall r_k \in \mathcal{R}$



Step 3: Rebalancing

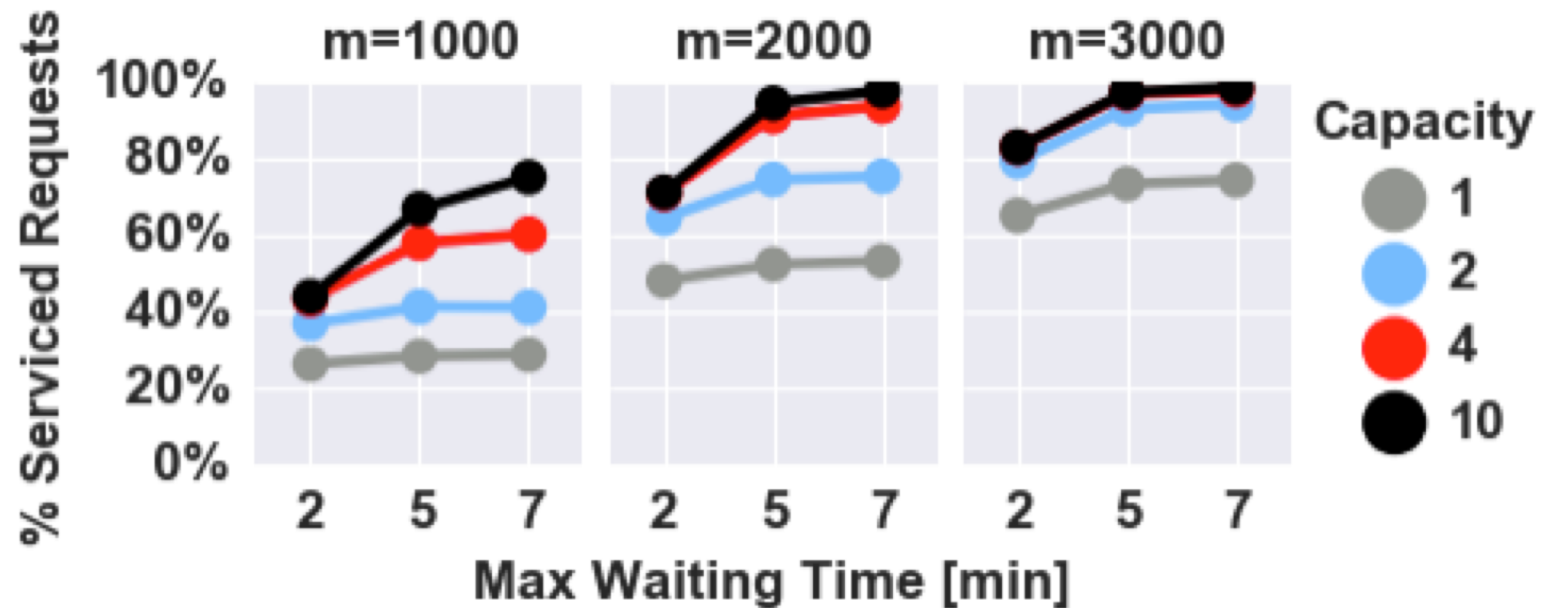
Move idle vehicles towards areas of high demand (formulated as a Linear Program)



1000, 2000 and 3000 vehicles

Capacity Four

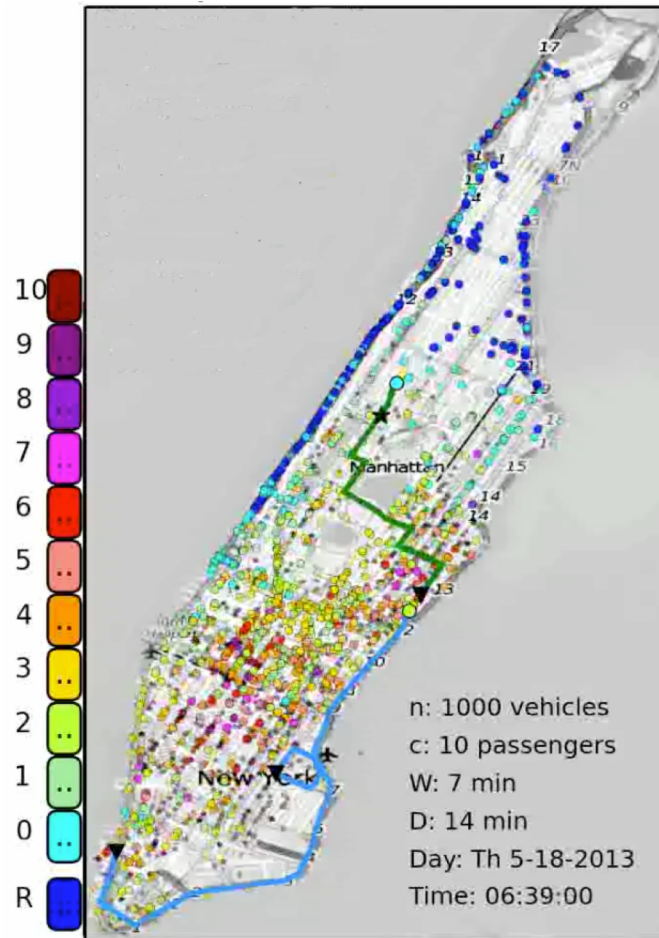
High service rate with less vehicles



High service rate with <25% of taxis

Predictive routing

At peak times mismatch of vehicles & demand

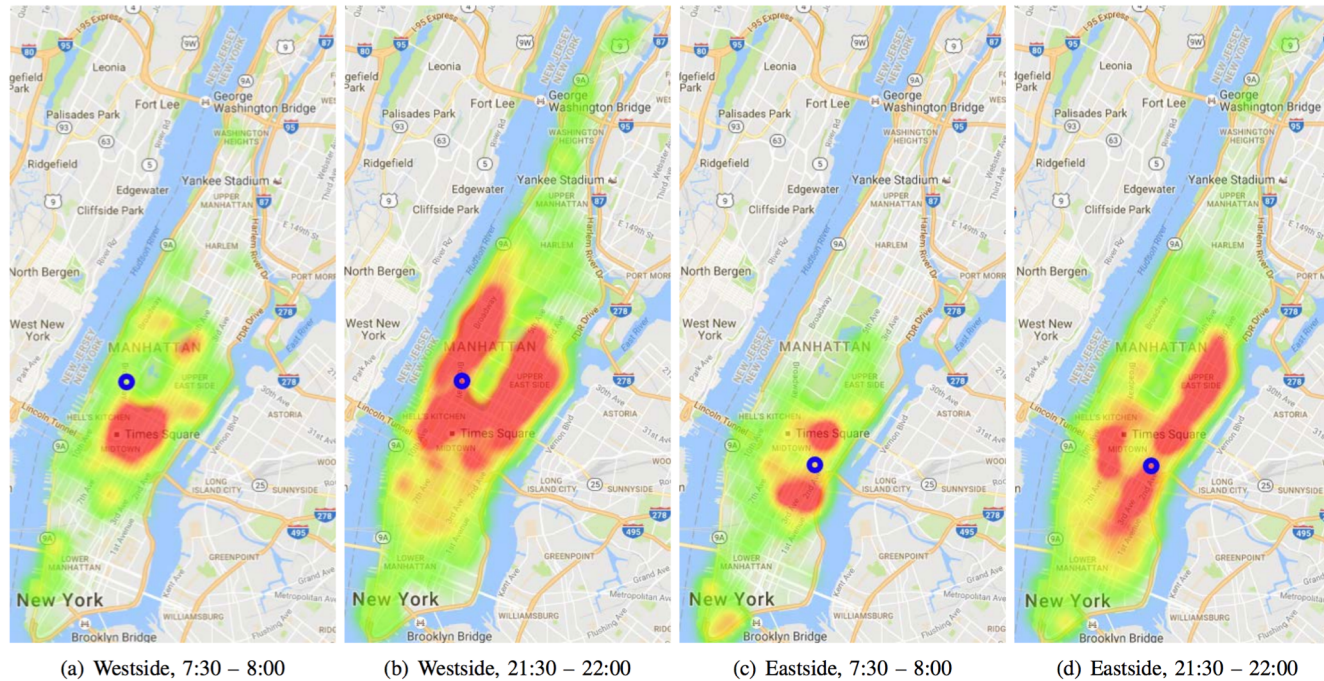


Predictive routing

At peak times mismatch of vehicles & demand

→ **Model of future demand** [from historical data]

$\Pr(\text{destination} \mid \text{origin, time})$



Predictive routing

At peak times mismatch of vehicles & demand

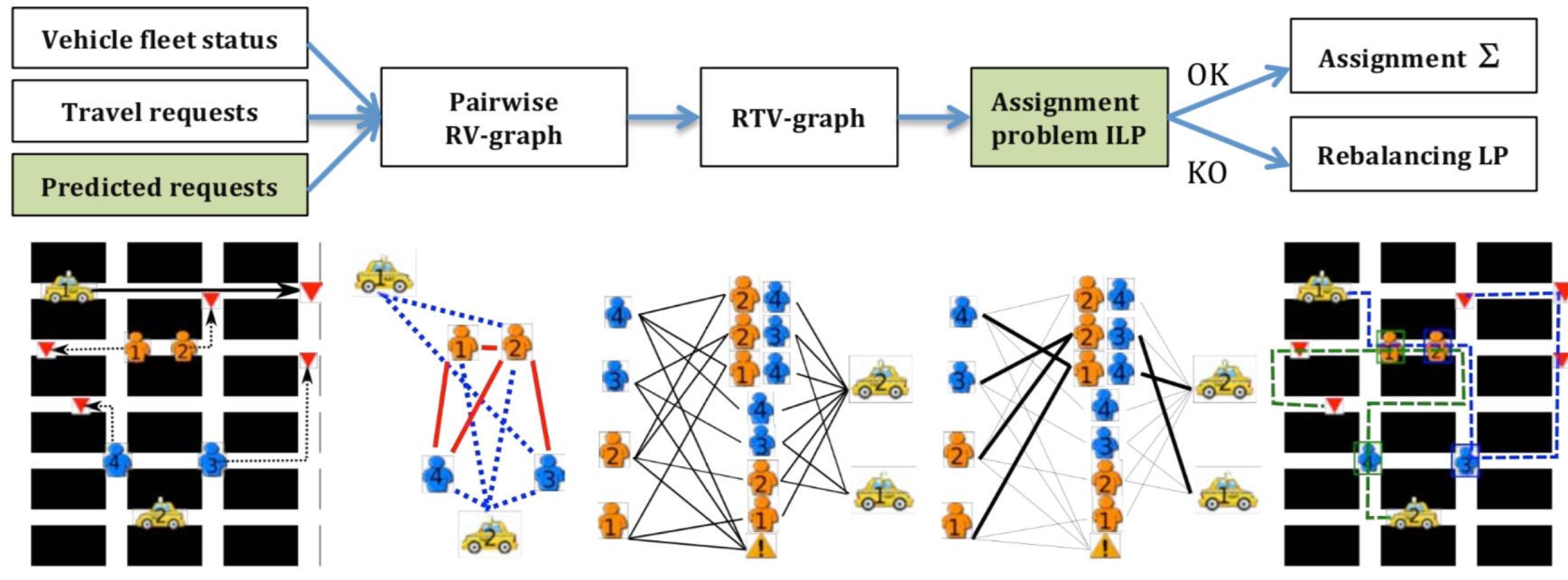
→ **Model of future demand** [from historical data]

→ Better position the vehicles for the future,
by **sampling expected requests**

→ Poor scalability

$\Pr(\text{destination} \mid \text{origin}, \text{time})$

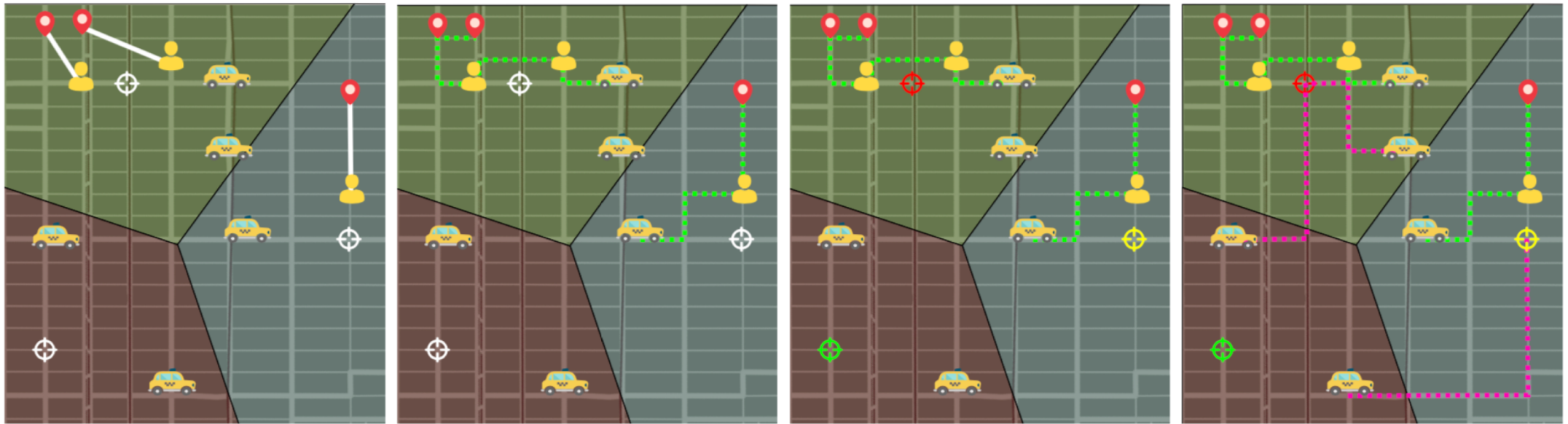
$$C_{now}(\Sigma) + C_{future}(\Sigma)$$



Proactive rebalancing

Estimate vehicle demand per region, based on real-time data

Assign idle vehicles to rebalancing regions using the estimated demand



(a) Initial state

(b) Schedule assignment

(c) Demand estimation

(d) Rebalancer assignment

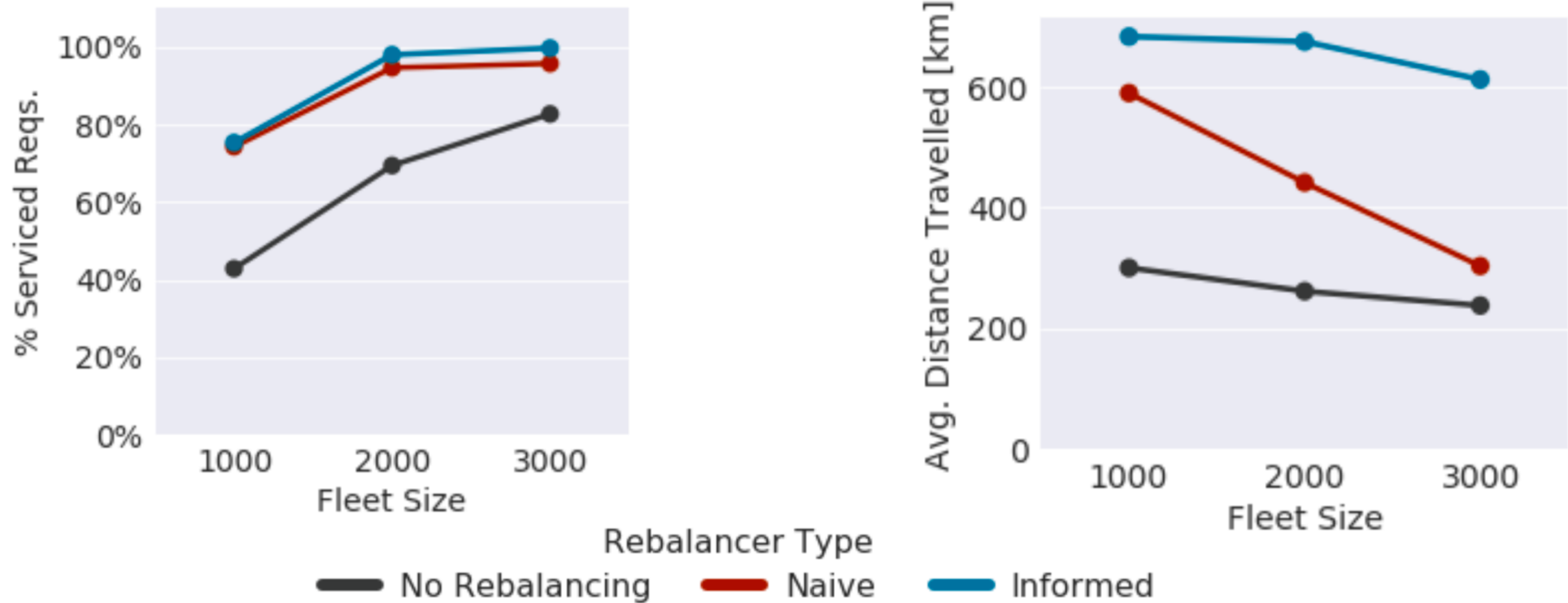
Proactive rebalancing

Estimate vehicle demand per region, based on real-time data

Assign idle vehicles to rebalancing regions using the estimated demand

→ Increase the service rate and reduce the waiting time

→ But, this might come at a cost of (much) **higher distance driven!**



Competing objectives



Quality of Service

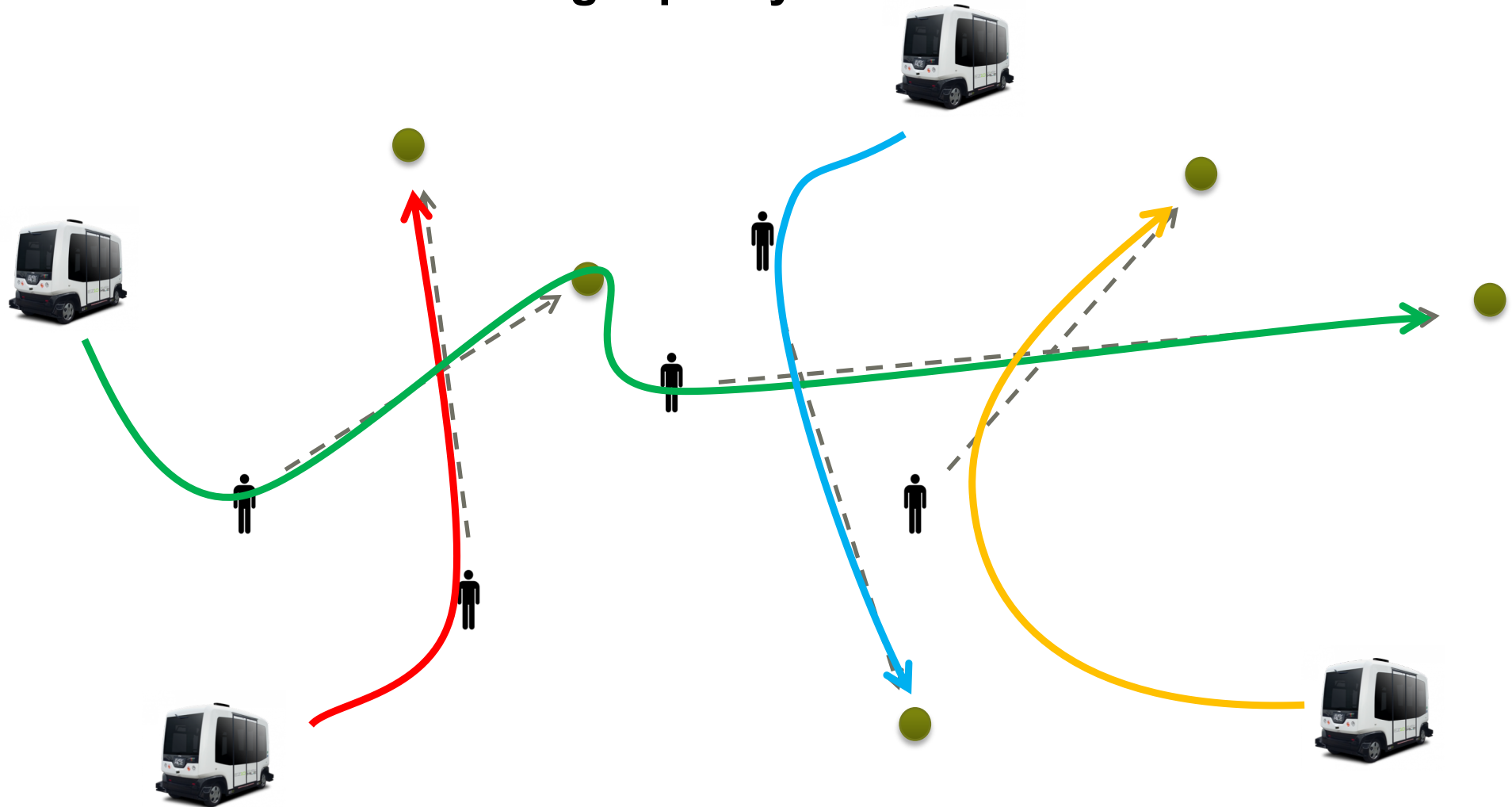


Operation Cost

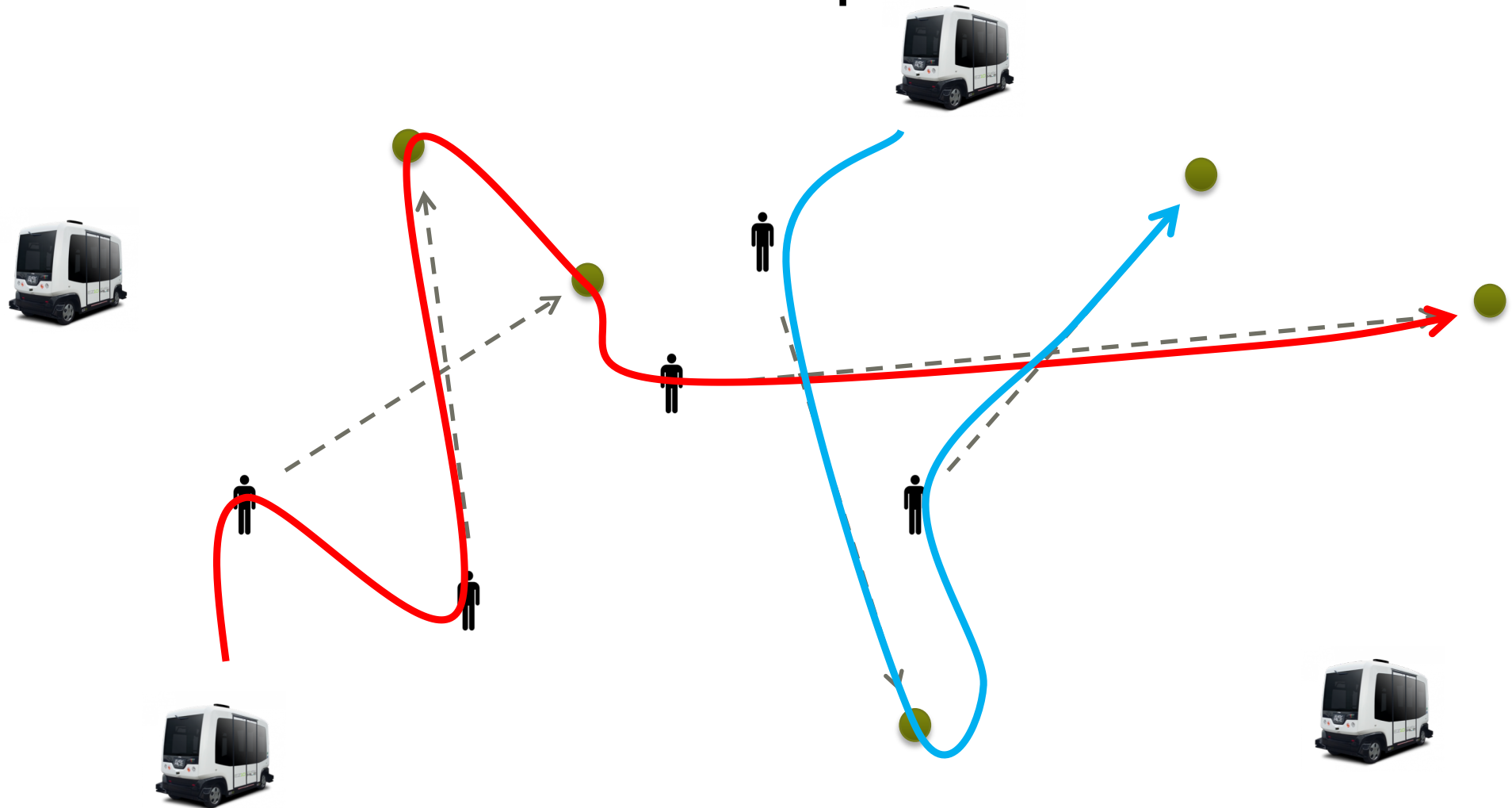
$C_{QoS} :=$ Avg. Passenger Travel Delay

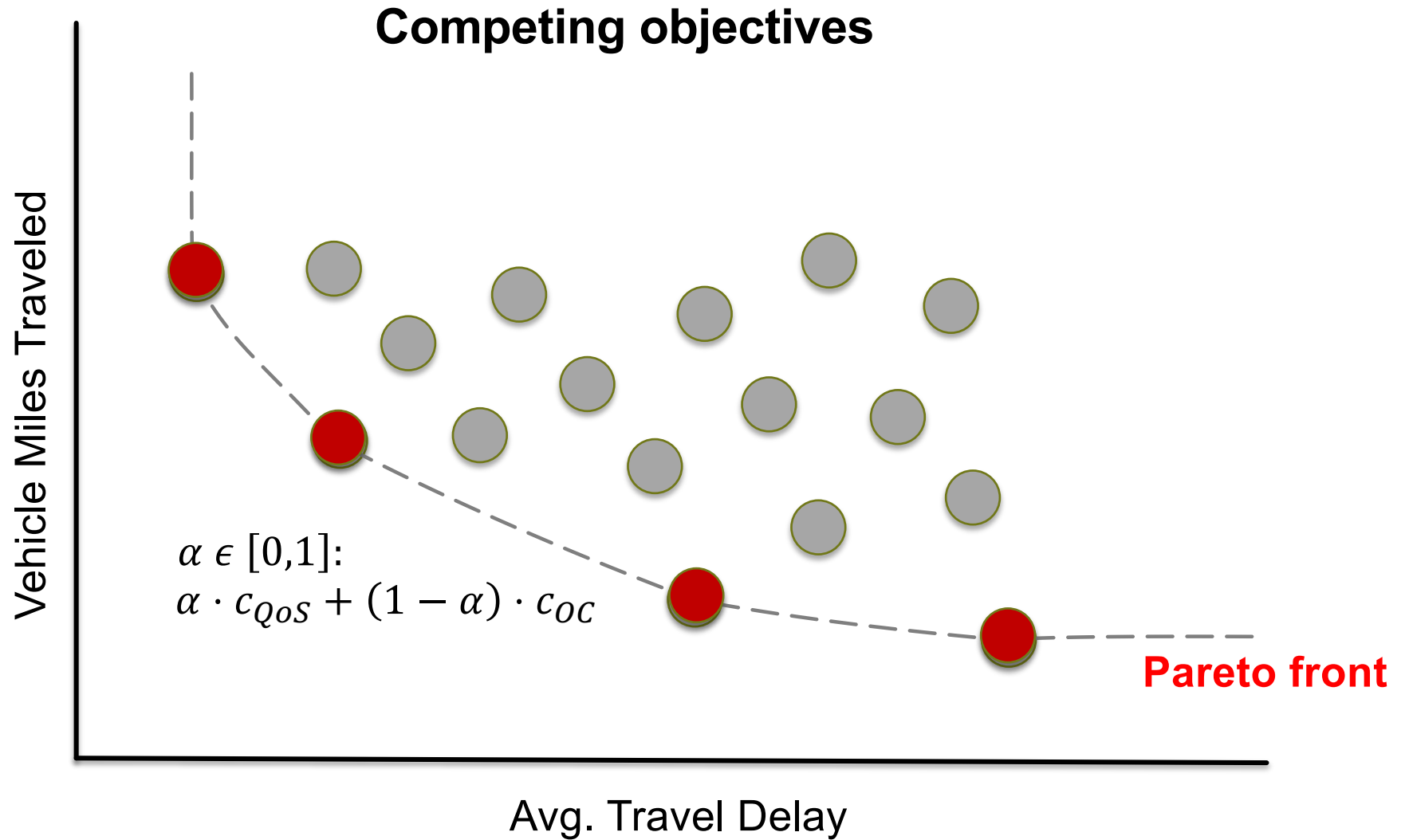
$C_{OC} :=$ Total Vehicle Distance Driven

High quality of service



Low cost of operation





Pareto front

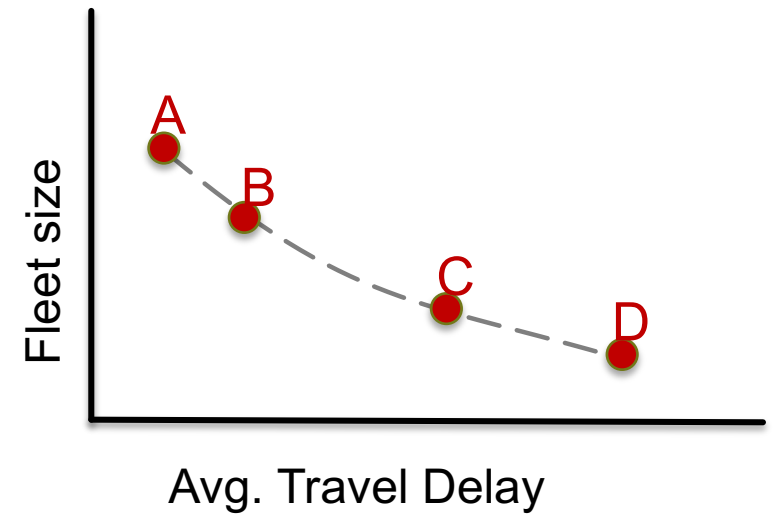
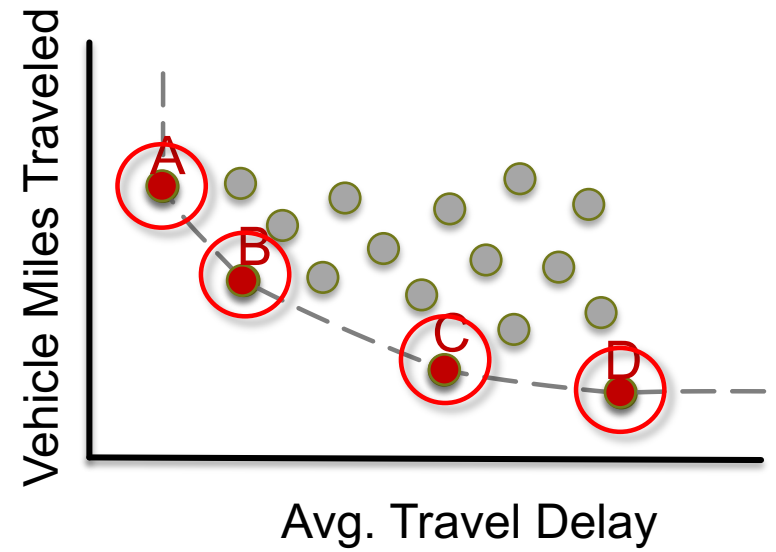
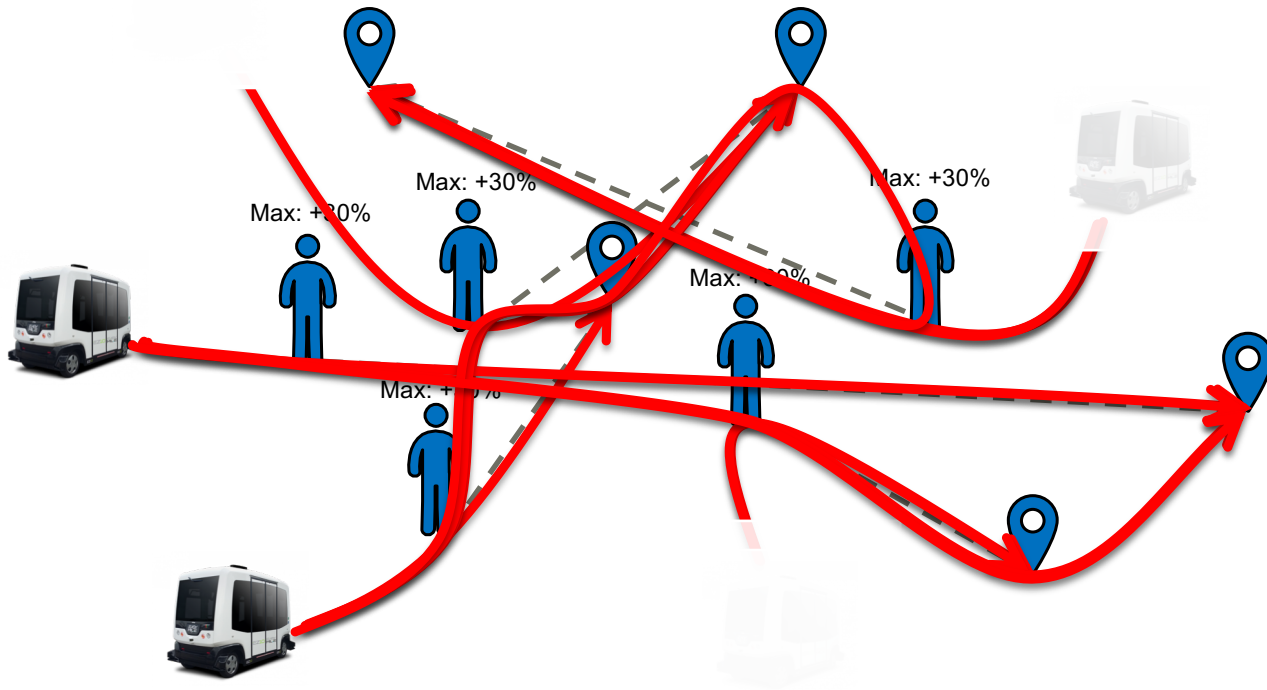


Illustration:

Synthetic travel demand
(50 requests)

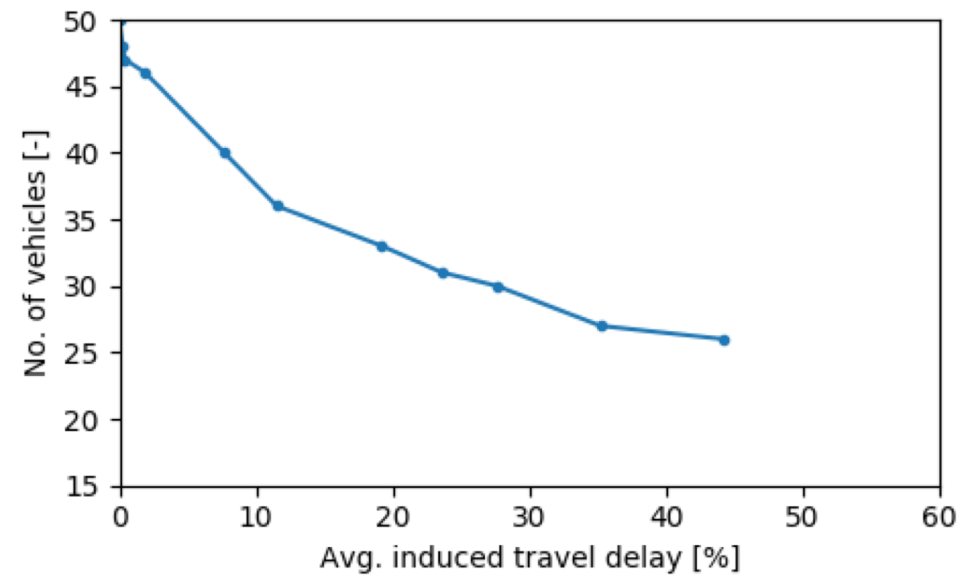
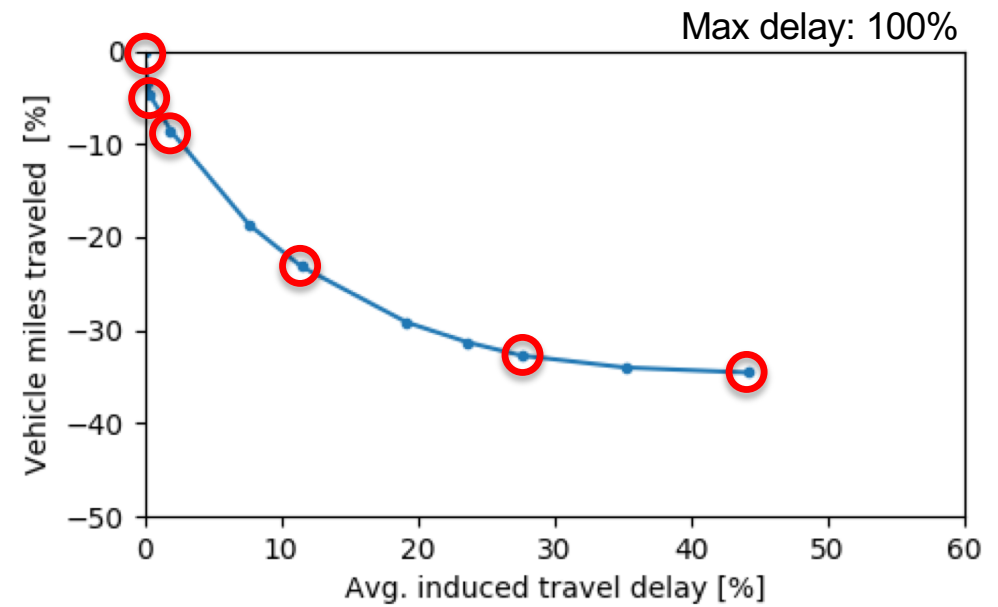
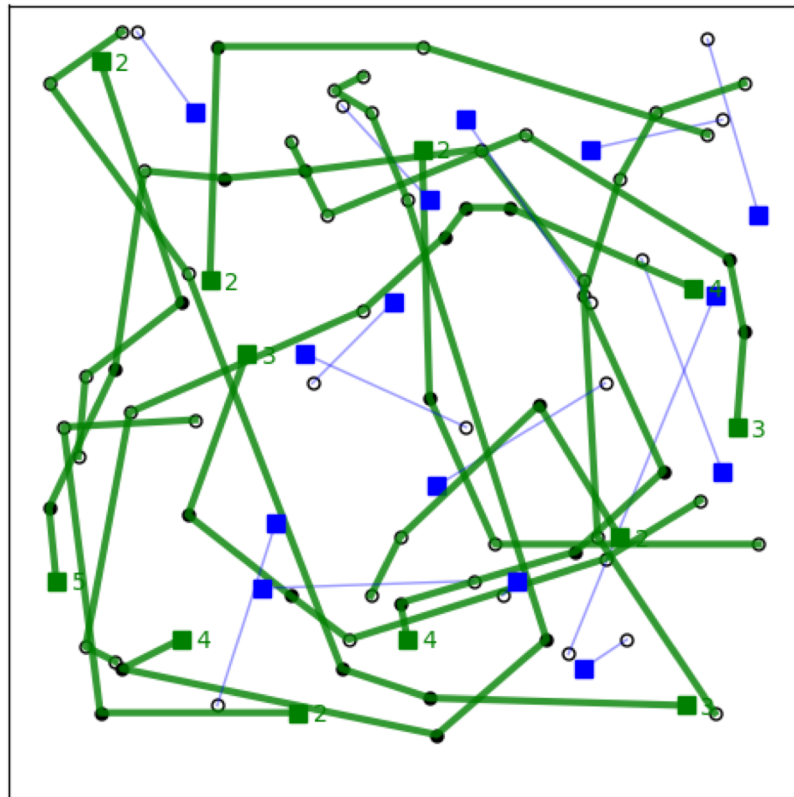


Illustration:
Synthetic travel demand
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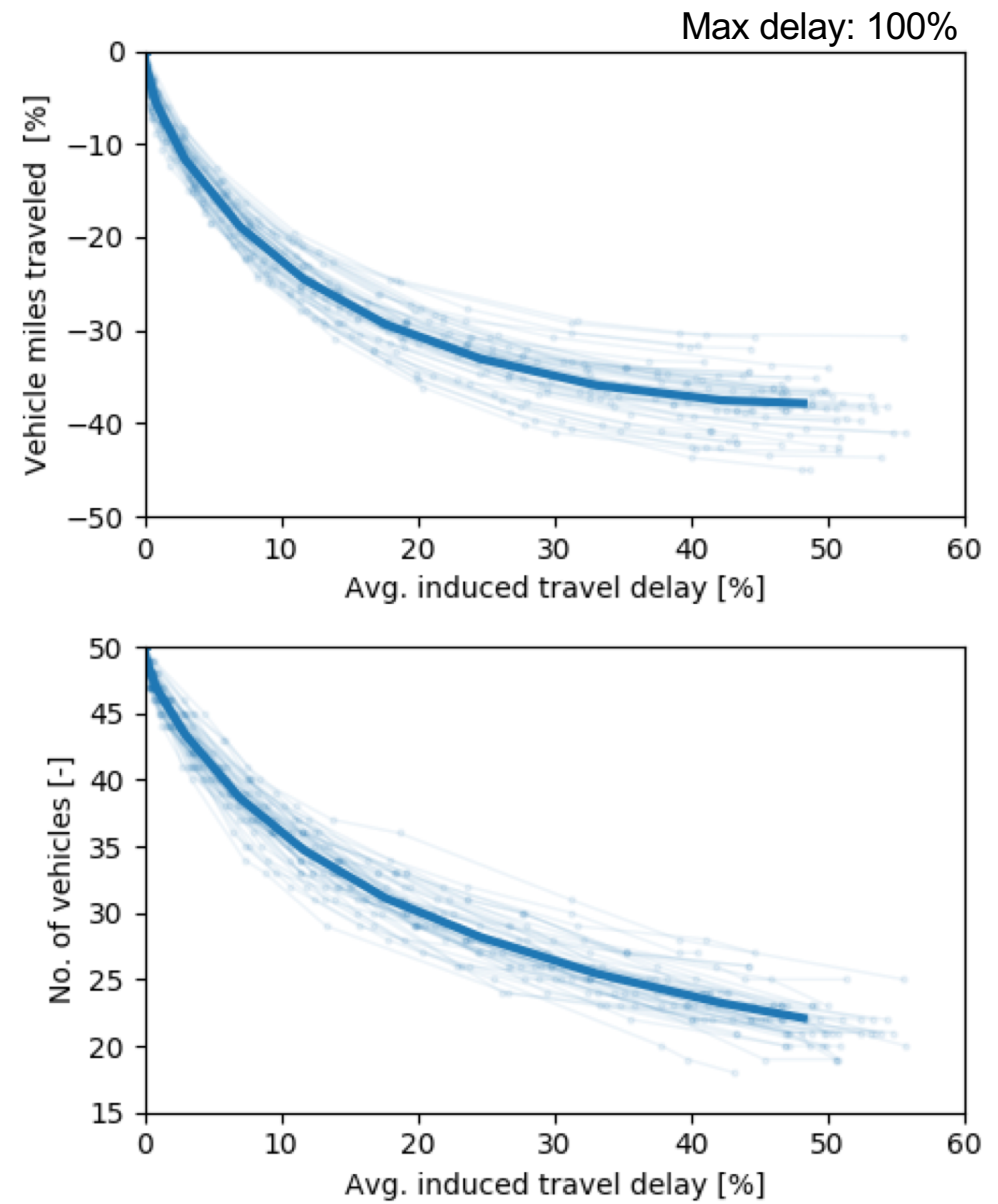
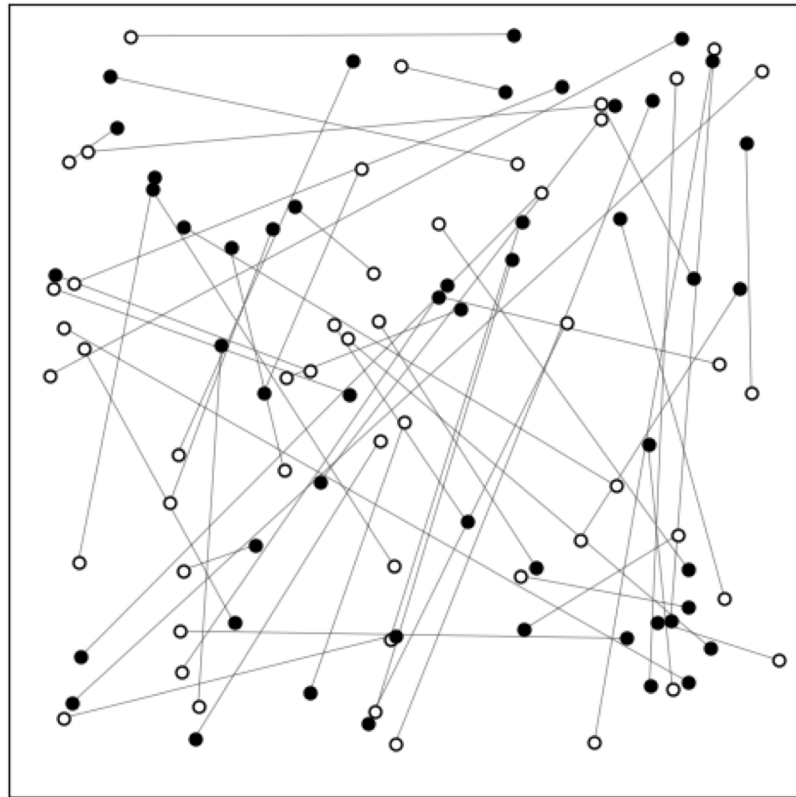
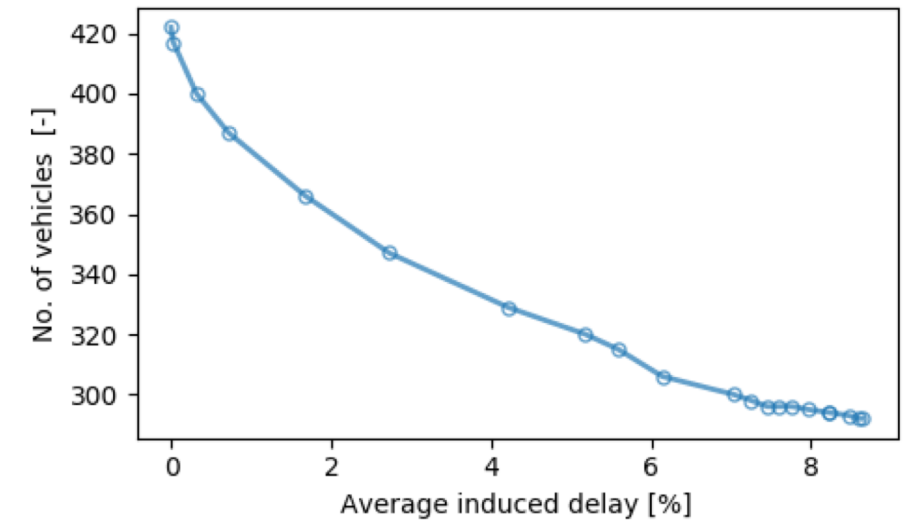
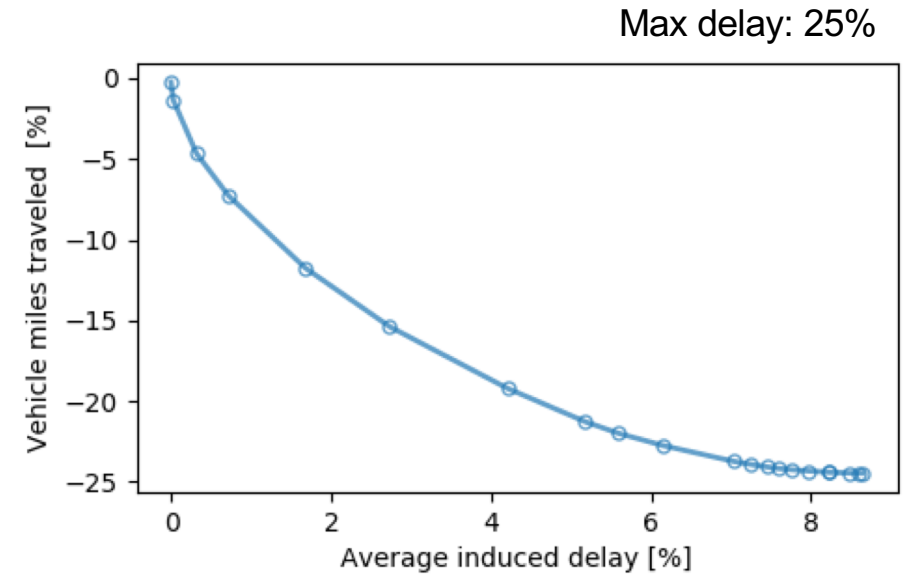
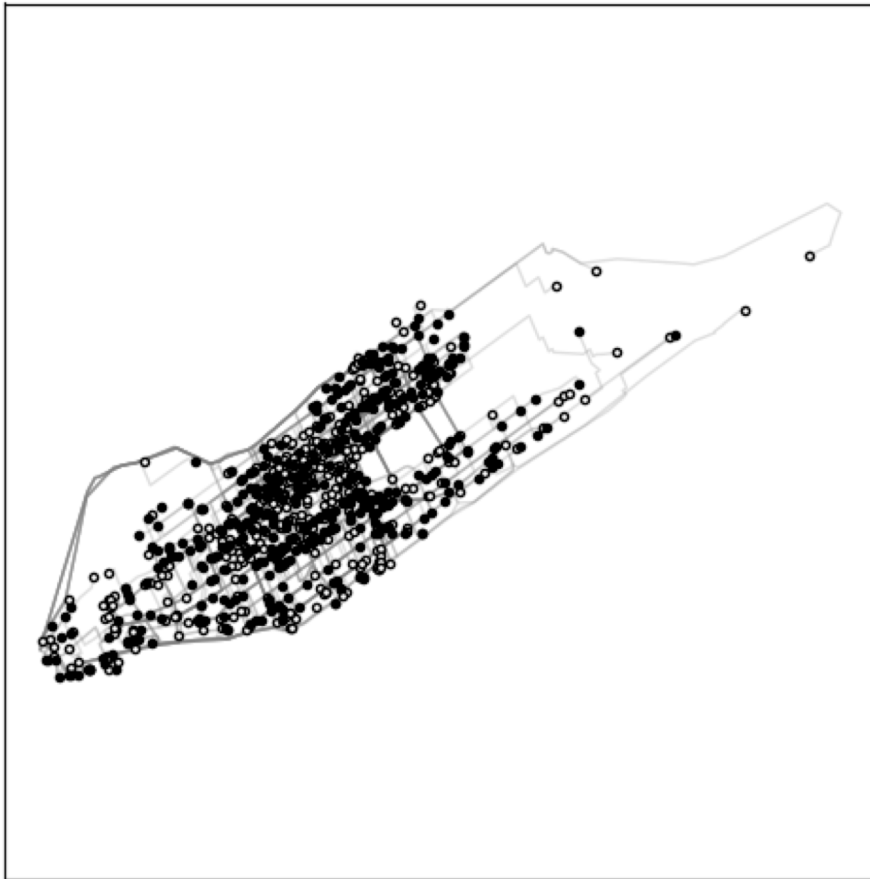


Illustration:

1 minute of Manhattan Taxi Requests
(427 requests)





Number of
vehicles

Fleet size and composition

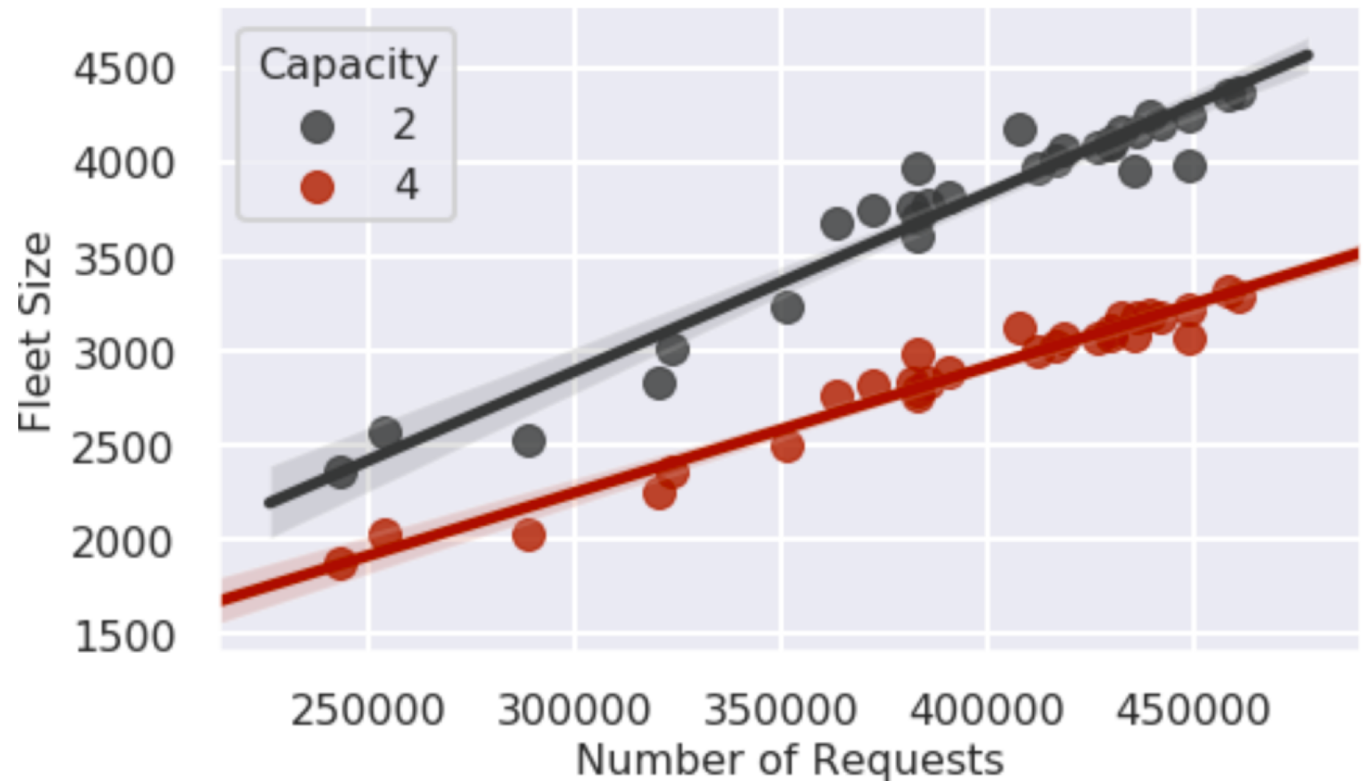
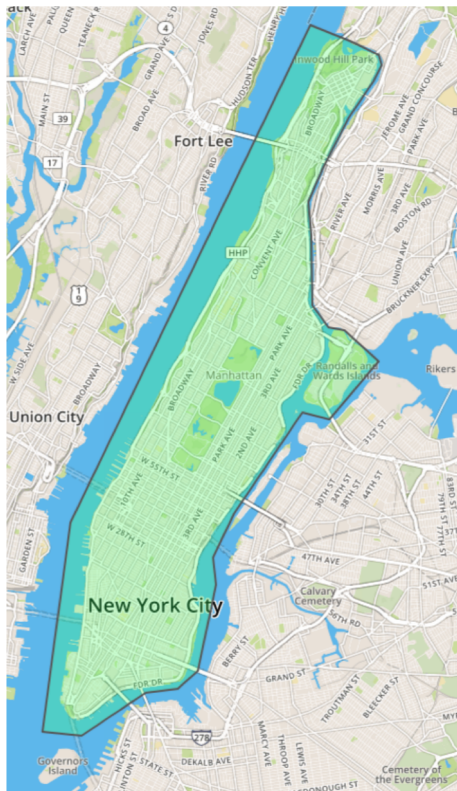
From historical data we can compute the fleet size and composition required for a given day

→ Constraints: service all requests, maximum waiting time and delay

1. Compute a set of deposits, e.g., distance from any point to closest deposit < 1 min
2. In small batches, e.g., 1 h, compute feasible and locally optimal schedules [Similar to RTV]
3. Long term rebalancing (chain schedules from multiple batches) [Max. matching ILP]

Fleet size and composition

From historical data we can compute the fleet size and composition required for a given day
→ Constraints: service all requests, maximum waiting time (3 min) and delay (6 min)



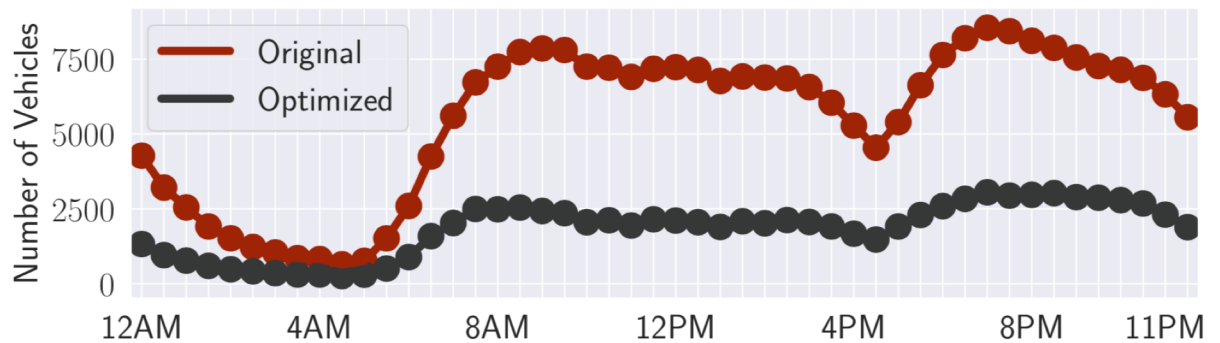
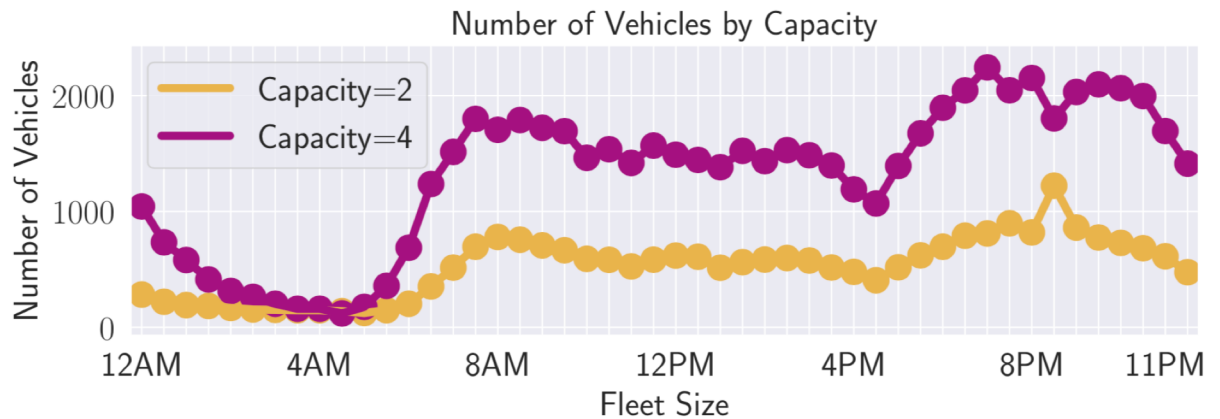
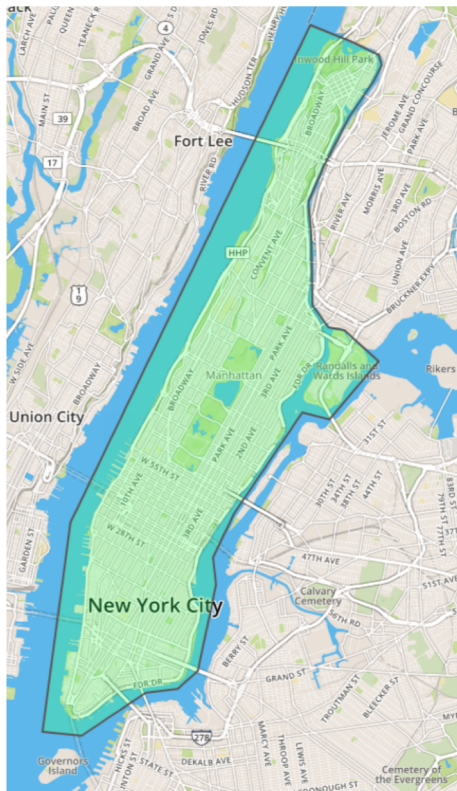
A. Wallar, J. Alonso-Mora and D. Rus, “**Optimizing Vehicle Distributions and Fleet Sizes for Shared Mobility-on-Demand**”, ICRA 2019

A. Wallar et al., “**Optimizing Multi-class Fleet Compositions for Shared Mobility-as-a-Service**”, ITSC 2019

Fleet size and composition [mixed fleet]

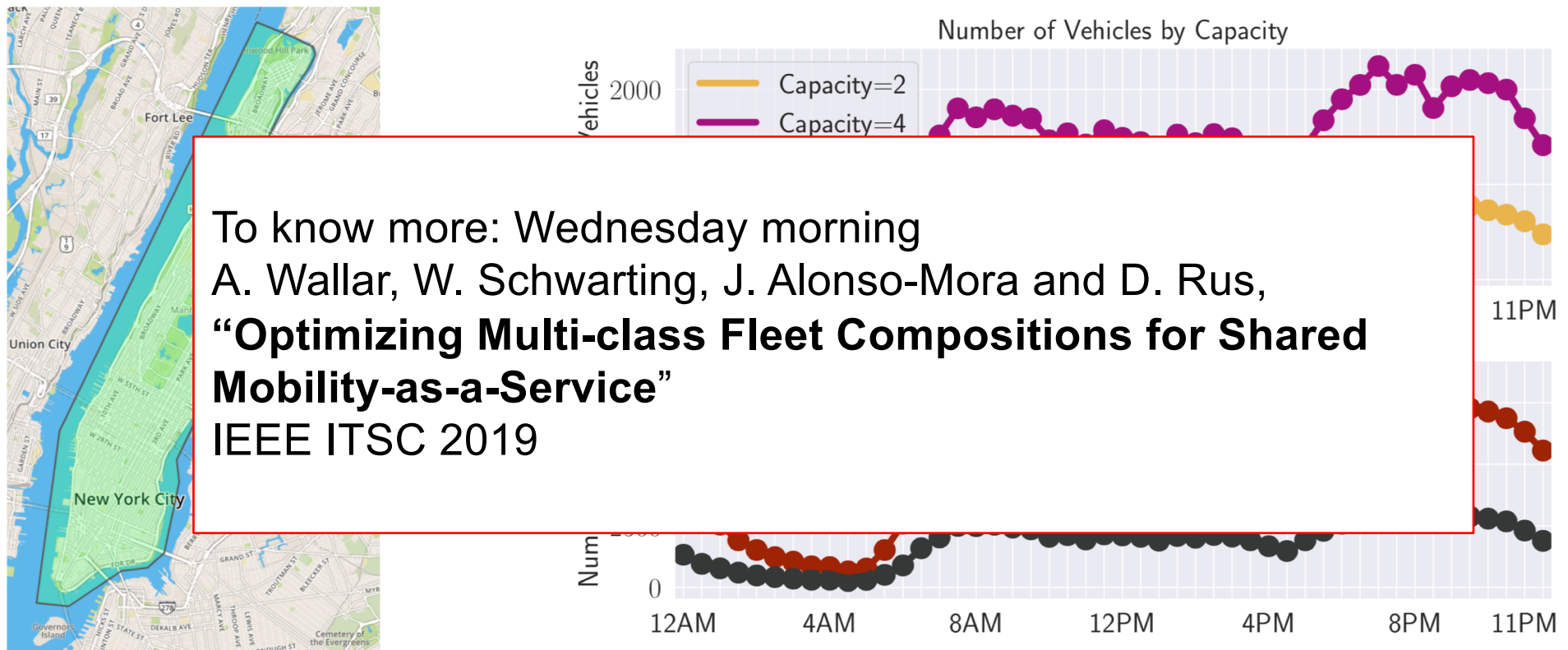
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Fleet size and composition

From historical data we can compute the fleet size and composition required for a given day
→ Constraints: service all requests, maximum waiting time (3 min) and delay (6 min)



Summary

Automated Mobility on Demand with Ride-Sharing

- Online method for high-capacity ride-sharing
- Predictive routing
- Multi-objective analysis
- Fleet sizing

To know more: www.alonsomora.com

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Funding:

