

AA203 Optimal and Learning-based Control

Lecture 16

Model-free RL: Policy optimization

Autonomous Systems Laboratory
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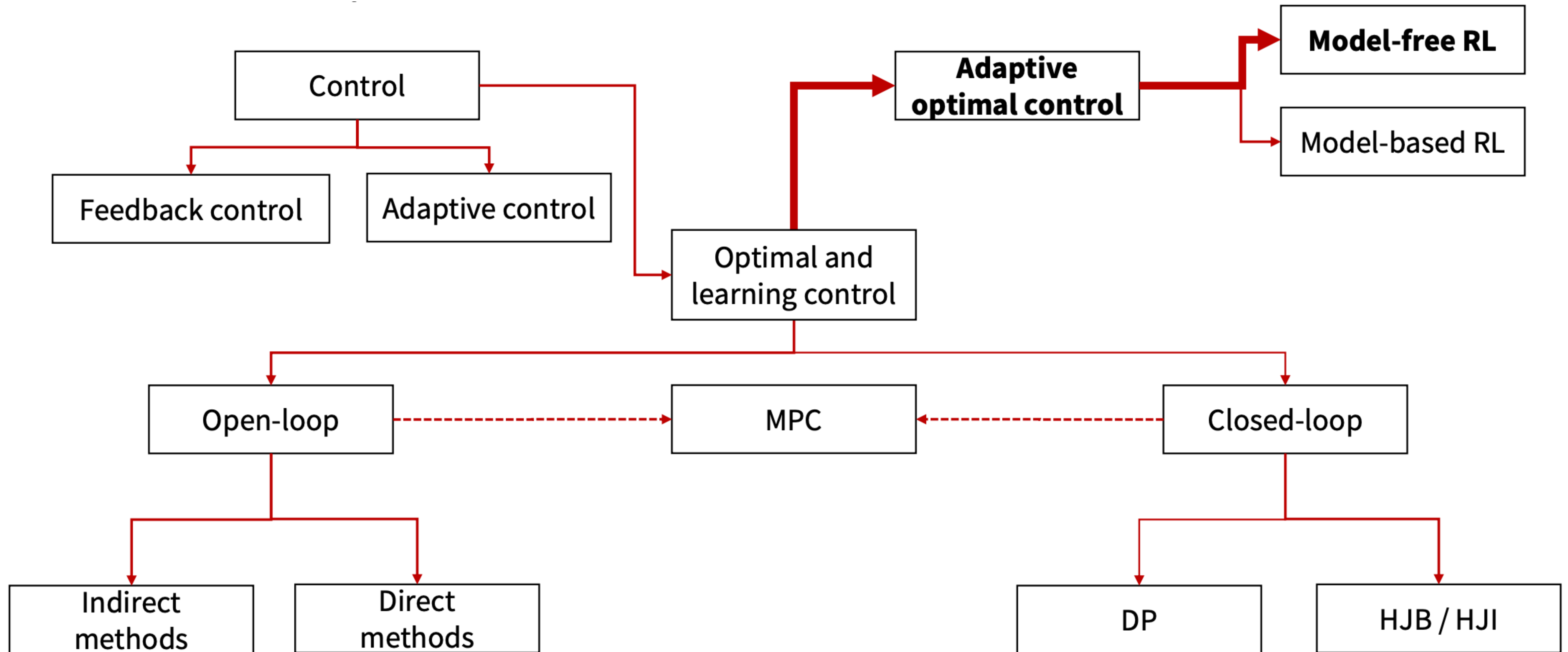


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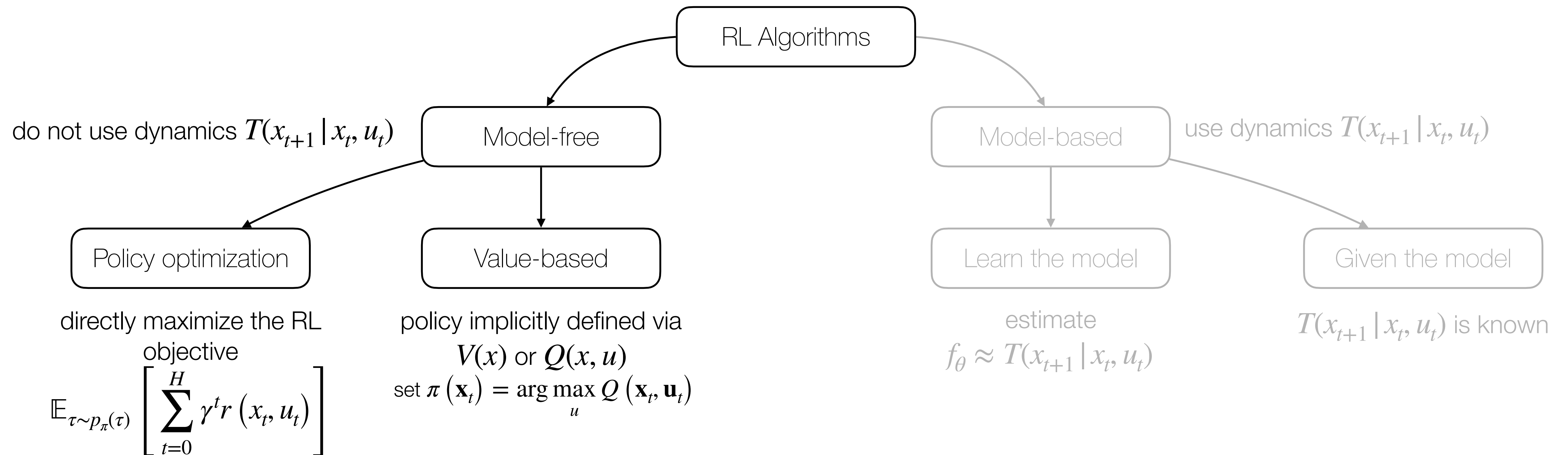


**Autonomous Systems Laboratory
Stanford Aeronautics & Astronautics**

Roadmap



A taxonomy of RL



Outline

Intro to policy gradients

- REINFORCE algorithm
- Reducing variance of policy gradient

Actor-Critic methods

- Advantage
- Architecture design

Deep RL Algorithms & Applications

Outline

Intro to policy gradients

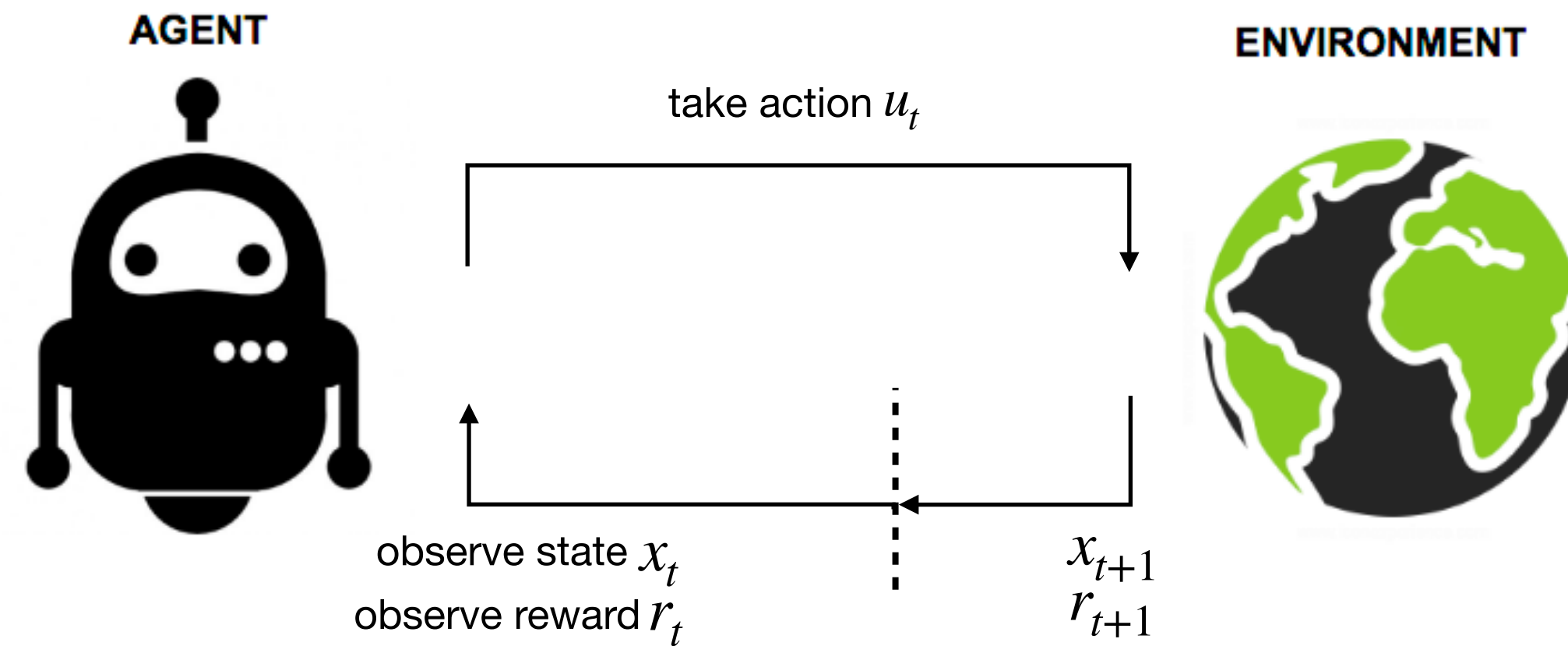
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Deep RL Algorithms & Applications

The goal of reinforcement learning



- The agent interacts with the environment to generate trajectories $\tau = (x_0, u_0, x_1, u_1, \dots, x_T)$
- We define the trajectory distribution

$$p(x_0, u_0, \dots, x_T) = p(\tau) = p(x_0) \prod_{t=1}^T \pi(u_t | x_t) p(x_{t+1} | x_t, u_t)$$

- We can express the RL objective as an expectation under the trajectory distribution

$$\pi^* = \arg \max_{\pi} \mathbb{E}_{\tau \sim p(\tau)} \left[\sum_{t \geq 0} \gamma^t R(x_t, u_t) \right]$$

Policy Optimization

- In policy optimization, we care about learning an (explicit) parametric policy π_θ , with parameters θ
- In light of this, we can re-write the Eqs from the previous slide w.r.t. θ :

$$p(x_0, u_0, \dots, x_T) = p(\tau) = p(x_0) \prod_{t=1}^T \pi_\theta(u_t | x_t) p(x_{t+1} | x_t, u_t)$$
$$\theta^* = \arg \max_{\pi} \underbrace{\mathbb{E}_{\tau \sim p(\tau)} \left[\sum_{t \geq 0} \gamma^t R(x_t, u_t) \right]}_{J(\theta)}$$

To simplify the notation, we'll ignore discounting for now ($\gamma = 1$) and consider

$$\theta^* = \arg \max_{\pi} \underbrace{\mathbb{E}_{\tau \sim p(\tau)} \left[\sum_{t \geq 0} R(x_t, u_t) \right]}_{J(\theta)}$$

Evaluating the objective

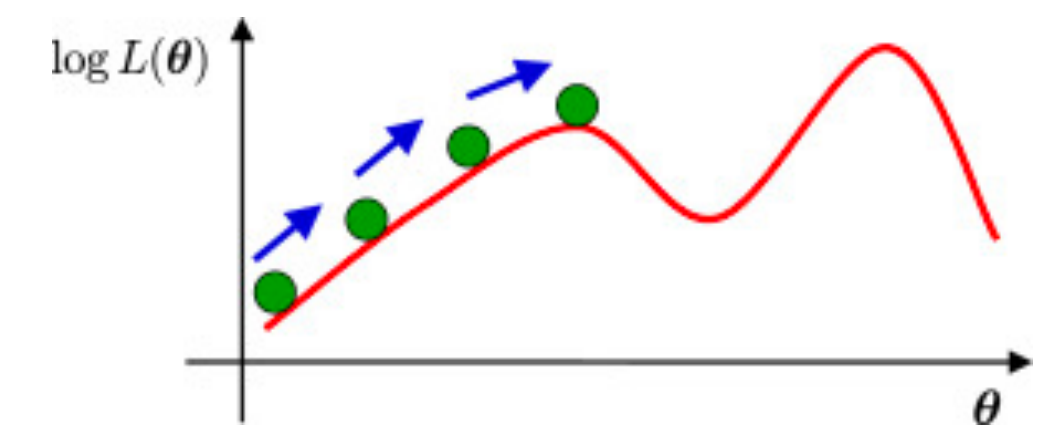
- Opposed to value-based methods, policy optimization attempts to learn the policy directly (i.e., optimize $J(\theta)$ w.r.t. θ)

$$J(\theta) = \mathbb{E}_{\tau \sim p(\tau)} \left[\sum_{t \geq 0} R(x_t, u_t) \right]$$

One of the most direct ways to optimize this objective is to:

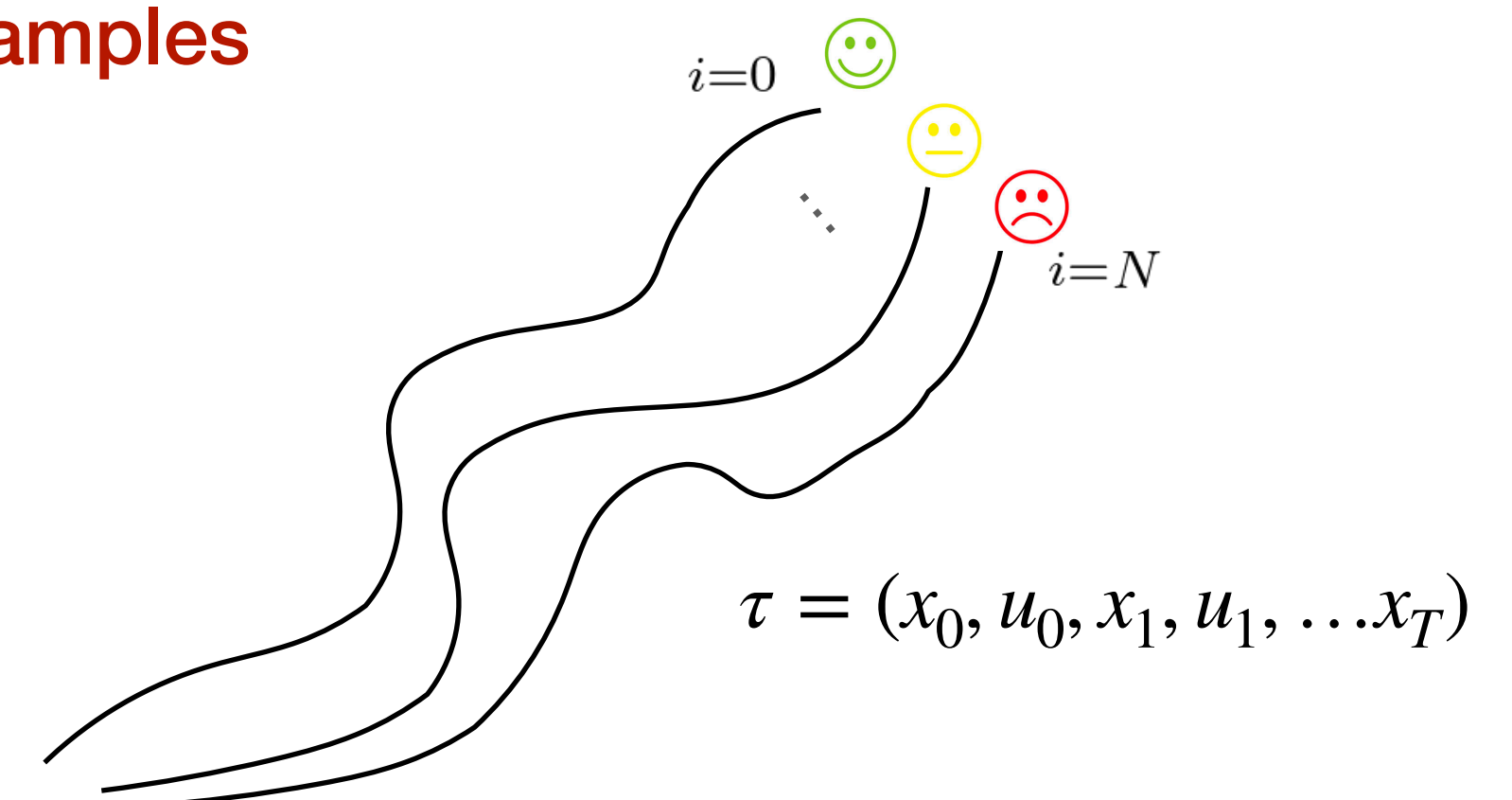
(1) estimate its gradient $\nabla_{\theta} J(\theta)$

(2) cast the learning process as approximate gradient ascent on $J(\theta)$ $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$



How can we evaluate the expectation in the objective? As usual in RL, **through samples**

$$J(\theta) = \mathbb{E}_{\tau \sim p(\tau)} \left[\sum_{t \geq 0} R(x_t, u_t) \right] \approx \frac{1}{N} \sum_i \sum_t R(x_{i,t}, u_{i,t})$$



Direct policy gradient

- In order to solve the problem through gradient-based optimization we need to compute $\nabla_{\theta} J(\theta)$

- Let us define the compact notation $r(\tau) = \sum_{t=1}^T R(x_t, u_t)$

- By definition of expectation $J(\theta) = \mathbb{E}_{\tau \sim p(\tau)} [r(\tau)] = \int p_{\theta}(\tau) r(\tau) d\tau$

- We can then write the gradient $\nabla_{\theta} J(\theta) = \int \nabla_{\theta} p_{\theta}(\tau) r(\tau) d\tau$

Problem: gradient depends on unknown dynamics and initial state distribution through $p_{\theta}(\tau)$

Useful identity:

$$p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) = p_{\theta}(\tau) \frac{\nabla_{\theta} p_{\theta}(\tau)}{p_{\theta}(\tau)} = \nabla_{\theta} p_{\theta}(\tau)$$

$$\nabla_{\theta} J(\theta) = \int \nabla_{\theta} p_{\theta}(\tau) r(\tau) d\tau = \int p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) r(\tau) d\tau = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} [\nabla_{\theta} \log p_{\theta}(\tau) r(\tau)]$$

On the right track since we can evaluate expectations through samples... but we still have $\nabla_{\theta} \log p_{\theta}(\tau)$

Direct policy gradient

Let us recall the trajectory distribution

$$p(x_0, u_0, \dots, x_T) = p(\tau) = p(x_0) \prod_{t=1}^T \pi(u_t | x_t) p(x_{t+1} | x_t, u_t)$$

$$\log p(\tau) = \log p(x_0) + \sum_{t=1}^T \log \pi_{\theta}(u_t | x_t) + \log p(x_{t+1} | x_t, u_t)$$

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} \left[\nabla_{\theta} \log p_{\theta}(\tau) r(\tau) \right] = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} \left[\nabla_{\theta} \left[\cancel{\log p(x_0)} + \sum_{t=1}^T \log \pi_{\theta}(u_t | x_t) + \cancel{\log p(x_{t+1} | x_t, u_t)} \right] r(\tau) \right]$$

- When taking the gradient w.r.t. θ , $\log p(x_0)$, $\log p(x_{t+1} | x_t, u_t)$ do not depend on θ
- While we can evaluate the log probability under our parametric policy π_{θ}
- This enable us to re-write the gradient $\nabla_{\theta} J(\theta)$ as:

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} \left[\left(\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_t | x_t) \right) \left(\sum_{t=1}^T R(x_t, u_t) \right) \right]$$

Everything inside this expectation is known

Direct policy gradient

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} \left[\left(\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_t | x_t) \right) \left(\sum_{t=1}^T R(x_t, u_t) \right) \right]$$

Everything inside this expectation is known

- Recall how we use samples to evaluate the objective: $J(\theta) = \mathbb{E}_{\tau \sim p(\tau)} \left[\sum_{t \geq 0} R(x_t, u_t) \right] \approx \frac{1}{N} \sum_i \sum_t R(x_{i,t}, u_{i,t})$
- We can use the same idea to evaluate the gradient:

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \left[\left(\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \right) \left(\sum_{t=1}^T R(x_{i,t}, u_{i,t}) \right) \right]$$

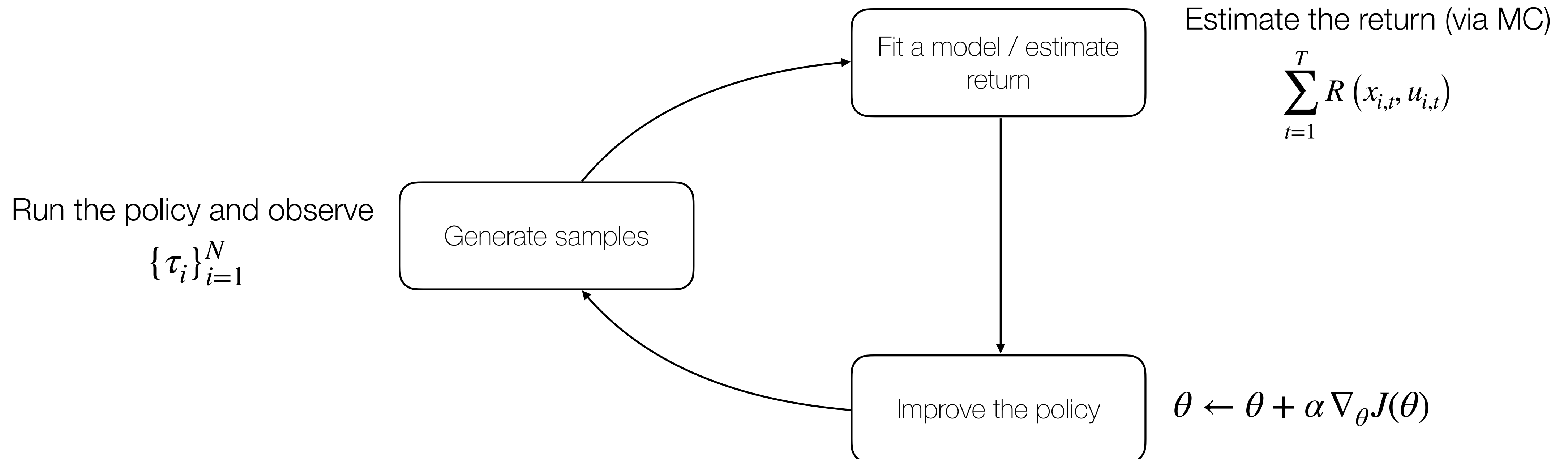
REINFORCE algorithm

The procedure described so far gives us the basic policy gradient algorithms, a.k.a. REINFORCE:

1. Sample trajectories $\{\tau_i\}_{i=1}^N$ from $\pi_\theta(u_t | x_t)$, i.e. run the policy in the environment

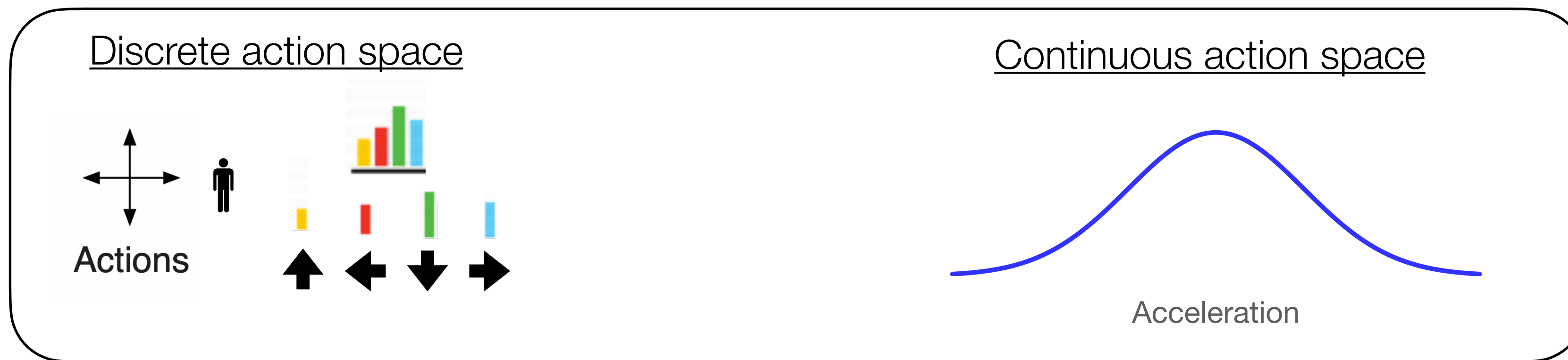
2. Evaluate the policy gradient $\nabla_\theta J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \left[\left(\sum_{t=1}^T \nabla_\theta \log \pi_\theta(u_{i,t} | x_{i,t}) \right) \left(\sum_{t=1}^T R(x_{i,t}, u_{i,t}) \right) \right]$

3. Take a gradient step to update the policy $\theta \leftarrow \theta + \alpha \nabla_\theta J(\theta)$

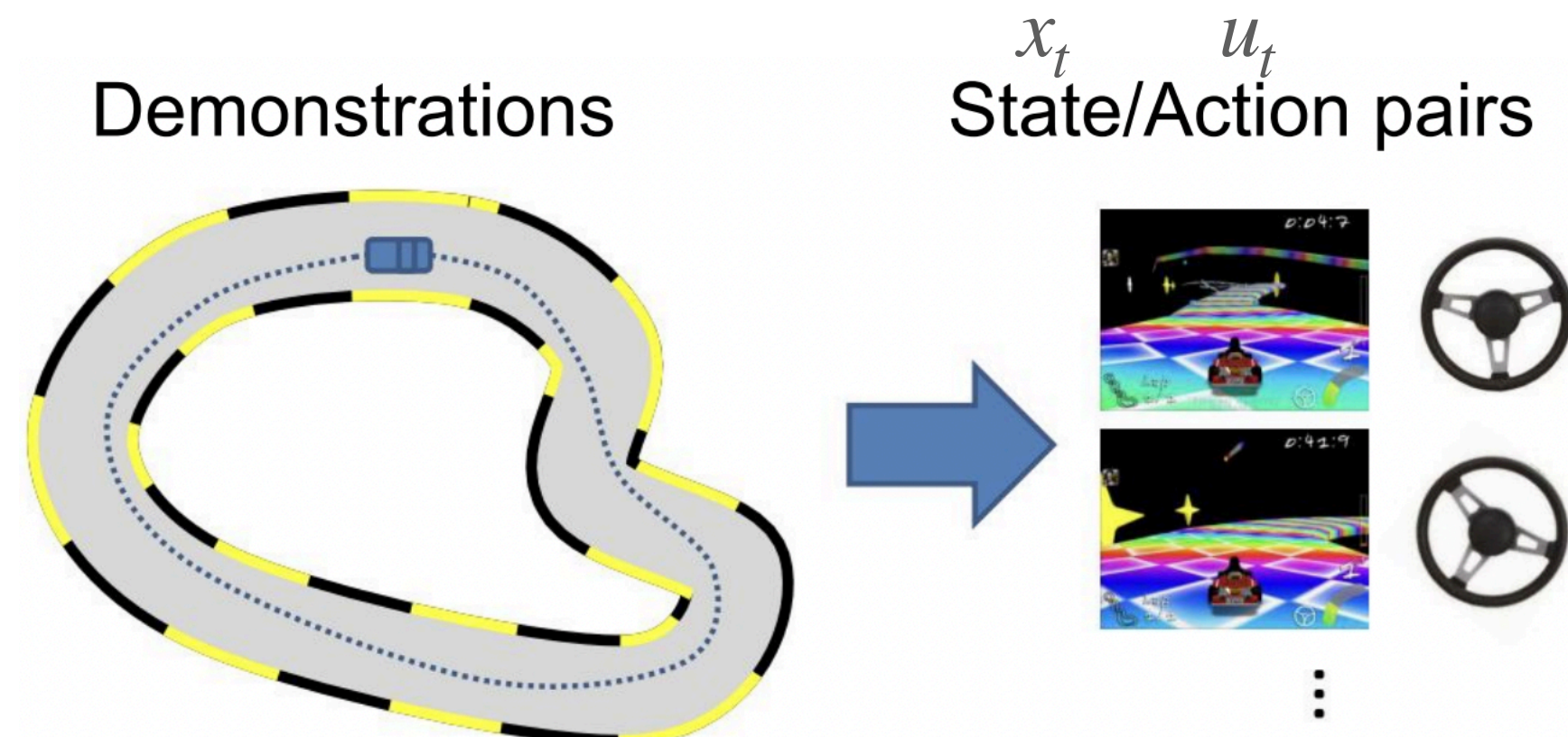


Intuition: “what is PG doing?”

Consider the expression we derived for the policy gradient $\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \left[\left(\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \right) \left(\sum_{t=1}^T R(x_{i,t}, u_{i,t}) \right) \right]$



Let’s compare it with the expression of the gradient when performing maximum likelihood (e.g., supervised learning):



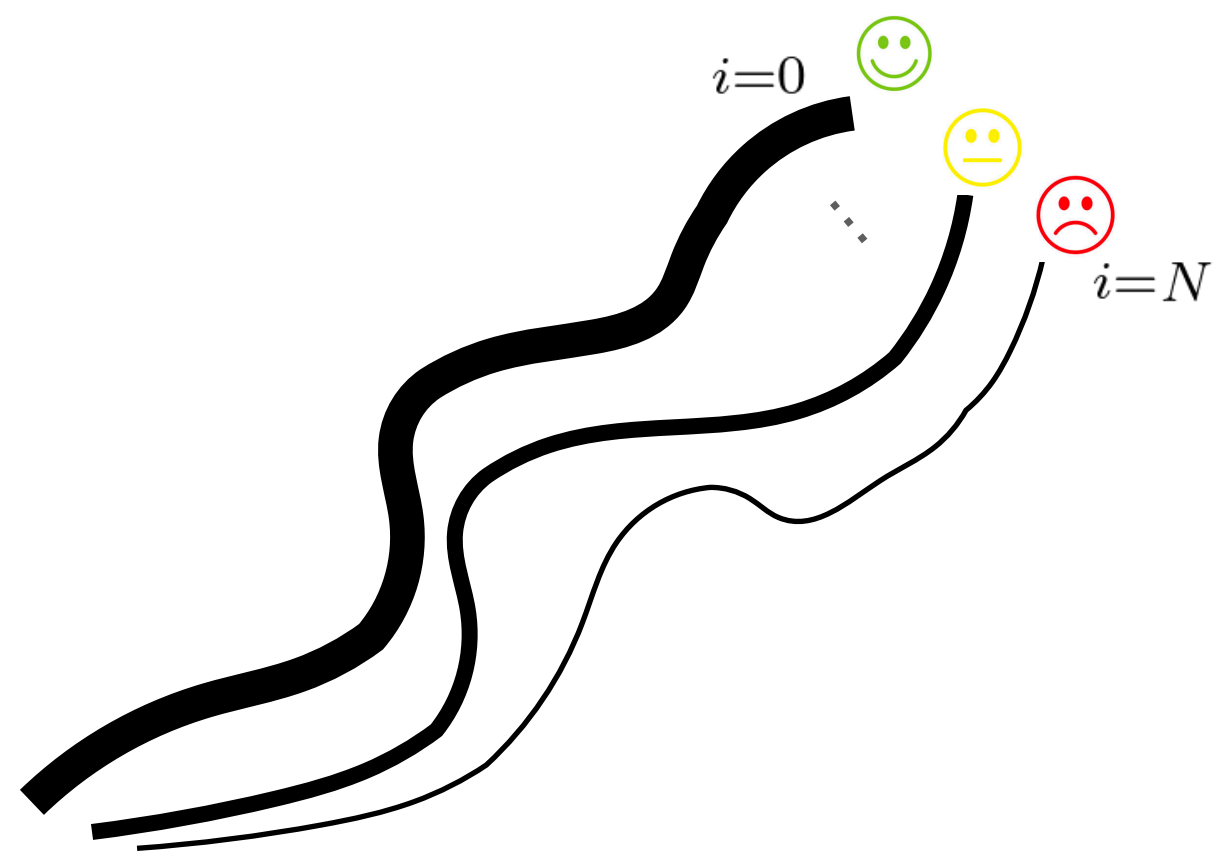
$$\nabla_{\theta} J_{MLE}(\theta) \approx \frac{1}{N} \sum_{i=1}^N \left[\left(\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \right) \right]$$

The policy gradient is a weighted version of the MLE gradient

Intuition: “what is PG doing?”

Policy gradient:
$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \left[\left(\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \right) \left(\sum_{t=1}^T R(x_{i,t}, u_{i,t}) \right) \right]$$

Maximum Likelihood:
$$\nabla_{\theta} J_{MLE}(\theta) \approx \frac{1}{N} \sum_{i=1}^N \left[\left(\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \right) \right]$$



Taking a step in the direction the policy gradient essentially means:

$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\pi_{\theta})$$

“Change parameters θ s.t. trajectories with higher reward have higher probability”

PG formalizes the idea of learning by “trial and error”

Outline

Intro to policy gradients

- REINFORCE algorithm
- Reducing variance of policy gradient

Actor-Critic methods

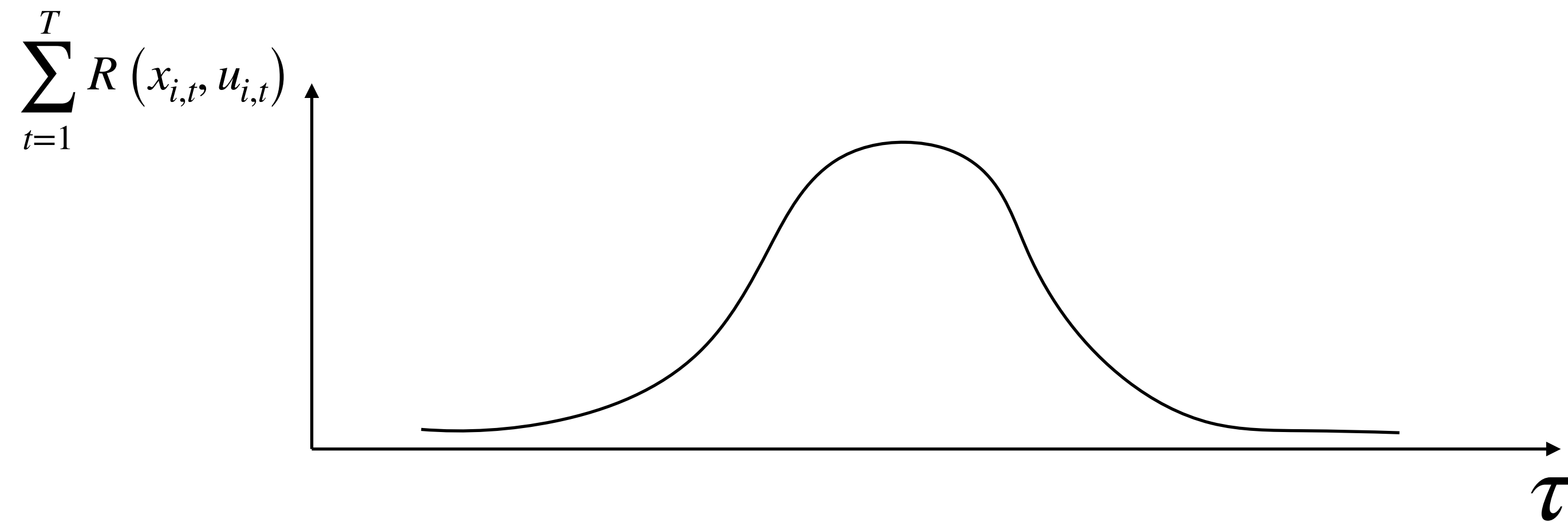
- Advantage
- Architecture design

Deep RL Algorithms & Applications

Problem: high variance of the PG

$$\text{Policy gradient: } \nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \left[\left(\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \right) \left(\sum_{t=1}^T R(x_{i,t}, u_{i,t}) \right) \right]$$

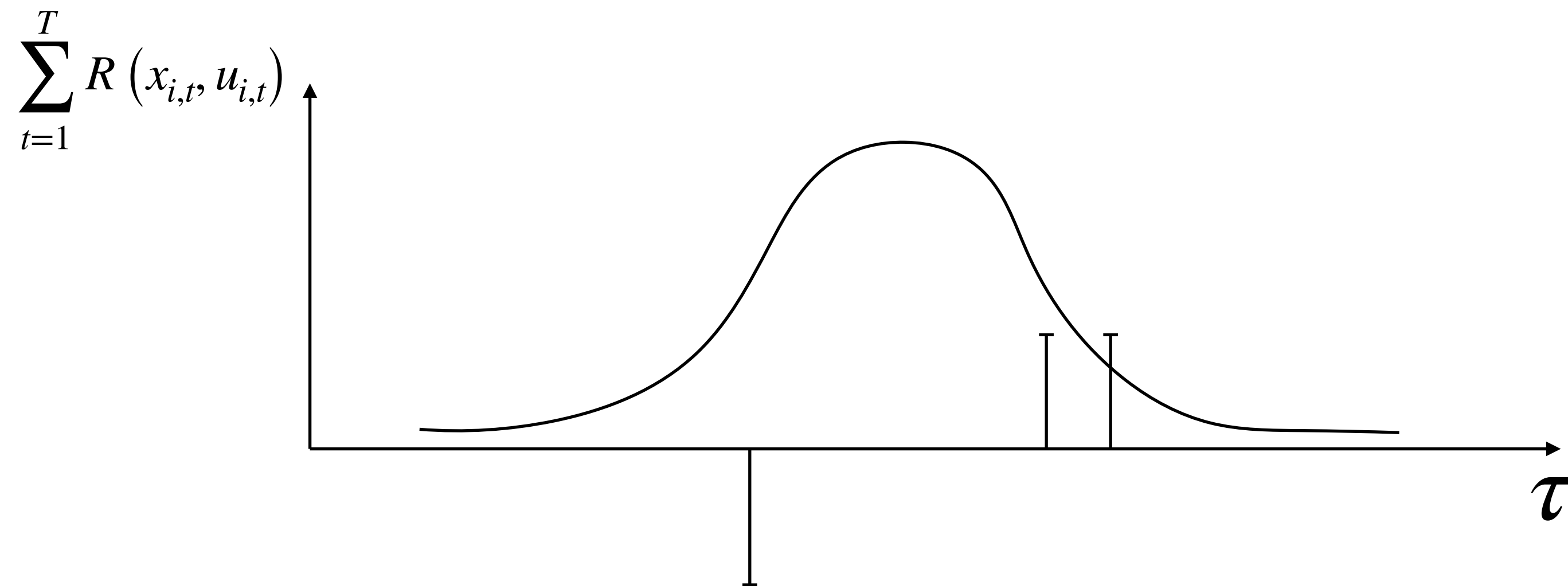
Let's consider the following example:



Problem: high variance of the PG

$$\text{Policy gradient: } \nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \left[\left(\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \right) \left(\sum_{t=1}^T R(x_{i,t}, u_{i,t}) \right) \right]$$

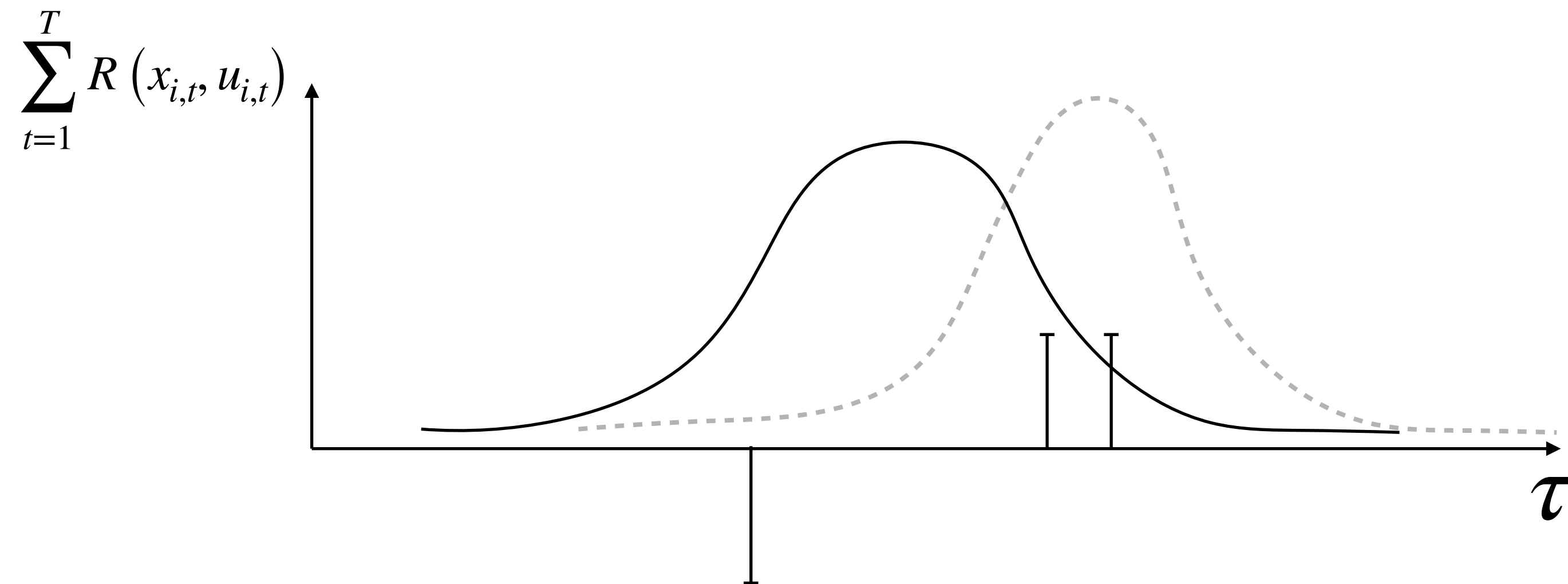
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Problem: high variance of the PG

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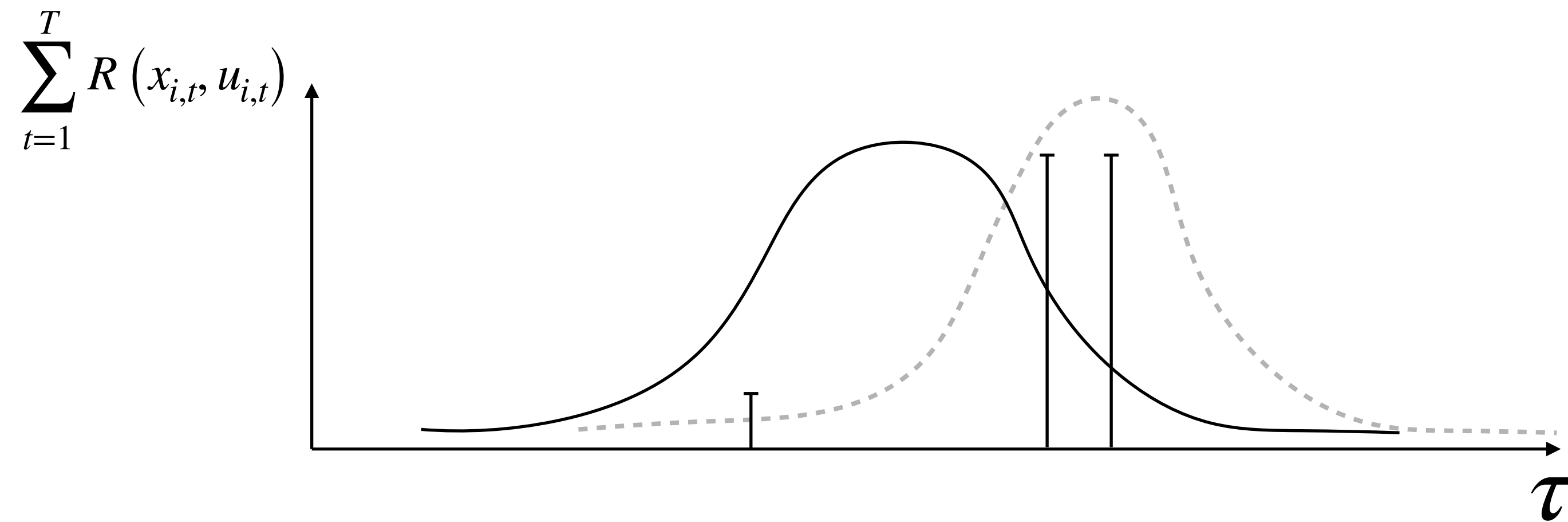
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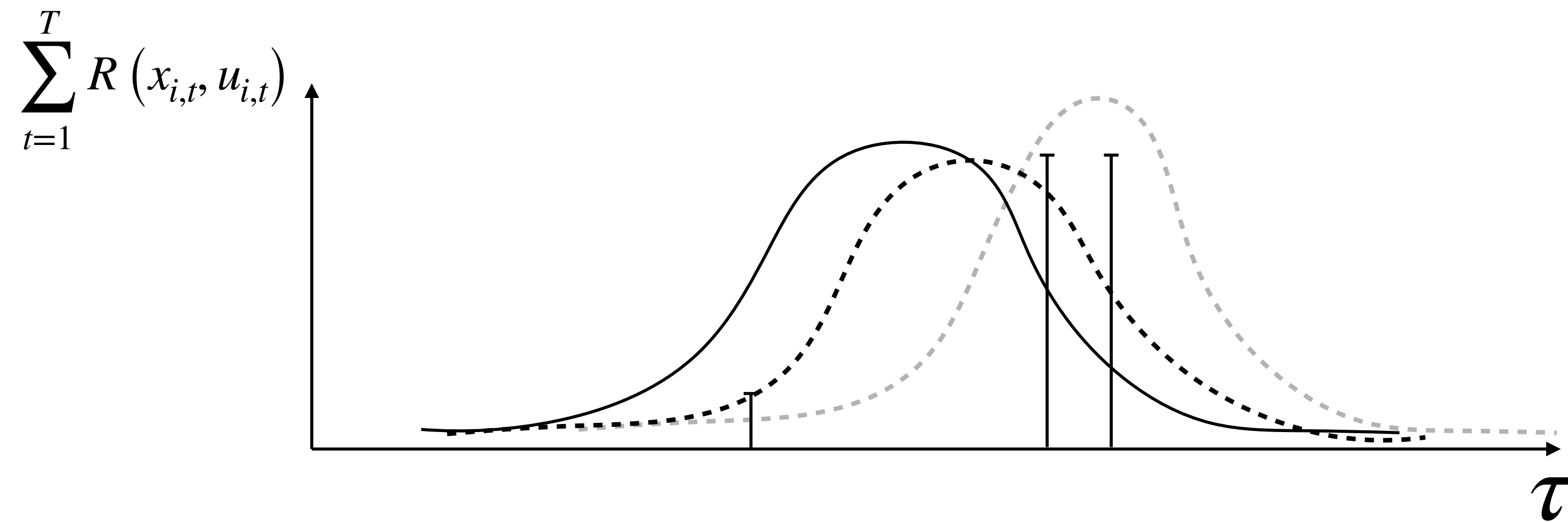
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Problem: high variance of the PG

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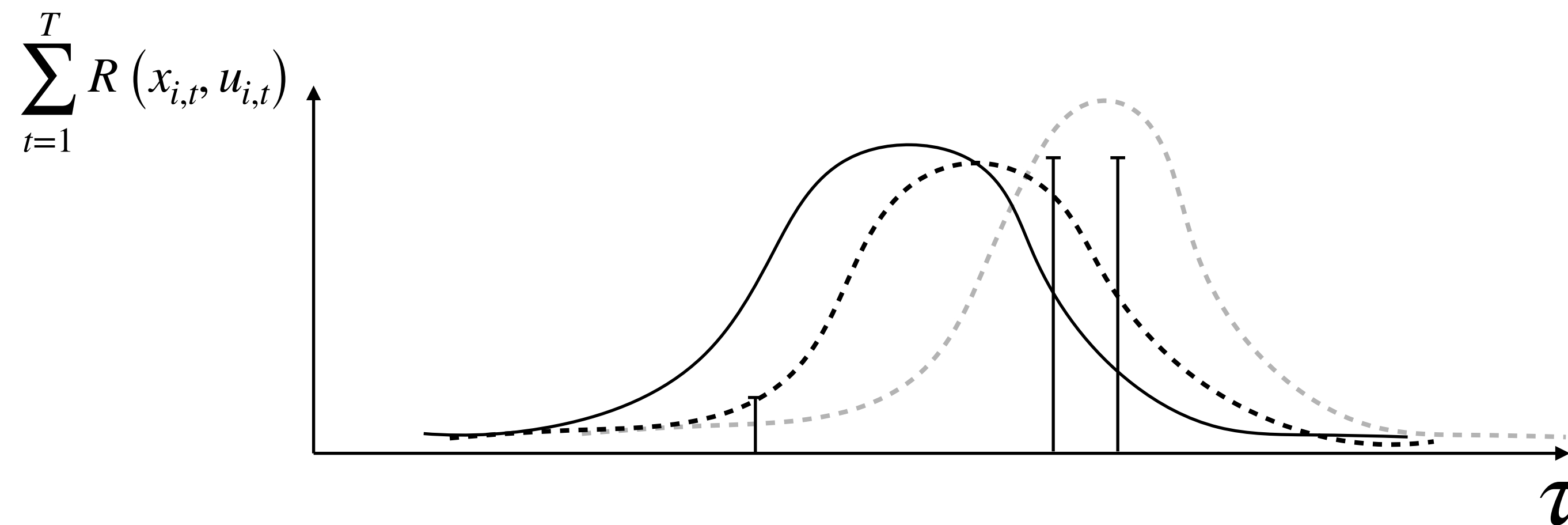
Let's consider the following example:



Problem: high variance of the PG

$$\text{Policy gradient: } \nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \left[\left(\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \right) \left(\sum_{t=1}^T R(x_{i,t}, u_{i,t}) \right) \right]$$

Let's consider the following example:



- Depending on the sample, the policy gradient can vary wildly: PG estimator has **high variance**
- This negatively affects learning: worse performance, slower convergence

A lot of research in the domain of Policy Optimization revolves around finding ways to lower the variance of the policy gradient

Reducing the variance

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \left[\left(\sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \right) \left(\sum_{t=1}^T R(x_{i,t}, u_{i,t}) \right) \right]$$

A first simple approach to reduce the variance entails using *causality*: “policy at time t' cannot affect reward at time $t < t'$ ”

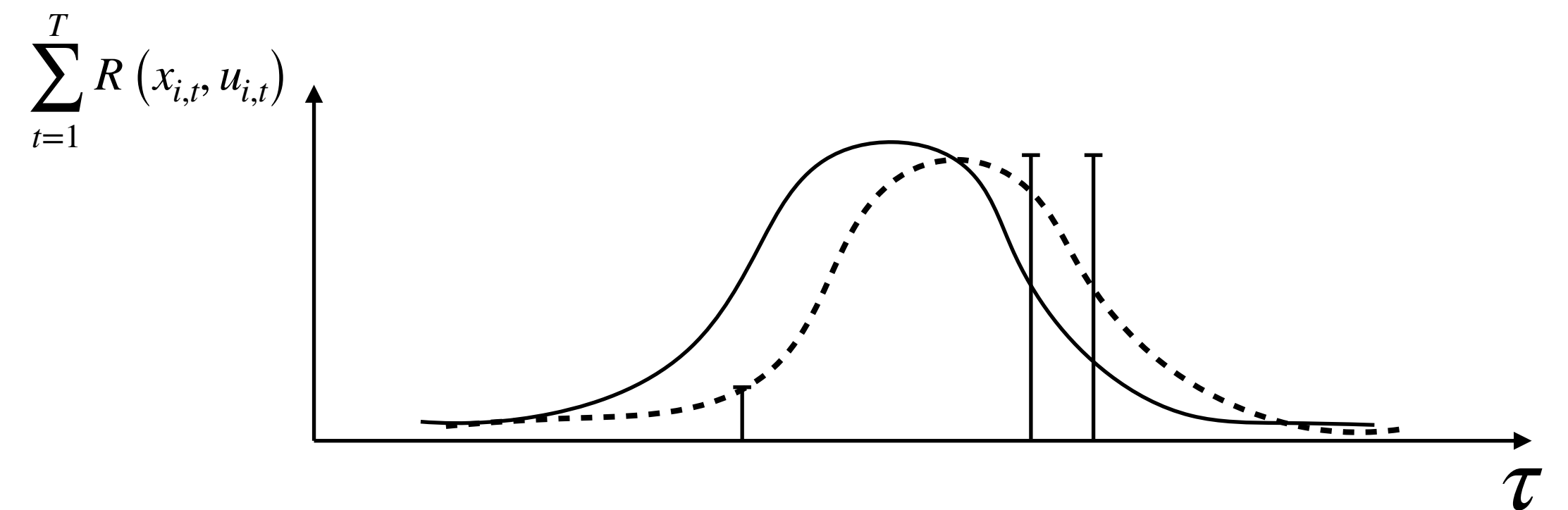
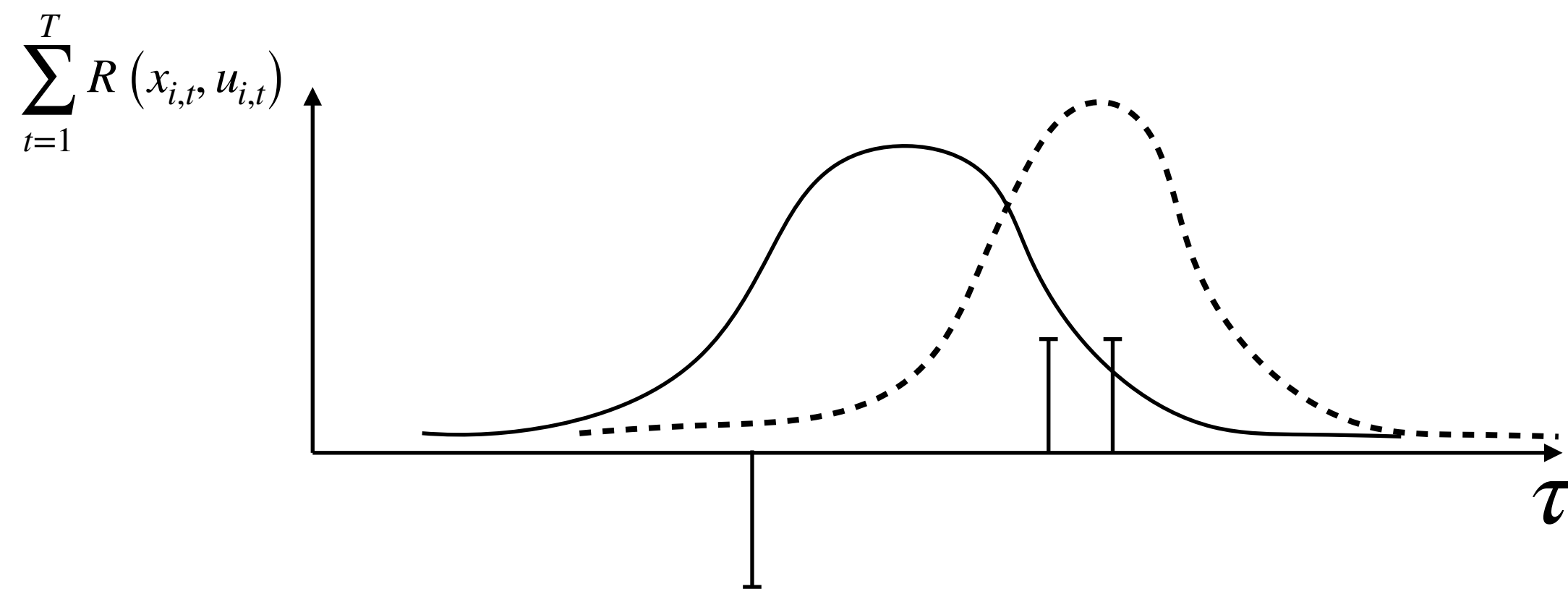
Consider this equivalent expression:

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \left(\sum_{t'=t}^T R(x_{i,t'}, u_{i,t'}) \right)$$

Baseline

A second (and extremely important) approach to reduce variance of PG estimators relates with the concept of **baseline**

Let's reconsider our intuition on PG, i.e., “making good behavior more likely”



However, PG will only do this **if the returns are centered** (e.g., consider the counter-example on the right)

Intuitively, we want to “center” our returns, such that:

- behavior better than average gets increased
- behavior worse than average gets decreased

We are going to subtract a baseline b from the expression of the PG

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \nabla_{\theta} \log \pi_{\theta}(\tau) [r(\tau) - b]$$

A closer look at the baseline

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \nabla_{\theta} \log \pi_{\theta}(\tau) [r(\tau) - b]$$

Claim: adding the baseline does not change the value of the expected gradient

- To prove that, let's consider the following expectation:

$$\mathbb{E} [\nabla_{\theta} \log p_{\theta}(\tau) b] = \int p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) b d\tau = \int \nabla_{\theta} p_{\theta}(\tau) b d\tau = b \nabla_{\theta} \int p_{\theta}(\tau) d\tau = b \nabla_{\theta} 1 = 0$$

which makes our estimate of the gradient (with baseline) *unbiased* in expectation

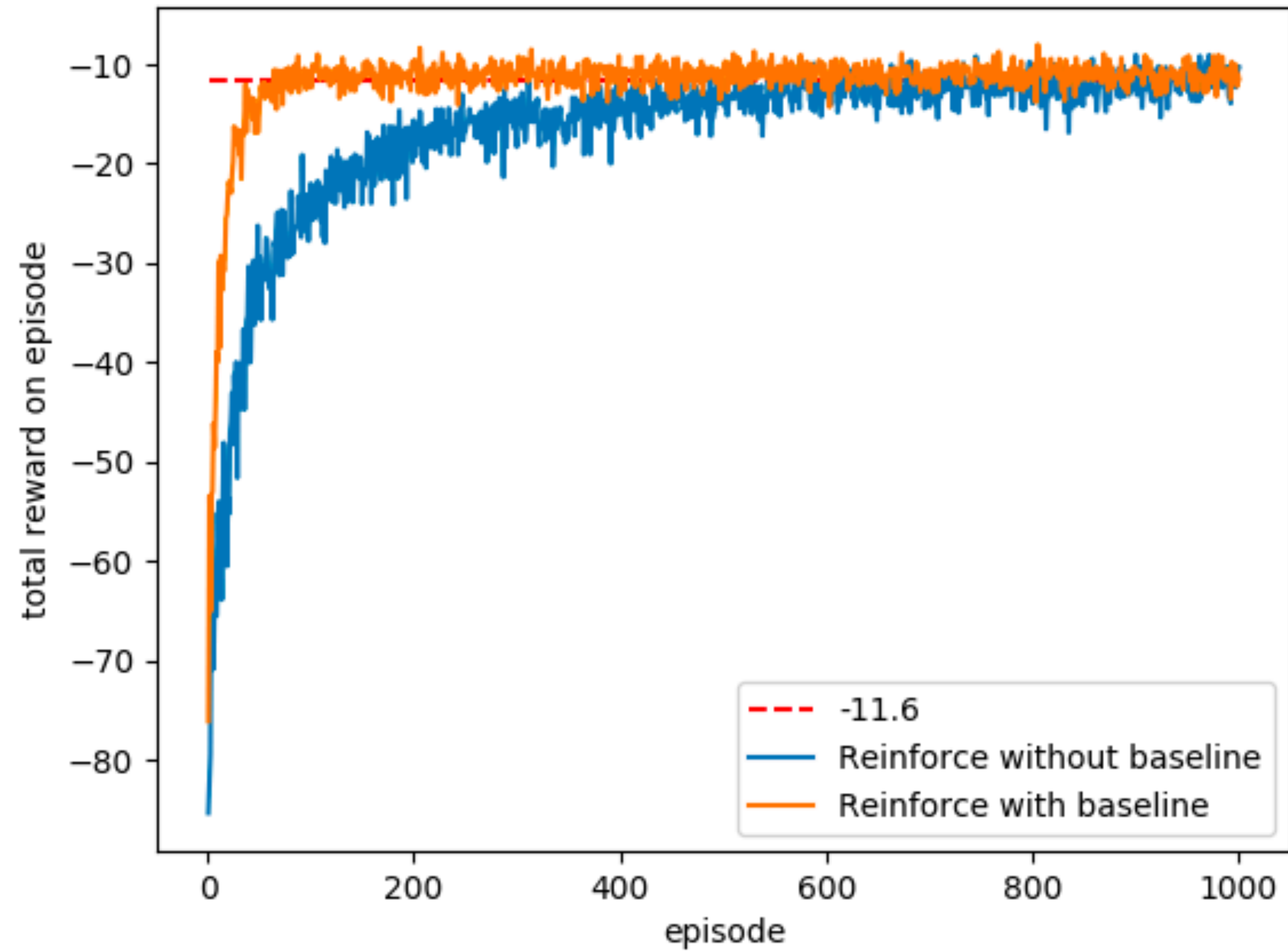
- An extremely effective choice of the baseline is the **average return**, $b = \frac{1}{N} \sum_{i=1}^N r(\tau)$

(We'll see how this motivates many popular RL algorithms...)

Useful identity:

$$p_{\theta}(\tau) \nabla_{\theta} \log p_{\theta}(\tau) = p_{\theta}(\tau) \frac{\nabla_{\theta} p_{\theta}(\tau)}{p_{\theta}(\tau)} = \nabla_{\theta} p_{\theta}(\tau)$$

Example



Properties of policy gradient

At a high-level, we've been defining a scheme where:

- Given the RL objective $J(\theta) = \mathbb{E}_{\tau \sim p(\tau)} [r(\tau)] = \int p_{\theta}(\tau) r(\tau) d\tau$
- We maximize the objective w.r.t. θ by:
 - Computing the gradient $\nabla_{\theta} J(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} [\nabla_{\theta} \log p_{\theta}(\tau) r(\tau)]$
 - Taking a gradient step to update the policy $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$

Pros:

- Naturally handles continuous/discrete action spaces
- Directly optimizes the RL objective — can be more stable than Q-learning, i.e., fixed-point iteration

Cons:

- On-policy. This can be extremely sample inefficient!

Question:

Is this on- or off-policy? And why?

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Deep RL Algorithms & Applications

From PG to Actor-Critic methods

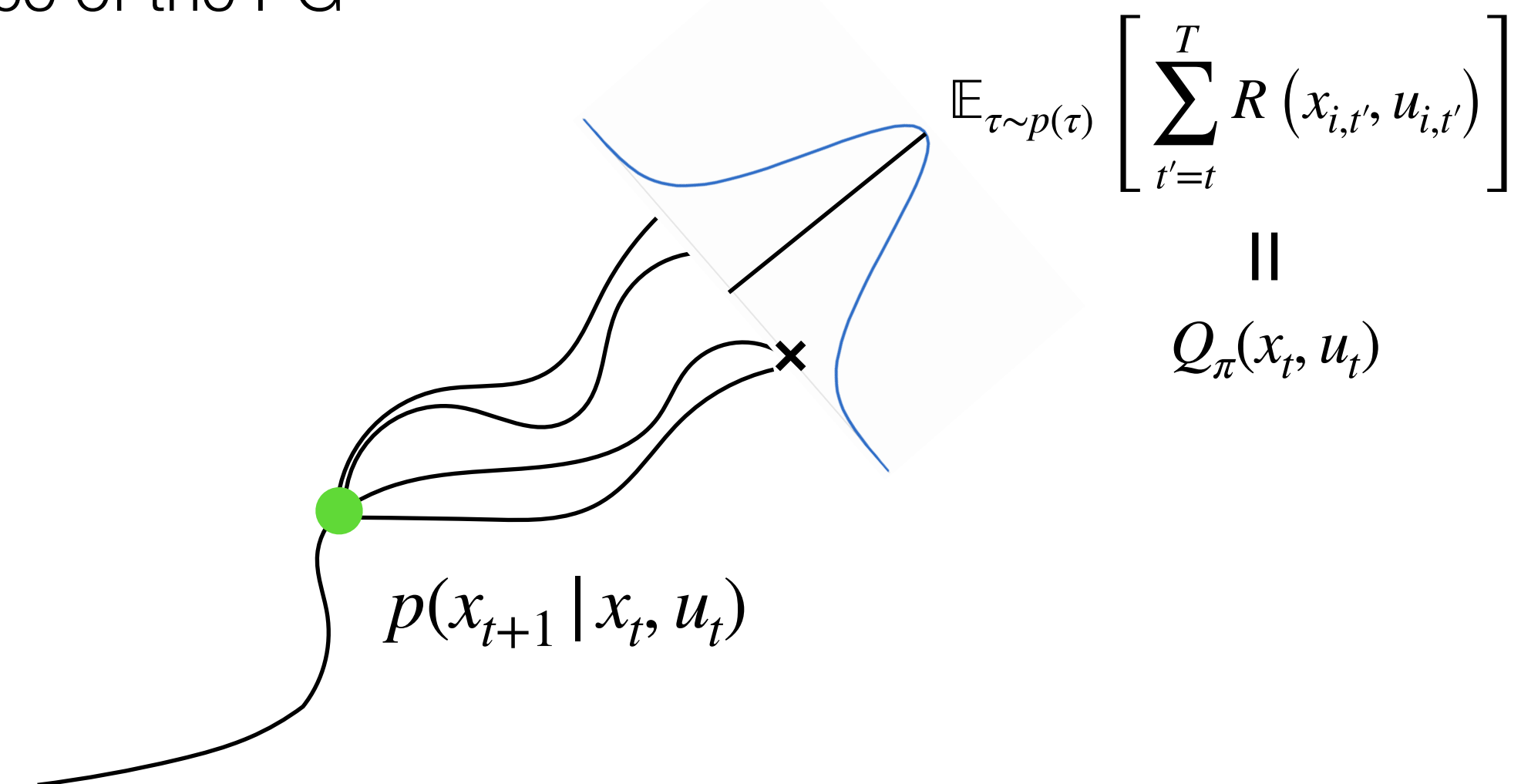
Once again, let's consider the policy gradient $\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \left(\sum_{t'=t}^T R(x_{i,t'}, u_{i,t'}) \right)$

“reward-to-go”

This one-sample estimate of the reward-to-go contributes to the high variance of the PG

The idea of actor-critic methods is to define:

- An “actor”, i.e., a policy $\pi_{\theta}(u_t | x_t)$
- A “critic” to better estimate the “reward-to-go”, e.g., estimate Q-values through function approximation $Q_{\phi}(x_t, u_t)$



By using this better estimate of the reward-to-go we can get a lower variance policy gradient:

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) Q_{\phi}(x_t, u_t)$$

What about the baseline?

Can we use a baseline when using the approximate reward-to-go and reduce the variance even further?

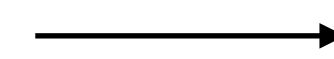
$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \left(Q_{\phi}(x_{i,t}, u_{i,t}) - b \right)$$

- An effective choice for b is a state-dependent baseline $b(x_t) = \mathbb{E}_{u_t \sim \pi(u_t | x_t)} [Q(x_t, u_t)] = V(x_t)$

- We can thus rewrite:

$$\nabla_{\theta} J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(u_{i,t} | x_{i,t}) \left(Q_{\phi}(x_{i,t}, u_{i,t}) - V(x_{i,t}) \right)$$

“How much u_t is better than the average action in x_t ”

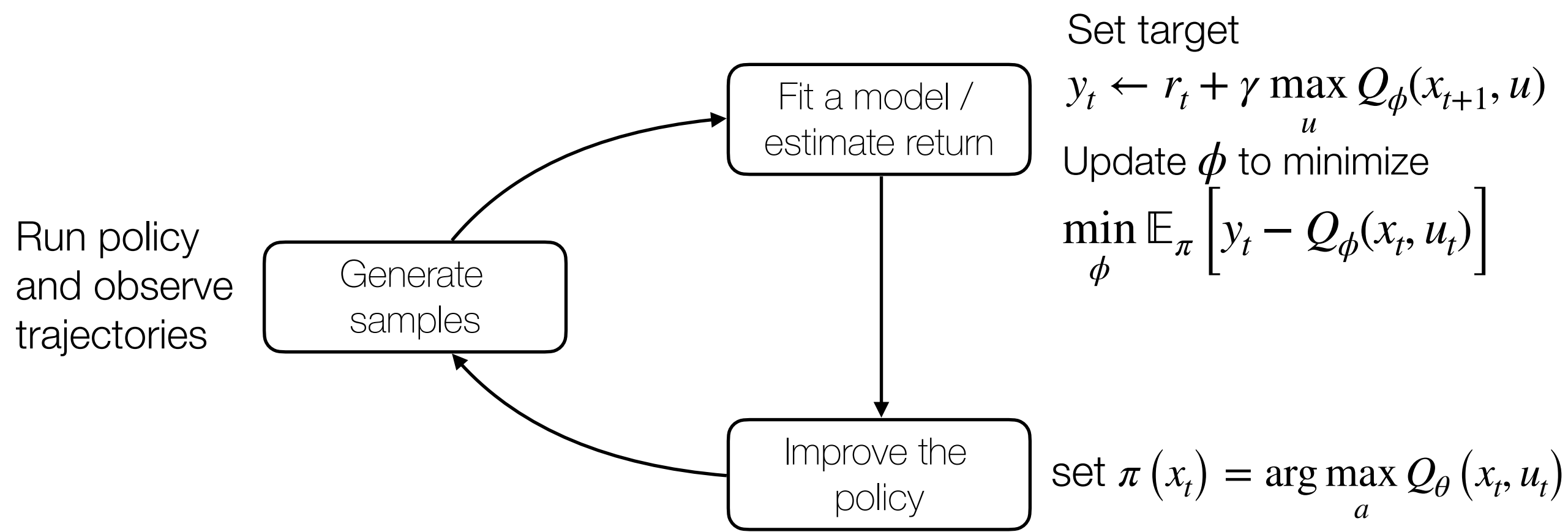


Following this gradient:

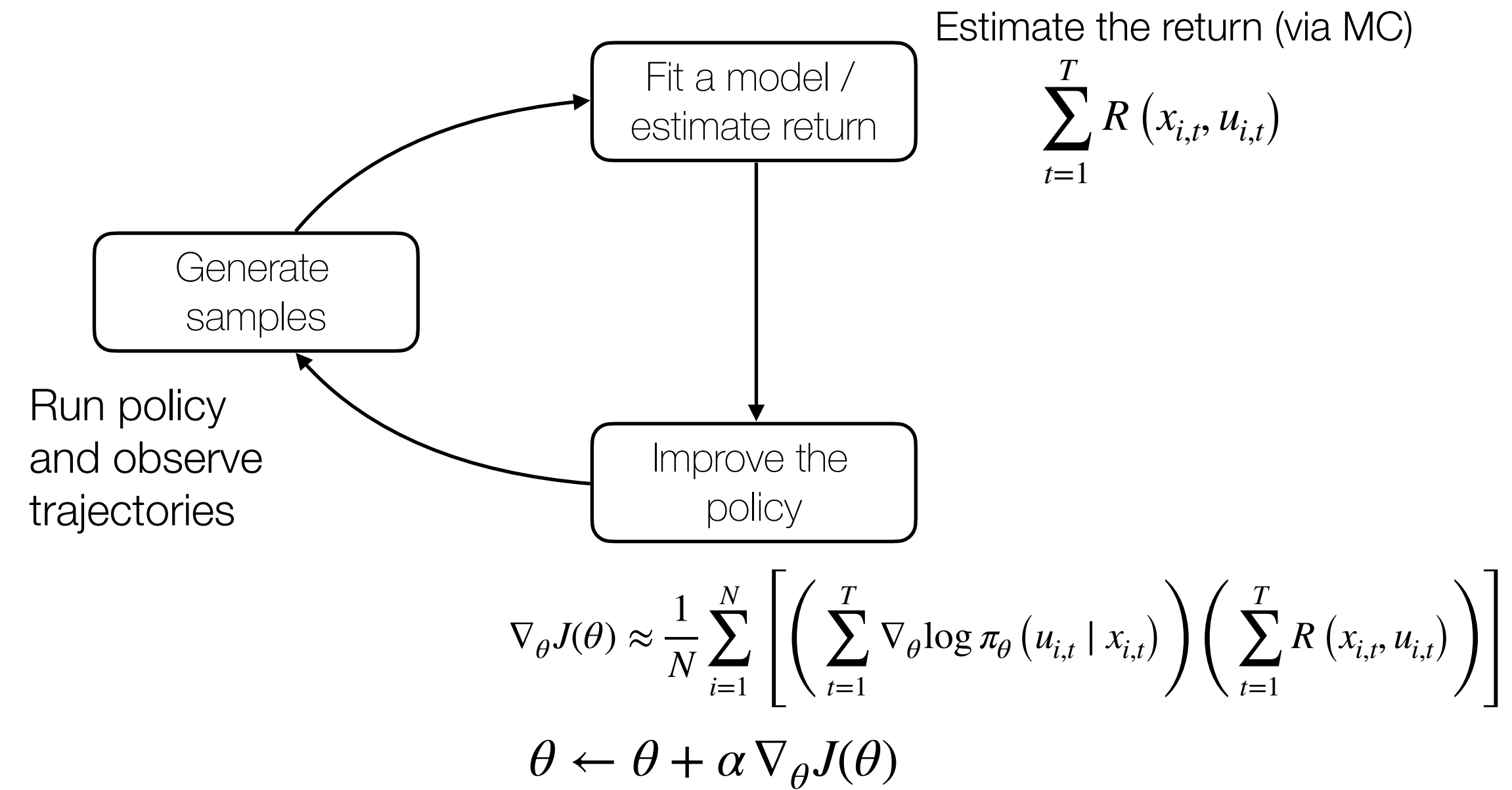
- increases the probability of actions that have returns better than average
- decreases the probability of actions that have returns worse than average

- The function $A(x_t, u_t) = Q_{\phi}(x_t, u_t) - V(x_t)$ is usually referred to as **advantage function**

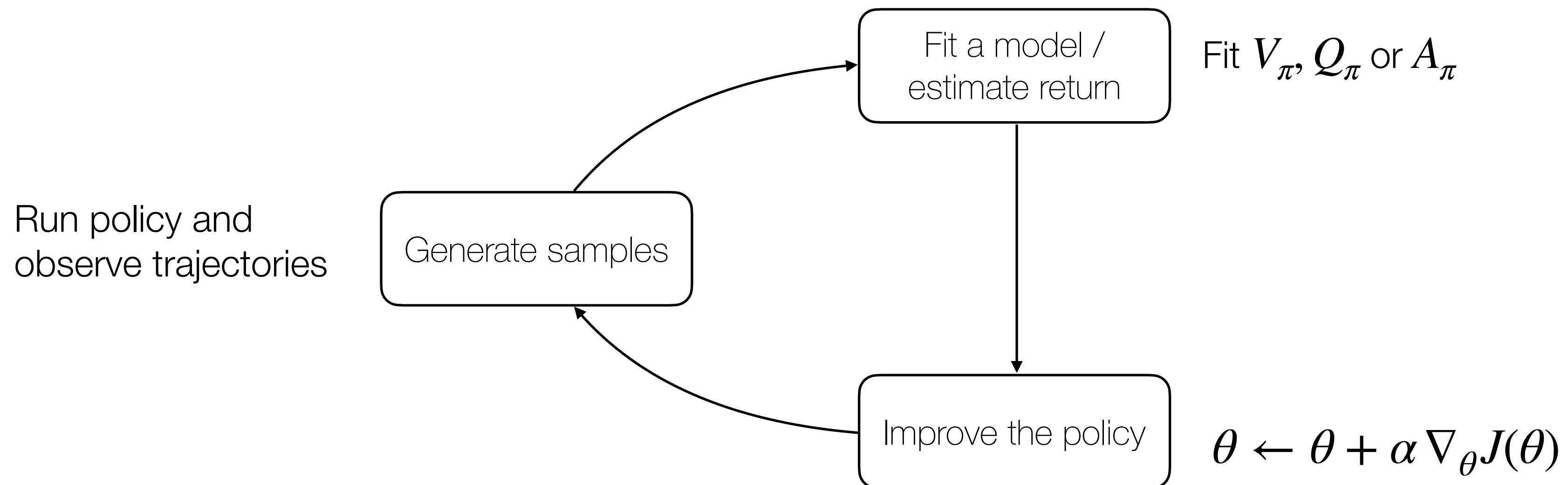
Fitted Q-learning:



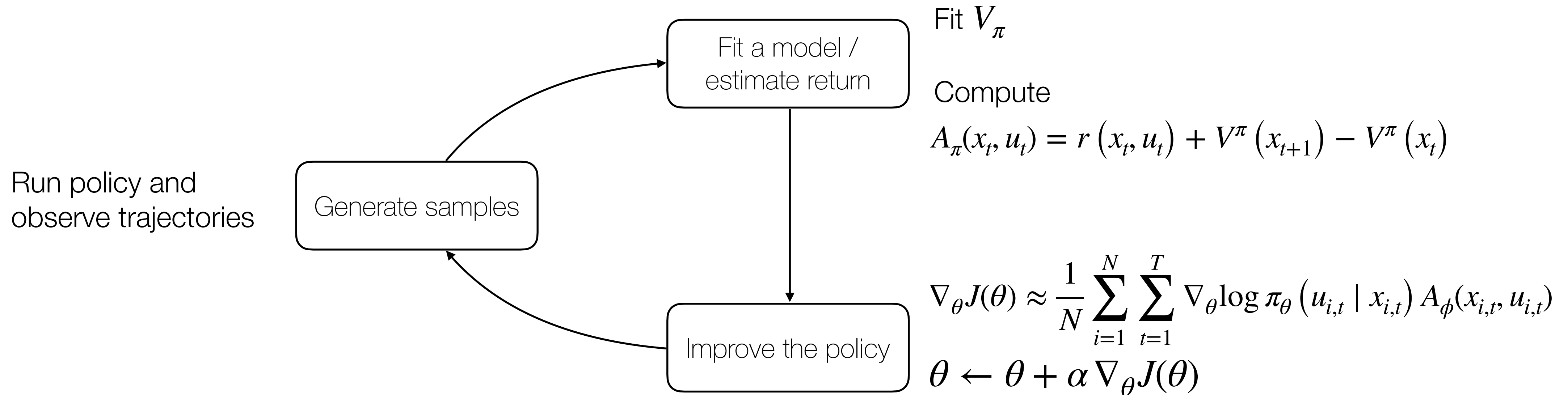
REINFORCE:



Actor-Critic:



Advantage Actor-Critic (A2C):



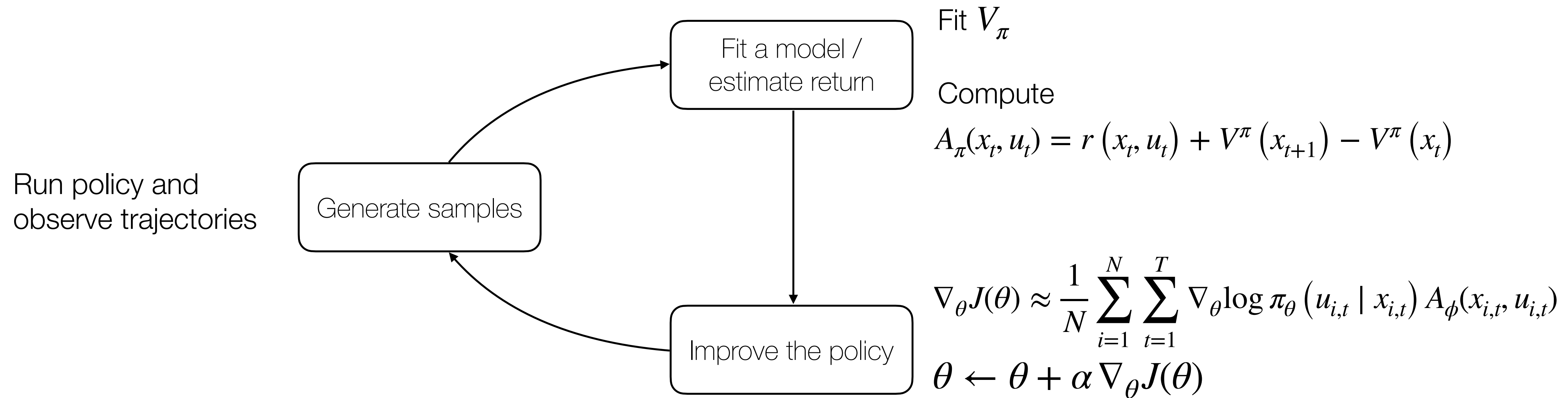
What quantity should we estimate? What are the trade-offs between estimating V_π , Q_π or A_π ? No wrong/right, answer, it depends. For now, let's consider the complexity of the estimation problem (i.e., fitting V_π is easier: only x_t as input)

$$Q_\pi(x_t, u_t) = \mathbb{E}_{\tau \sim p(\tau)} \left[\sum_{t'=t}^T R(x_{i,t'}, u_{i,t'}) \right] = r(x_t, u_t) + \mathbb{E}_{x_{t+1} \sim p(x_{t+1} | x_t, u_t)} \left[V^\pi(x_{t+1}) \right] \approx r(x_t, u_t) + V^\pi(x_{t+1})$$

$$A_\pi(x_t, u_t) = Q_\pi(x_t, u_t) - V_\pi(x_t) \approx r(x_t, u_t) + V^\pi(x_{t+1}) - V^\pi(x_t)$$

This enables us to “only” fit V_π

Advantage Actor-Critic (A2C):



When fitting V_π , we can use different *targets* to define the supervised learning labels

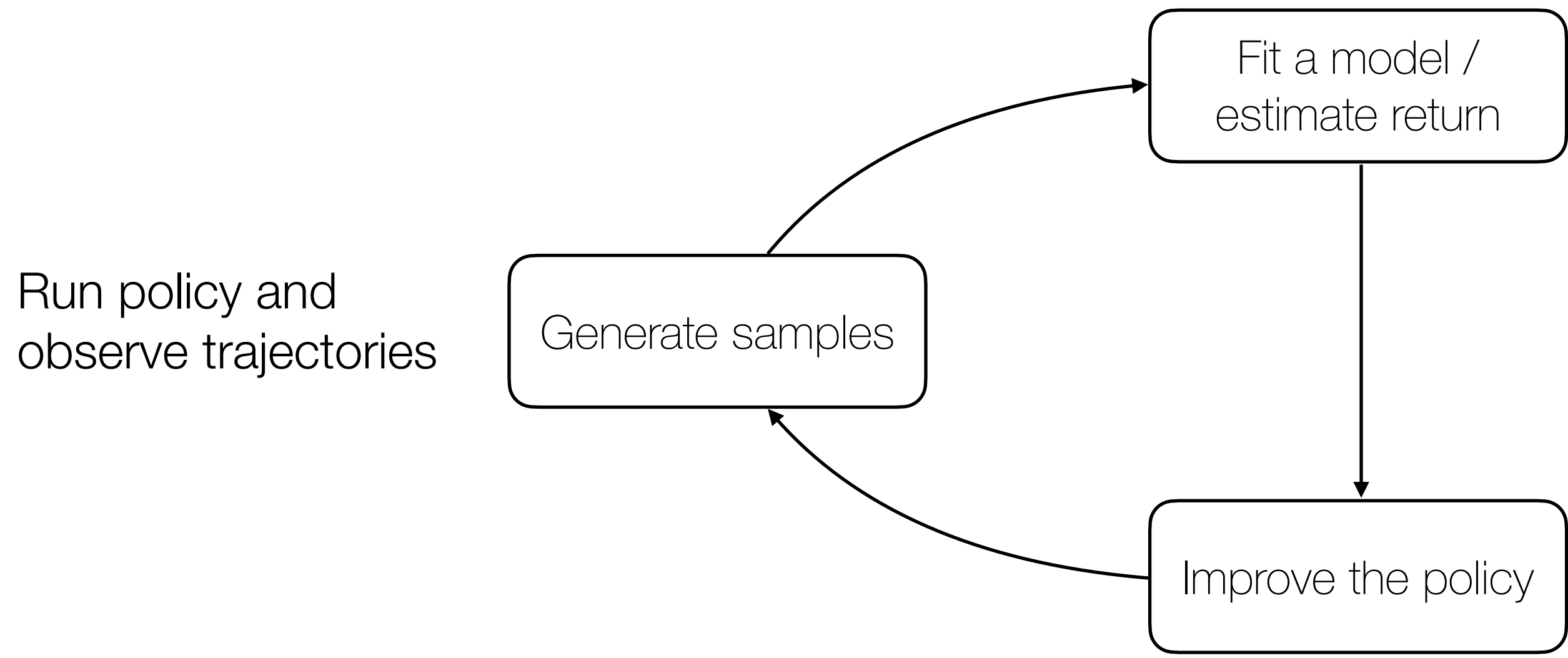
Question:

How to fit with MC target?

How to fit with TD target?

Example: AlphaGo paper

Architecture design



Fit V_π

Compute

$$A_\pi(x_t, u_t) = r(x_t, u_t) + V^\pi(x_{t+1}) - V^\pi(x_t)$$

$$\nabla_\theta J(\theta) \approx \frac{1}{N} \sum_{i=1}^N \sum_{t=1}^T \nabla_\theta \log \pi_\theta(u_{i,t} | x_{i,t}) A_\phi(x_{i,t}, u_{i,t})$$

$$\theta \leftarrow \theta + \alpha \nabla_\theta J(\theta)$$

In practice, one could opt for different designs of this same algorithms, e.g.,:

- Two network vs shared network
- Parallel processing: synchronized vs asynchronous

Simple, typically more stable

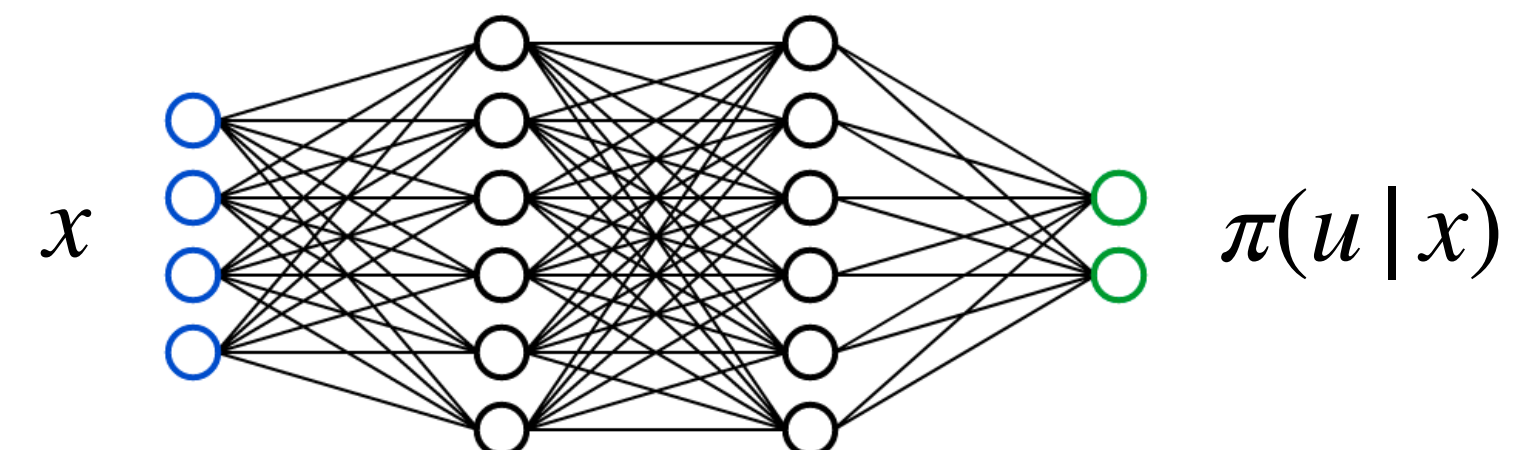
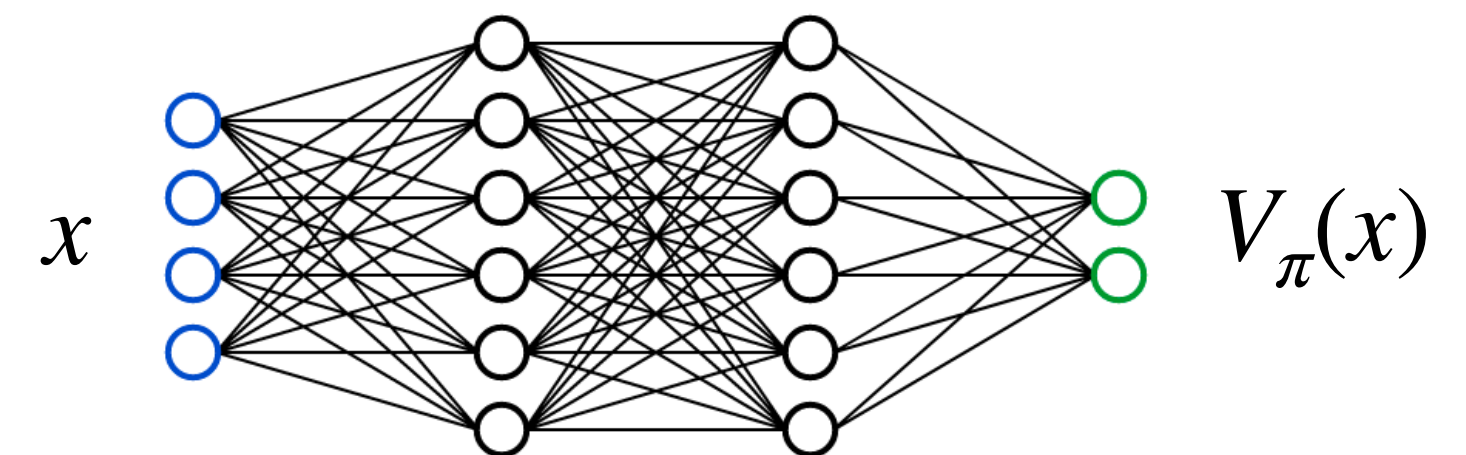
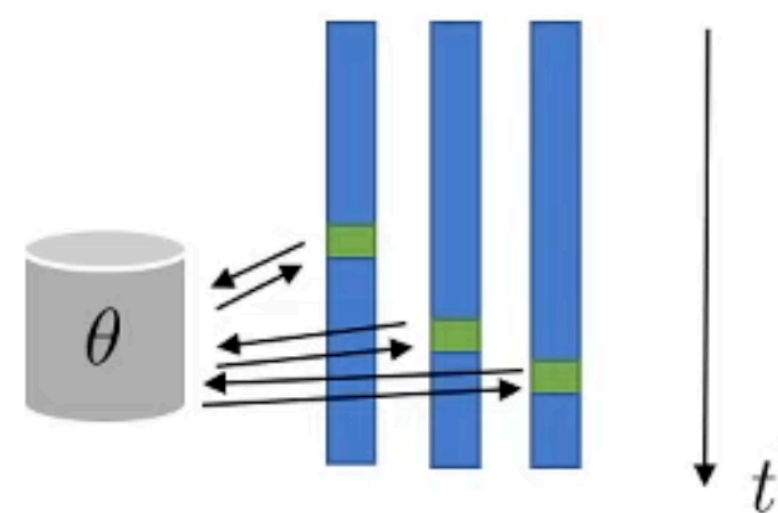
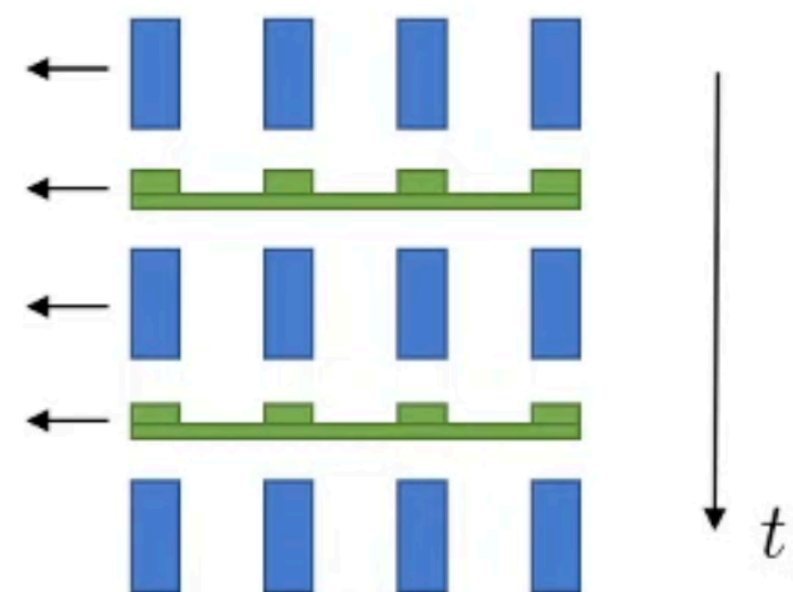
Does not share features

Get (x_t, u_t, x_{t+1}, r_t)

Update θ

Get (x_t, u_t, x_{t+1}, r_t)

Update θ



Outline

Intro to policy gradients

- REINFORCE algorithm
- Reducing variance of policy gradient

Actor-Critic methods

- Advantage
- Architecture design

Deep RL Algorithms & Applications

Practical implementation (and alternative formulation)

- We discussed how, in PO, we want to compute the following gradient $\nabla_{\theta} J(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} [\nabla_{\theta} \log p_{\theta}(\tau) A(\tau)]$
- To implement this using modern auto-diff tools (e.g., Torch, Jax, Tensorflow), this means writing the following loss function:

$$L^{PG}(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} [\log p_{\theta}(\tau) A(\tau)]$$

- But we don't want to optimize it too far, since we are not working with the *true* advantage, rather with a noisy estimate
- Let's define an alternative loss

$$L^{IS}(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} \left[\frac{\pi_{\theta}(u_t | x_t)}{\pi_{\theta_{old}}(u_t | x_t)} A(\tau) \right]$$

- If we take the derivative of L^{IS} and evaluate at $\theta = \theta_{old}$, we get the same gradient

$$\nabla_{\theta} \log f(\theta) \Big|_{\theta_{old}} = \frac{\nabla_{\theta} f(\theta) \Big|_{\theta_{old}}}{f(\theta_{old})} = \nabla_{\theta} \left(\frac{f(\theta)}{f(\theta_{old})} \right) \Big|_{\theta_{old}}$$

Trust Region Policy Optimization (TRPO)

$$\begin{aligned} & \underset{\theta}{\text{maximize}} \hat{\mathbb{E}}_t \left[\frac{\pi_{\theta}(u_t | x_t)}{\pi_{\theta_{old}}(u_t | x_t)} \hat{A}_t \right] \\ & \text{subject to } \hat{\mathbb{E}}_t \left[\text{KL}[\pi_{\theta_{old}}(\cdot | x_t), \pi_{\theta}(\cdot | x_t)] \right] \leq \delta \end{aligned}$$

- Main idea: use trust region to constrain change **in distribution space** (opposed to e.g., parameter space)
- Hard to use with architectures with multiple outputs, e.g., policy and value function
- Empirically performs poorly on tasks requiring CNNs and RNNs
- Conjugate gradient makes implementation more complicated

Proximal Policy Optimization (PPO)

- Can we solve the problem defined in TRPO without second-order optimization?

PPO v1 - Surrogate loss with Lagrange multipliers

$$\text{maximize}_{\theta} \hat{\mathbb{E}}_t \left[\frac{\pi_{\theta}(u_t | x_t)}{\pi_{\theta_{old}}(u_t | x_t)} \hat{A}_t \right] + \beta \left(\hat{\mathbb{E}}_t \left[\text{KL}[\pi_{\theta_{old}}(\cdot | x_t), \pi_{\theta}(\cdot | x_t)] \right] - \delta \right)$$

- Run SGD on the above objective
- Do dual descent update for β

PPO v2 - Clipped surrogate loss

$$r(\theta) = \frac{\pi_{\theta}(u_t | x_t)}{\pi_{\theta_{old}}(u_t | x_t)}, \quad r(\theta_{old}) = 1$$

$$\text{maximize}_{\theta} \hat{\mathbb{E}}_t \left[\min(r(\theta)A(\tau), \text{clip}(r(\theta), 1 - \epsilon, 1 + \epsilon)A(\tau)) \right]$$

- Heuristically replicates constraint in the objective
- One of the (if not the) most popular PO algorithm

Examples: Maze Navigation

- Mnih et al. 2016 "Asynchronous Methods for Deep Reinforcement Learning"
- Advantage Actor-Critic
- Asynchronous parallel workers
- Policy and Value networks: CNNs & RNNs

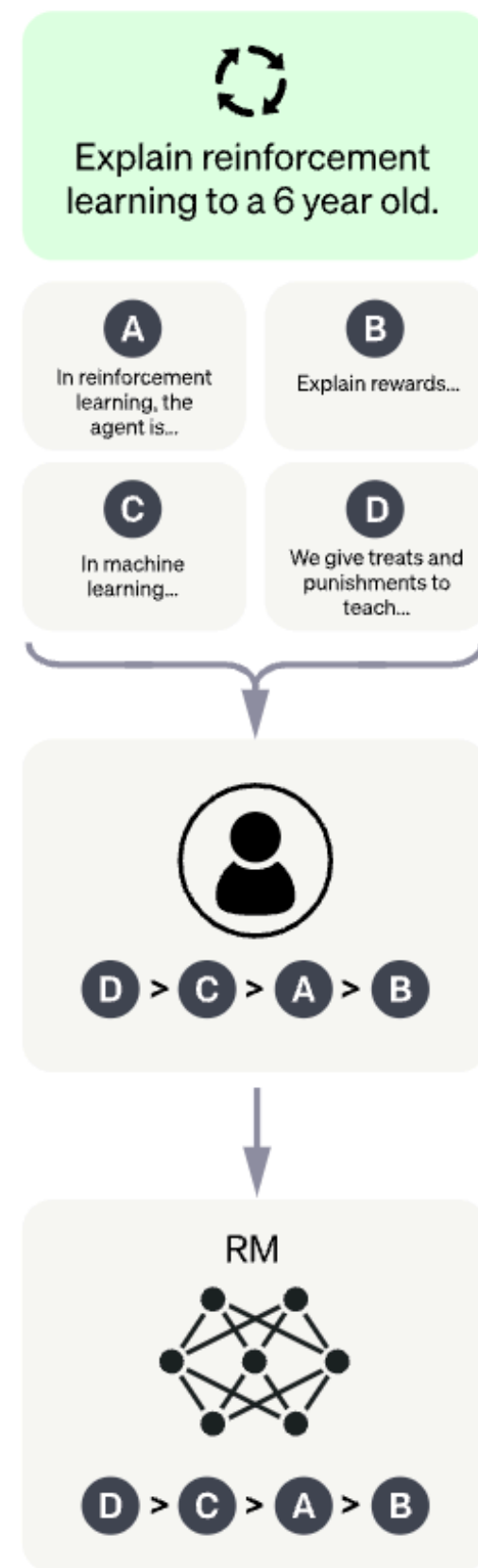


Examples: Alignment of ChatGPT

Step 2

Collect comparison data and train a reward model.

A prompt and several model outputs are sampled.



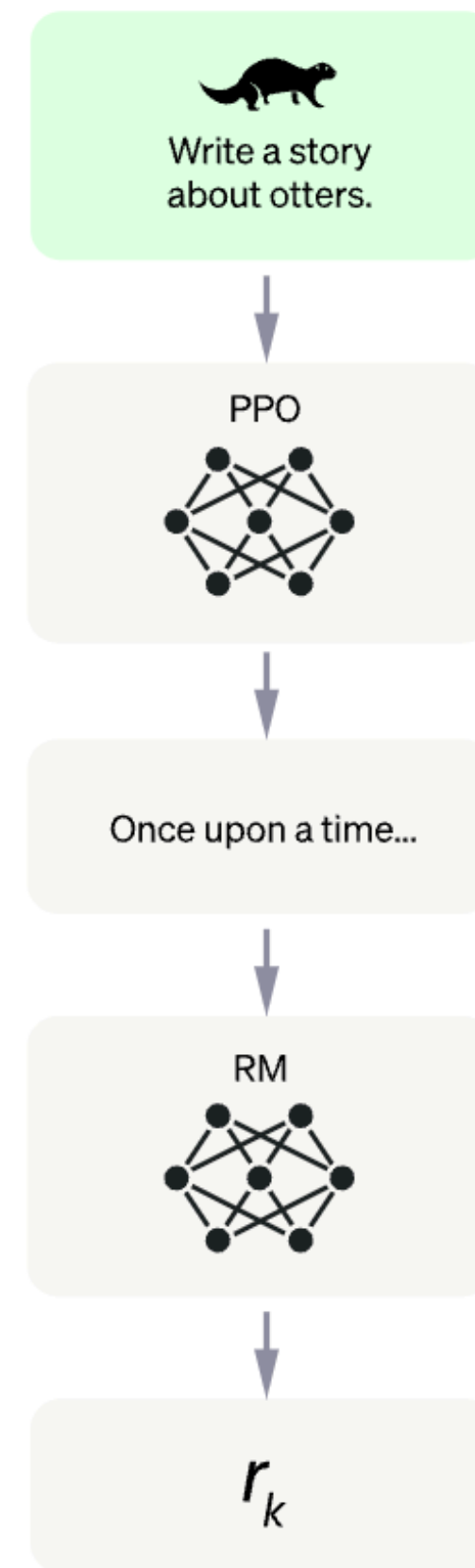
A labeler ranks the outputs from best to worst.

This data is used to train our reward model.

Step 3

Optimize a policy against the reward model using the PPO reinforcement learning algorithm.

A new prompt is sampled from the dataset.



The PPO model is initialized from the supervised policy.

The policy generates an output.

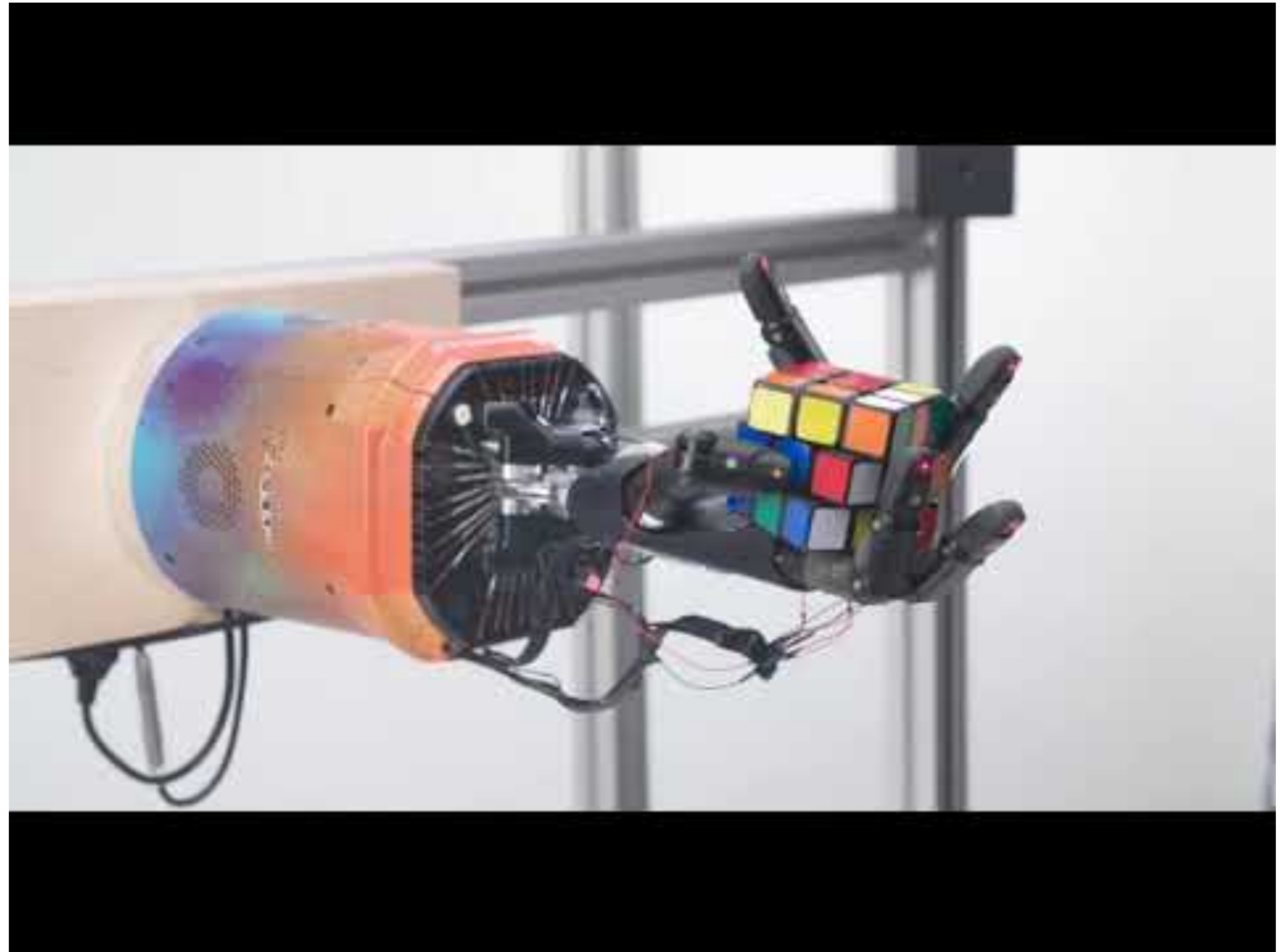
The reward model calculates a reward for the output.

The reward is used to update the policy using PPO.



Examples: Robot manipulation

- PPO
- Trained entirely in Sim



Next time

- Model-based RL