

# Principles of Robot Autonomy I

Finite state machines



# Logistics

- It's the final (project) stretch!

- All sections are open office hours for project discussion with TAs

Monday: 5:30 – 7:30pm (virtual) rabrown1

Tuesday: 4:30 – 6:30pm (in-person) lewt

Wednesday: 10am – 12pm (in-person) somrita

Wednesday: 12pm – 2pm (in-person) schneids

Wednesday: 5 – 7pm (in-person) rabrown1

Thursday: 11:45am – 1:45pm (in-person) somrita

Thursday: 4:30 – 6:30pm (virtual) lewt

Friday: 9:45am – 11:45am (in-person) rdyro

Friday: 12 – 2pm (in-person) schneids

- Final project demos: Wednesday, December 8<sup>th</sup>, 8:30 – 11:30am
- Simulation server should be more stable now, but perhaps see [“Running ROS locally” \(EdStem post\)](#)



# Today's lecture

- Aim

- Introduce and formalize the concept of Finite State Machines (FSMs)
- Discuss their relevance, strengths and limitations
- Introduce tools to allow you to use them effectively

- Readings

- Chapter 4 of Leslie Kaelbling, Jacob White, Harold Abelson, Dennis Freeman, Tomás Lozano-Pérez, and Isaac Chuang. *6.01SC Introduction to Electrical Engineering and Computer Science I*. Spring 2011. Massachusetts Institute of Technology: MIT OpenCourseWare.



# Finite State Machines

Definition: *A computational model for systems whose output depends on the **entire history** of their inputs.*

\*A finite state machine is a modeling framework, NOT an algorithm (similar to Markov decision processes, probability densities, factor graphs etc.)\*

# Finite State Machines in practice

- In practice, used in many different ways
  - Synthetically (specifies a program)
    - E.g. a product manager and an engineer specifies how an ATM machine should “behave” before starting its implementation
  - Analytically (describe the behavior of a combination of systems)
    - E.g. two self-driving cars could be modeled as FSMs. An engineer could try to see if they might end up stuck in some infinite loop at an intersection
  - Predictively (to predict interaction with an environment)
    - A self-driving car could have an internal model of a pedestrian as an FSM and use it to figure out how it should behave around it

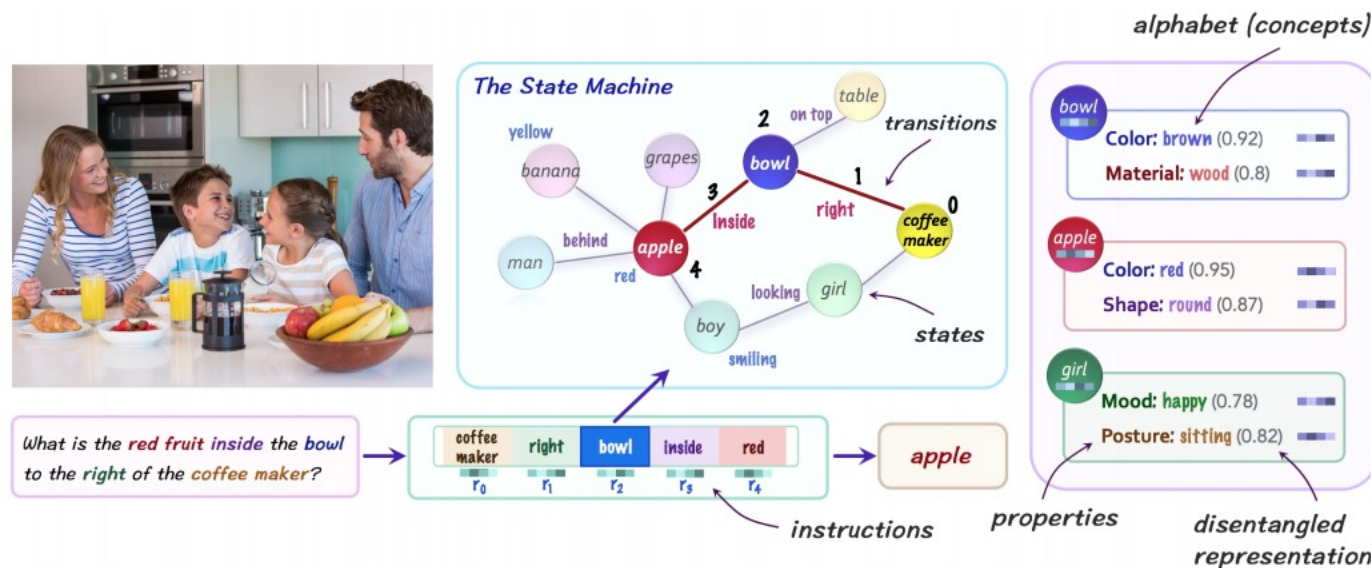
# Why are we teaching FSMs?

- For the practitioner: designing the extremely complex state machines required to fly drones, drive self-driving cars or operate warehouse robots is still one of the most time-consuming/difficult tasks faced by companies...
- How do we handle the failure of a combination of sensors gracefully?
- How do we negotiate an intersection?
- How do I get my turtlebot to start backtracking after a collision?



# Why are we teaching FSMs?

- For the researcher: It's a fundamental building block of how we understand computation, and still relevant to research today...



Hudson, Drew A., and Christopher D. Manning. "Learning by abstraction: The neural state machine." *arXiv preprint arXiv:1907.03950* (2019).

# Mathematical definition

- Sets:
  - A set of states  $S$
  - A set of inputs  $I$ , called the input vocabulary
  - A set of outputs  $O$ , called the output vocabulary
- Maps:
  - Next-state function that maps input and the state to the next state  
 $n(i_t, s_t) \rightarrow s_{t+1}$
  - Output function  $o(i_t, s_t) \rightarrow o_t$
- An initial state  $s_0$

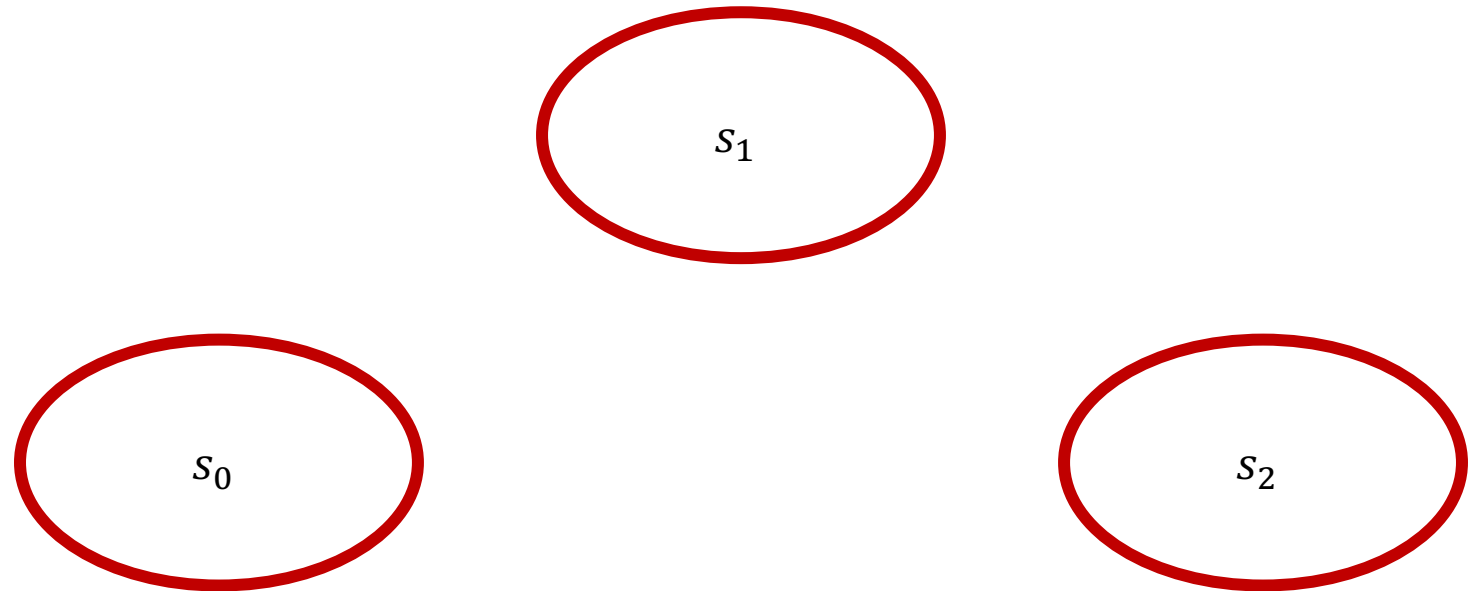
# Graphical representation

- Given the sets  $(S, I, O)$ , it is common to express the maps  $(n, o)$  by using a graph

$S: \{s_0, s_1, s_2\}$

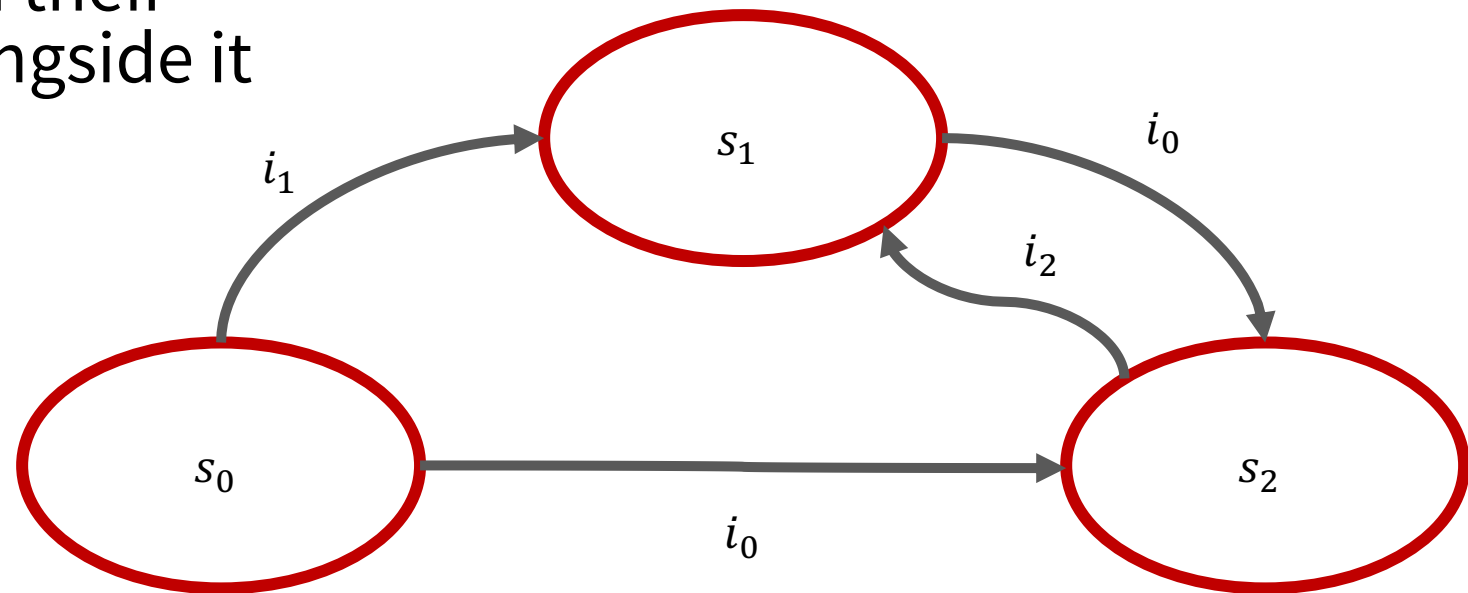
$I: \{i_0, i_1, i_2\}$

$O: \{o_0, o_1\}$



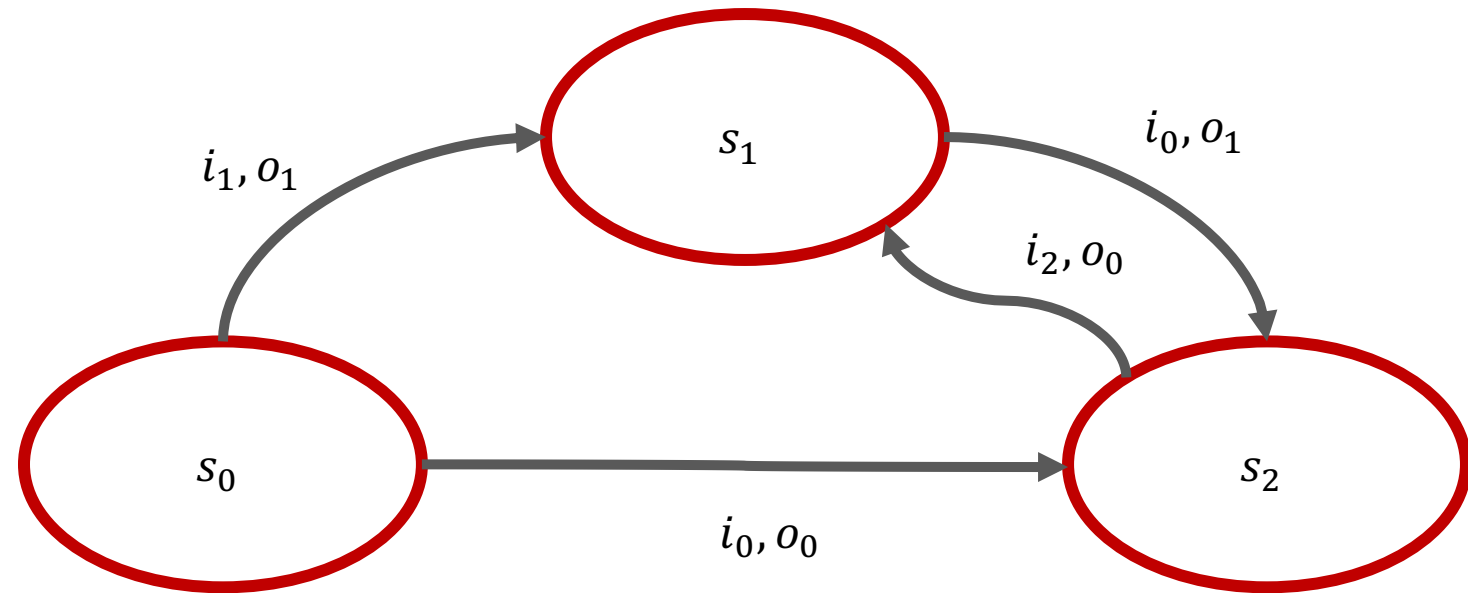
# Graphical representation

The transition (next-state) map is represented by arrows between states, with their associated input alongside it



# Graphical representation

The output map is written alongside each transition



# Example: parking gate control

The gate can be in one of three positions: 'top', 'middle' or 'bottom'

A sensor tells the gate if a car is waiting in front of it

A sensor tells the gate if a car has just passed through it

The gate can take the following actions: raise the gate, lower the gate, no operation (nop).

We want the following behavior:

- If a car wants to come through, need to raise the arm to 'top' position
- The gate has to stay there until the car has driven through the gate
- The gate has to go back down after the car has gone through



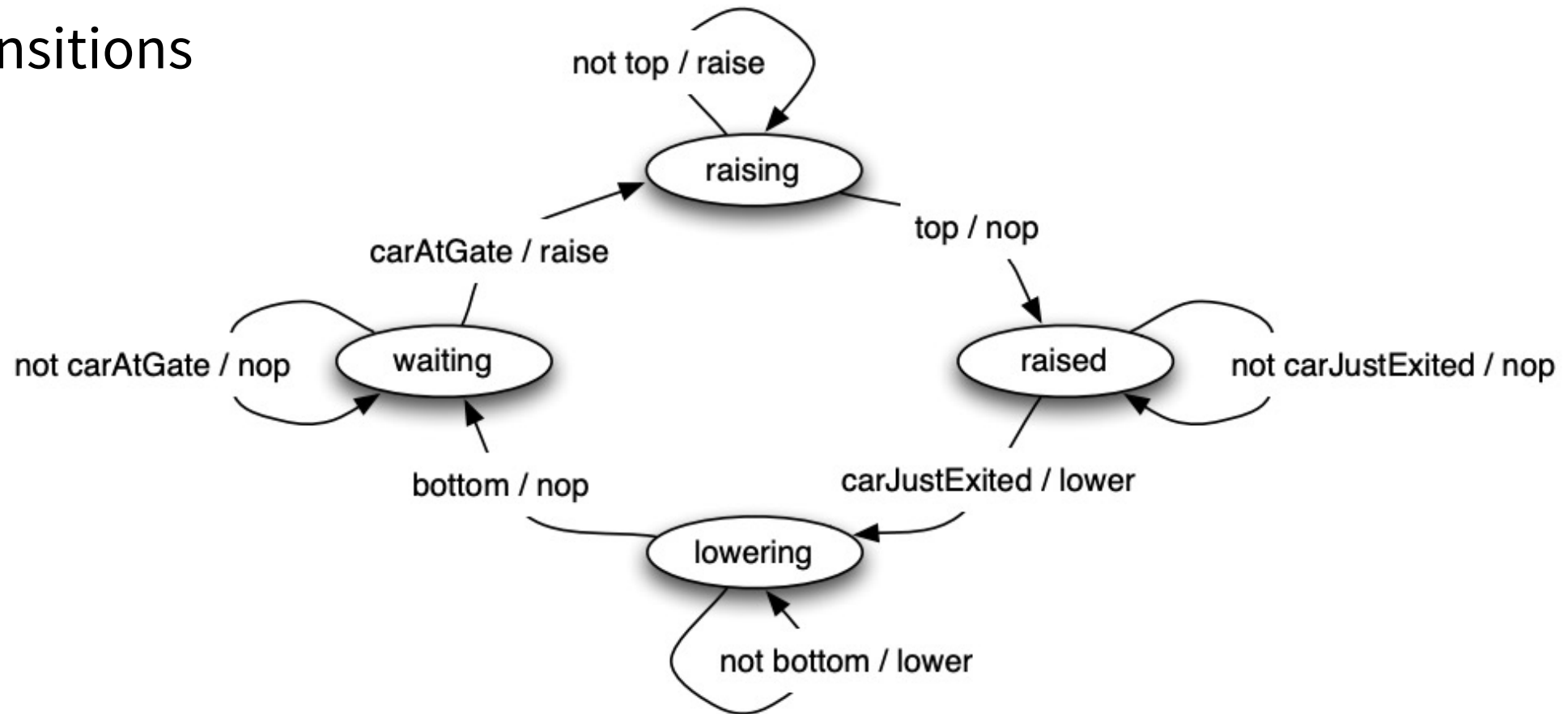
# Example: parking gate control

- States: 'waiting', 'raising', 'raised', 'lowering'
- Input: 'no car at gate', 'car at gate', 'gate at top', 'not gate at top', 'gate at bottom', 'not gate at bottom', 'car just exited', 'not car just existed'
- Output: 'raise', 'lower', 'nop'



# Example: parking gate control

- Transitions



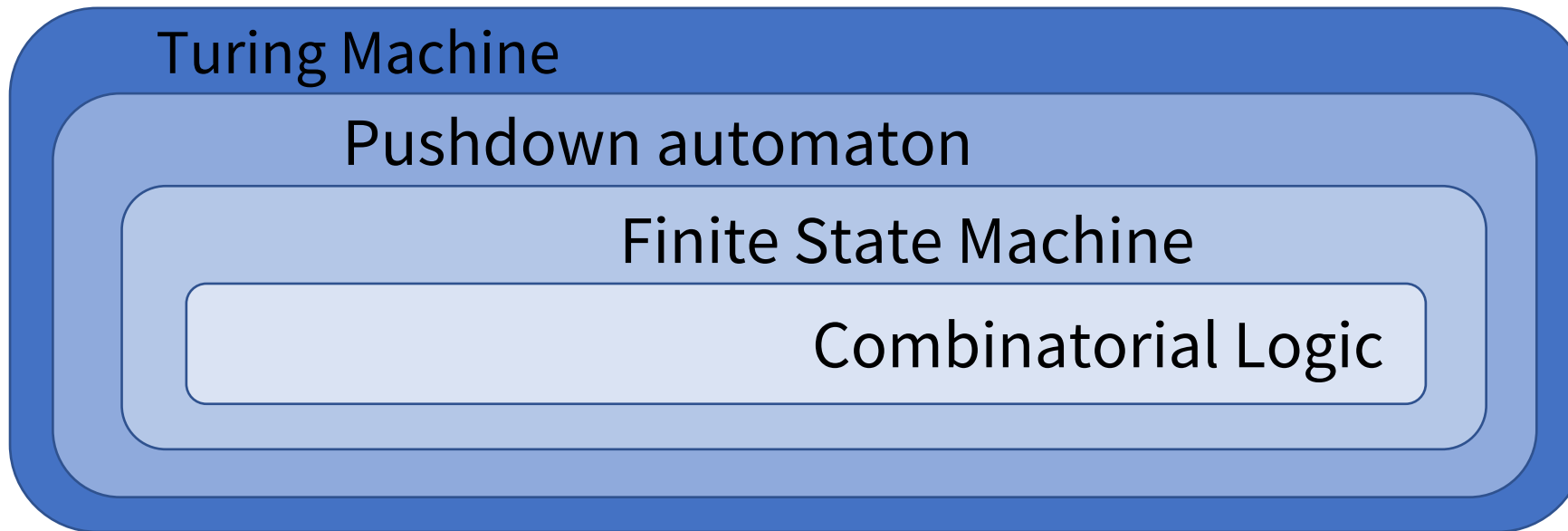


# Example: parentheses balancing

- We want to design an automata that can read a string of text of any length and say whether or not the parentheses in the string are balanced or not
  - Balanced: "1 + ( 2 + 3 - ( 4 \* 5 ) )"
  - Not balanced: "1 + ( 2 + 3 - 4 \* 5 ) )"
- "... a string of text of **any length**..."
- A robot that can accomplish such a task would need an infinite number of states... and cannot therefore be represented by a **finite** state machine

# FSM in the bigger picture of computation

- In terms of computational power, (deterministic) finite state machines are actually somewhat low on the totem pole of automata... with Turing Machines somewhere close to the top.



A Turing Machine could solve our parentheses balancing problem!

# Architecture

- The architecture of finite state machines can become quite complex
- Additional states can generate an exponential number of transitions
- Strategies to keep the architecture tractable:
  1. Reduction of redundant states
  2. Hierarchical finite state machines
  3. Composition using common patterns

# Finite State Machine optimization

- Algorithms exist to identify and combine states that have equivalent behavior
- Equivalent states:
  - Same output
  - For all input combinations, state transition to same or equivalent states
- Sketch of polynomial time algorithm:
  - Place all states in one set
  - Initially partition set based on output behavior
  - Successively partition resulting subsets based on next state transitions
  - Repeat until no further partitioning

# Finite State Machine optimization

Input Sequence	Present State	Next State		Output	
		X=0	X=1	X=0	X=1
Reset	S0	S1	S2	0	0
0	S1	S3	S4	0	0
1	S2	S5	S6	0	0
00	S3	S0	S0	0	0
01	S4	S0	S0	1	0
10	S5	S0	S0	0	0
11	S6	S0	S0	1	0



Input Sequence	Present State	Next State		Output	
		X=0	X=1	X=0	X=1
<b>Reset</b>	<b>S0</b>	<b>S1'</b>	<b>S1'</b>	<b>0</b>	<b>0</b>
<b>0 + 1</b>	<b>S1'</b>	<b>S3'</b>	<b>S4'</b>	<b>0</b>	<b>0</b>
<b>X0</b>	<b>S3'</b>	<b>S0</b>	<b>S0</b>	<b>0</b>	<b>0</b>
<b>X1</b>	<b>S4'</b>	<b>S0</b>	<b>S0</b>	<b>1</b>	<b>0</b>

Sequence detector for 010 or 110

( S0 S1 S2 S3 S4 S5 S6 )

( S0 S1 S2 S3 S5 ) ( S4 S6 )

( S0 S3 S5 ) ( S1 S2 ) ( S4 S6 )

( S0 ) ( S3 S5 ) ( S1 S2 ) ( S4 S6 )

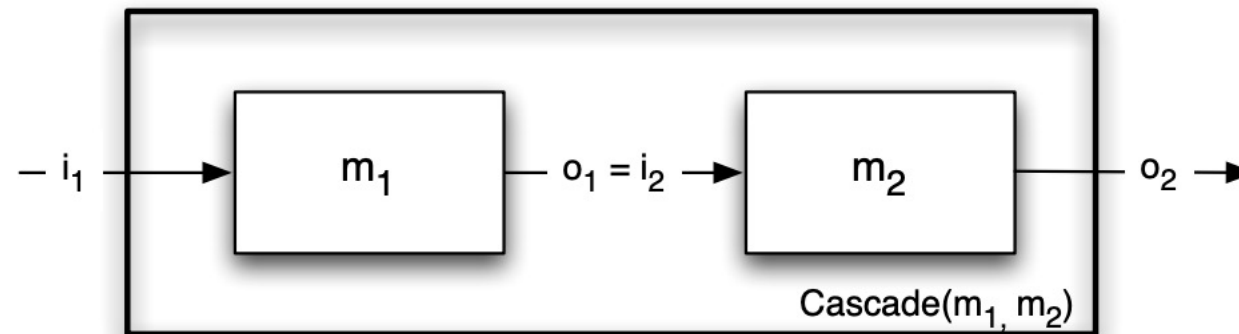
# Hierarchical Finite State Machines

- Some states might not be equivalent, but it might still be beneficial to group closely related ones together
- This leads to the following two concepts:
  - Super-states (groups of states)
  - Generalized transitions (transitions between super-states)

# Composition

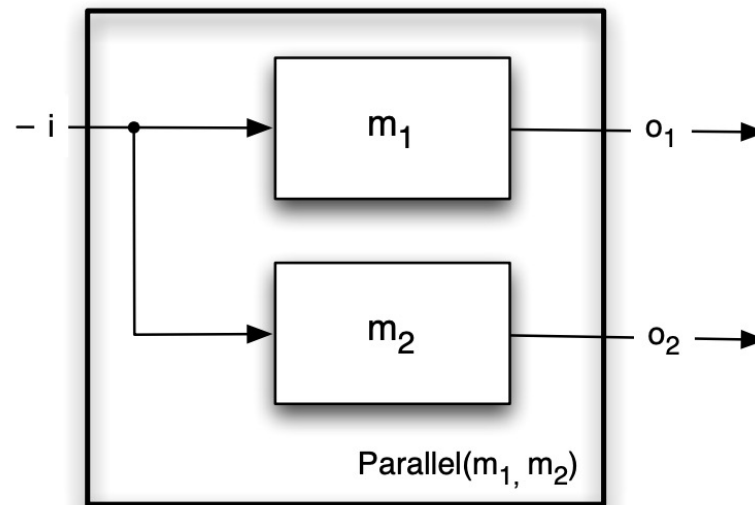
- Cascade

- Requirement: output vocabulary of  $m_1$  must match input vocabulary of  $m_2$
- Resulting state: concatenation of states
- Resulting input: input of  $m_1$
- Resulting output: output of  $m_2$



# Composition

- Parallel
  - Requirement: Input vocabularies must be the same
  - Resulting state: concatenation of states
  - Resulting input: same as input vocabulary of component machines
  - Resulting output: concatenation of outputs

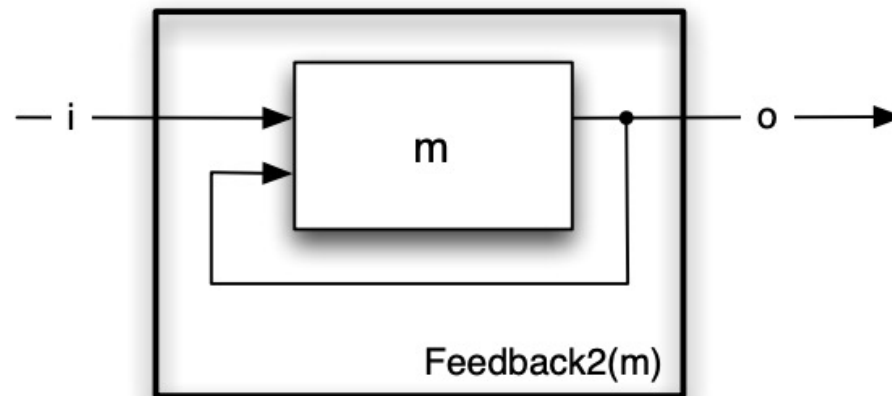




# Composition

- Feedback

- Requirement: Input and output vocabularies must be the same
- Resulting state: same
- Resulting input: partial input
- Resulting output: same



# Implementation

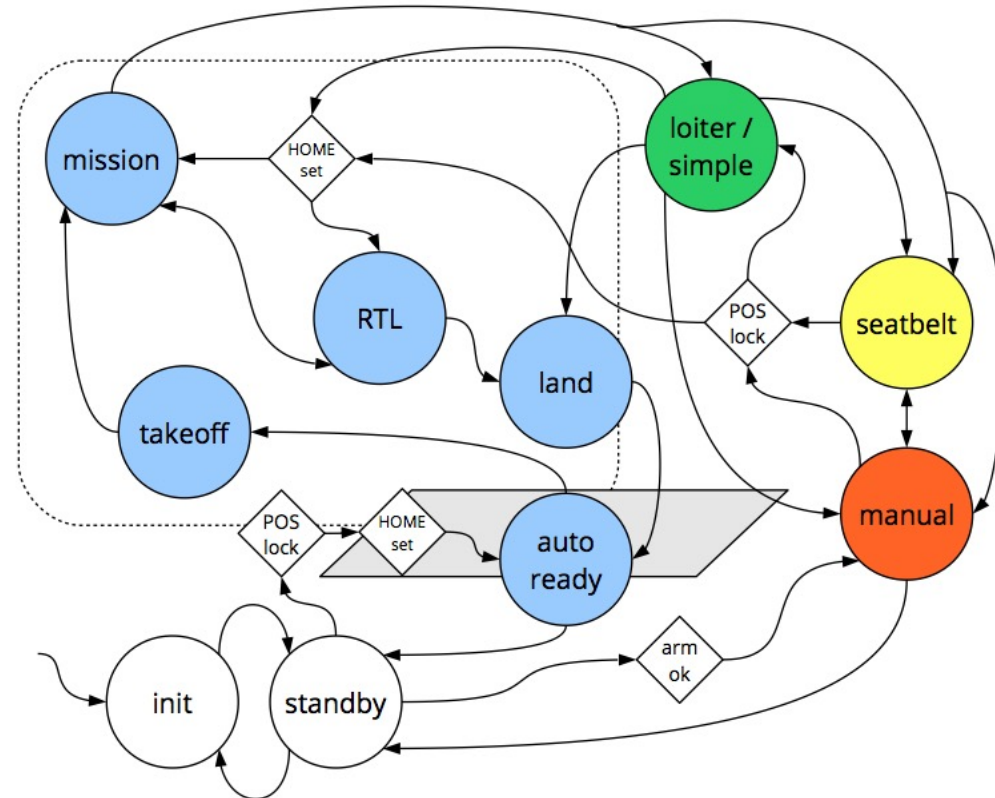
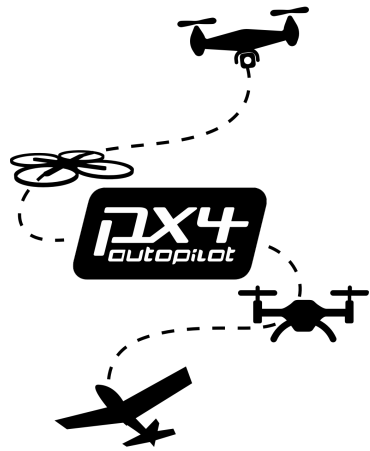
- Aim of this section
  - Understand that you do NOT have to use anything in particular in order to implement a FSM
  - Understand that there are however common ways to implement finite state machines
  - Grow awareness of tools available to help you build and analyze them

# Implementation

- A common strategy is to exploit Object Oriented Programming (OOP) and implement a class that corresponds to your finite state machine
- The class keeps track of which state the FSM is in (e.g. in a variable)
- A loop repeats at some fixed rate
- Each loop, the FSM input is read (e.g. sensors, clock)
- The current state is executed (as an if/else block)
  - Actions that need to be taken (e.g. set actuator setpoints)
  - Transition to next state (e.g. state variable updated)

# Example implementation

- PX4: in many ways the leading open source flight software for drones



# Example implementation

- Commander.cpp

```
1463         while (!should_exit()) {  
2355             bool nav_state_changed = set_nav_state(&status,
```

- state\_machine\_helper.cpp

```
441         switch (internal_state->main_state) {  
442             case commander_state_s::MAIN_STATE_ACRO:  
443                 status->nav_state = vehicle_status_s::NAVIGATION_STATE_ACRO;  
444                 break;
```

# Example implementation

- 14 open issues that involve a “state machine”...

🔔 14 Open	✓ 93 Closed	Author	Labels	Projects	Milestones	Assignee	Sort
🔔	Commander mode initialization	enhancement	failsafe	stale			1
	#12688 opened on Aug 13 by MaEtUgR						
🔔	Incorrect log publisher topic by commander modules	bug					5
	#12670 opened on Aug 8 by tecnic08						
🔔	Unable to build px4 native on beaglebone blue	beaglebone	enhancement	question			8
	#12509 opened on Jul 18 by Kirit01136						
🔔	Improved Fixed Wing Loss of GPS (global position) failsafe behavior when landing	enhancement	fixedwing				7
	#10906 opened on Nov 24, 2018 by Antiheavy						
🔔	add support for MAV_CMD_DO_MOTOR_TEST (GCS driven motor testing)	enhancement	pinned				7
	#10782 opened on Oct 29, 2018 by dagar ⚙️ Release v1.10.0						
🔔	Need to prevent Arming when in configurations (e.g. modes or waypoints) not appropriate for takeoff.	enhancement	fixedwing				11
	#10657 opened on Oct 5, 2018 by Antiheavy						
🔔	State Machine Options (Library, Framework, Generator, Compiler, etc)	enhancement	pinned				12
	#10584 opened on Sep 27, 2018 by dagar						
🔔	Simulated RC via QGC is broken	bug	stale				24
	#9318 opened on Apr 17, 2018 by RomanBapst						
🔔	**Feature Request**: block arming after sensor calibration, require system reboot (or graceful re-init) prior to flight	enhancement	pinned	priority-critical			13

# Example implementation

- Your very own navigator.py!

```
# STATE MACHINE LOGIC
# some transitions handled by callbacks
if self.mode == Mode.IDLE:
    pass
elif self.mode == Mode.ALIGN:
    if self.aligned():
        self.current_plan_start_time = rospy.get_rostime()
        self.switch_mode(Mode.TRACK)
elif self.mode == Mode.TRACK:
    if self.near_goal():
        self.switch_mode(Mode.PARK)
    elif not self.close_to_plan_start():
        rospy.loginfo("replanning because far from start")
        self.replan()
    elif (rospy.get_rostime() - self.current_plan_start_time).to_sec() > self.current_plan_duration:
        rospy.loginfo("replanning because out of time")
        self.replan() # we aren't near the goal but we thought we should have been, so replan
elif self.mode == Mode.PARK:
    if self.at_goal():
        # forget about goal:
        self.x_g = None
        self.y_g = None
        self.theta_g = None
        self.switch_mode(Mode.IDLE)

self.publish_control()
rate.sleep()
```

# ROS State Machines: SMACH

- A ROS tool that allows you to synthesize FSMs more easily
- Provides visualization tools
- Support hierarchical state machines
- Enables easy composition
- See <http://wiki.ros.org/smach/Tutorials/Getting%20Started>



# SMACH: Basic Syntax

- Two main components:
  - SMACH State
  - SMACH Container (e.g. FSM)

# SMACH: Basic Syntax

- SMACH State
  - The basic state abstraction. Corresponds 1:1 with the FSM states described earlier
  - Inherit from `smach.State` and must implement two functions:
    - `__init__`
    - `execute`
  - `execute` should return 'outcomes'

# SMACH: Basic Syntax

```
class Foo(smach.State):
    def __init__(self, outcomes=[ 'outcome1', 'outcome2' ]):
        # Your state initialization goes here

    def execute(self, userdata):
        # Your state execution goes here
        if xxxx:
            return 'outcome1'
        else:
            return 'outcome2'
```

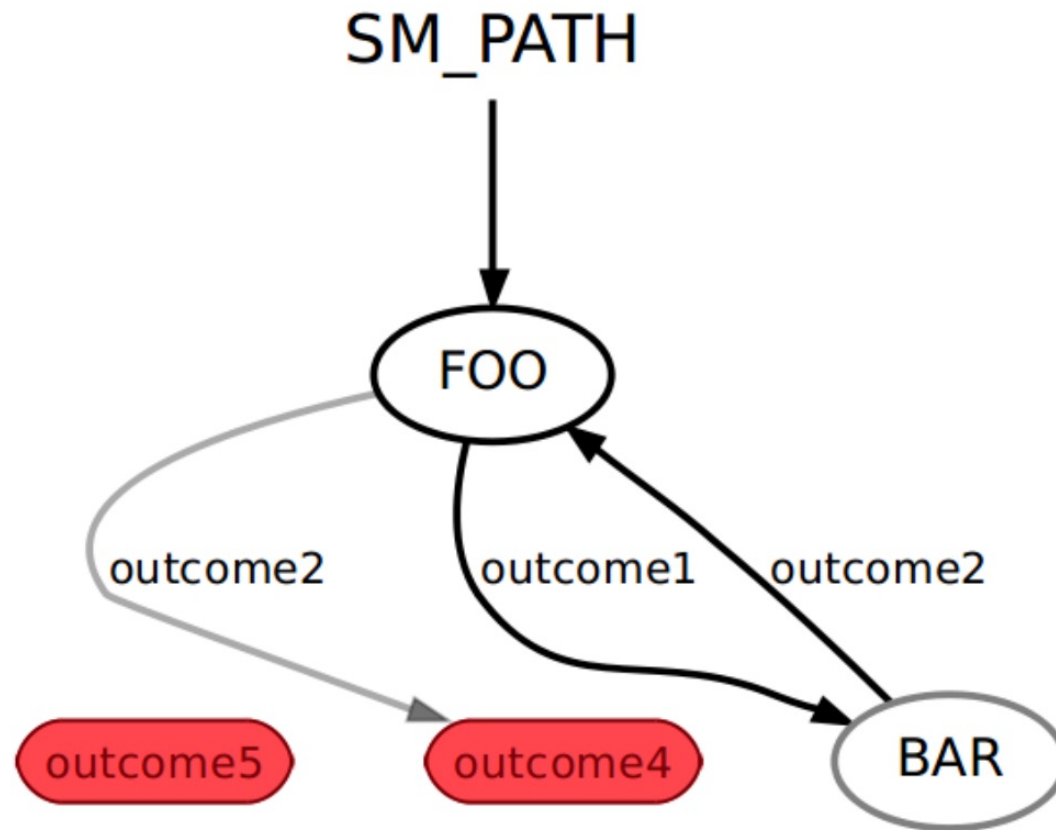
# SMACH: Basic Syntax

- SMACH Container
  - Roughly corresponds to the idea of a finite state machine, with variations.
  - You are most likely to use the container `smach.StateMachine`
  - States can be added to containers
  - Containers can be composed

# SMACH: Basic Syntax

```
sm = smach.StateMachine(outcomes=[ 'outcome4', 'outcome5' ])
with sm:
    smach.StateMachine.add('FOO', Foo(),
                           transitions={ 'outcome1': 'BAR',
                                           'outcome2': 'outcome4' })
    smach.StateMachine.add('BAR', Bar(),
                           transitions={ 'outcome2': 'FOO' })
```

# SMACH: Basic Example



# SMACH: Basic Example

```
# define state Foo
class Foo(smach.State):
    def __init__(self):
        smach.State.__init__(self, outcomes=['outcome1', 'outcome2'])
        self.counter = 0

    def execute(self, userdata):
        rospy.loginfo('Executing state FOO')
        if self.counter < 3:
            self.counter += 1
            return 'outcome1'
        else:
            return 'outcome2'
```

# SMACH: Basic Example

```
# define state Bar
class Bar(smach.State):
    def __init__(self):
        smach.State.__init__(self, outcomes=[ 'outcome2' ])

    def execute(self, userdata):
        rospy.loginfo('Executing state BAR')
        return 'outcome2'
```



# SMACH: Basic Example

```
# main
def main():
    rospy.init_node('smach_example_state_machine')

    # Create a SMACH state machine
    sm = smach.StateMachine(outcomes=['outcome4', 'outcome5'])

    # Open the container
    with sm:
        # Add states to the container
        smach.StateMachine.add('FOO', Foo(),
                               transitions={'outcome1': 'BAR',
                                           'outcome2': 'outcome4'})
        smach.StateMachine.add('BAR', Bar(),
                               transitions={'outcome2': 'FOO'})

    # Execute SMACH plan
    outcome = sm.execute()
```

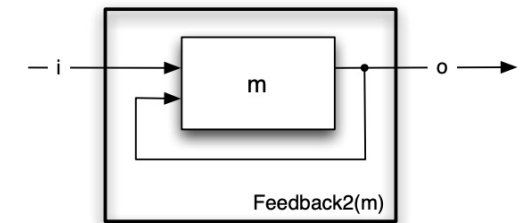
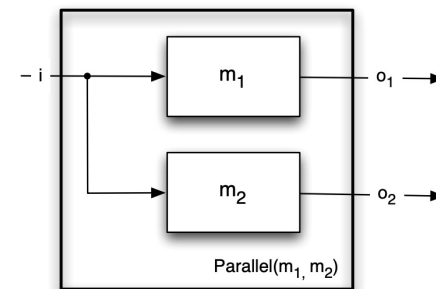
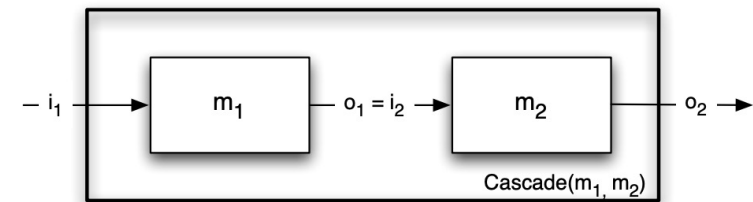
# SMACH: Composition

- The composition operations described earlier (cascade, parallel, feedback) are also possible in SMACH

Cascade -> smach.Sequence

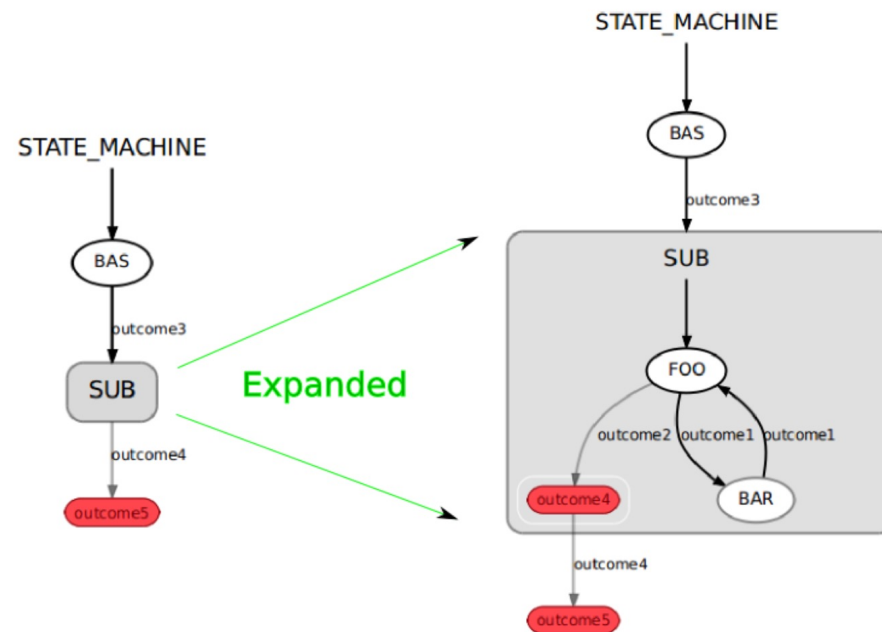
Parallel -> smach.Concurrence

Feedback -> smach.Iterator



# SMACH: Visualization

- The package `smach_visualizer` allows you to easily inspect and monitor your state machine



# DEMO: AA274 Navigator using SMACH

Thanks for a great quarter!