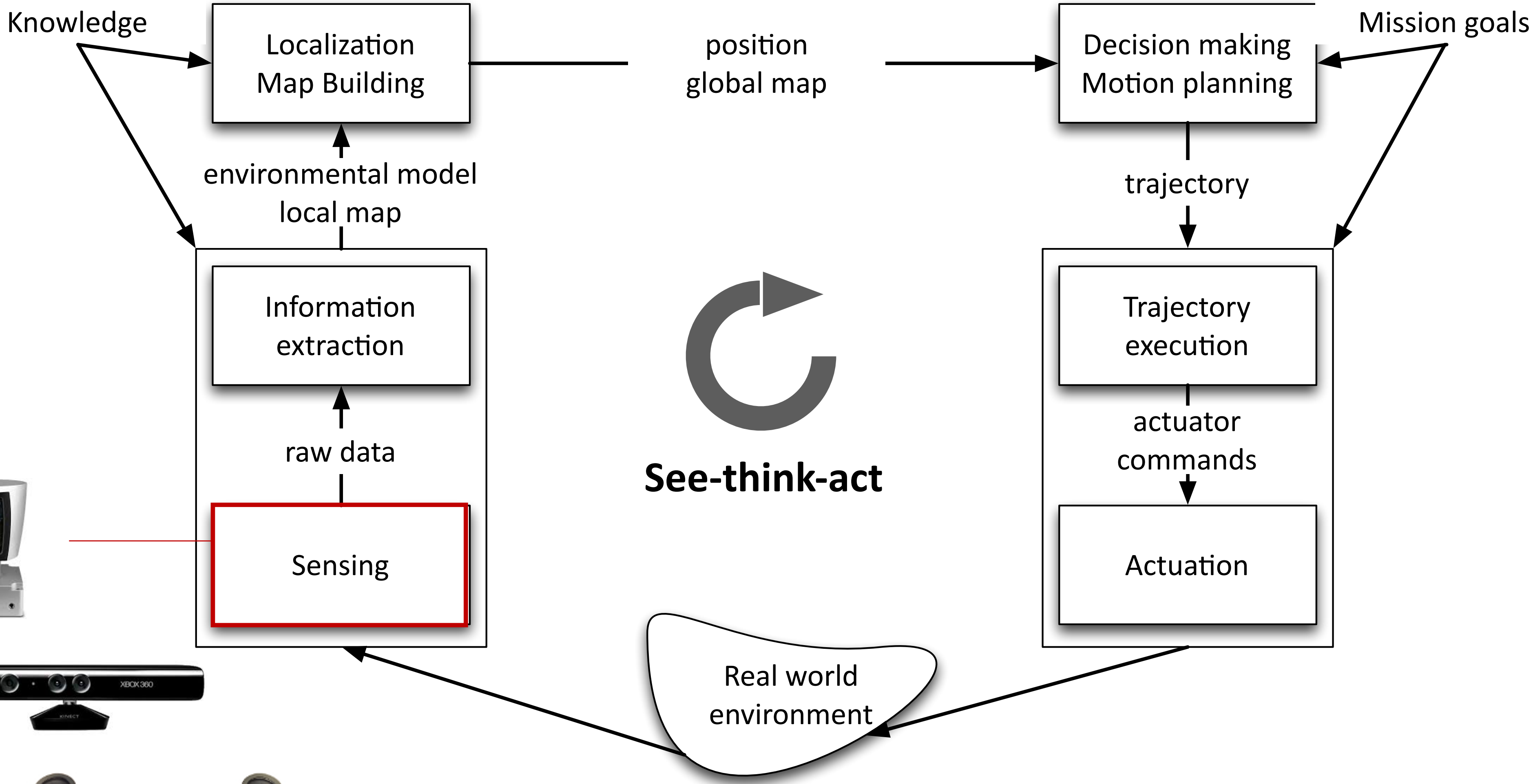
Principles of Robot Autonomy I

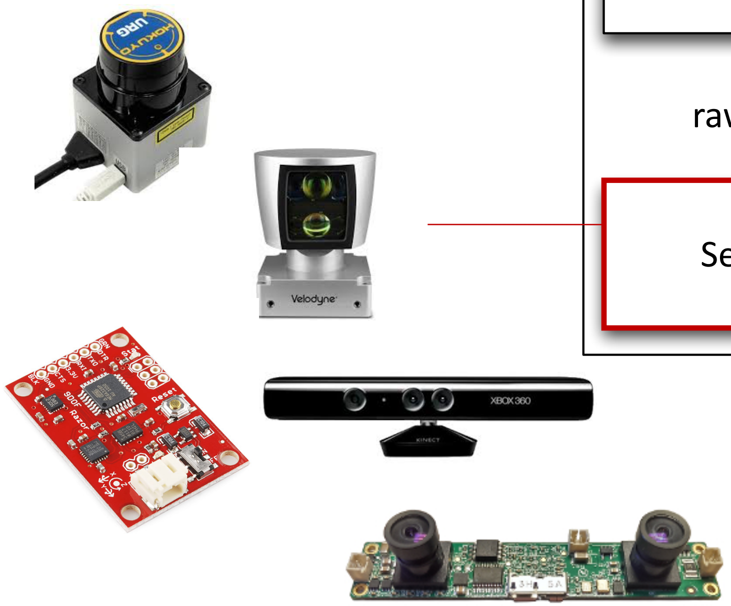
Robotic sensors and introduction to computer vision

Stanford University

Autonomous Systems Lab

Sensors for mobile robots



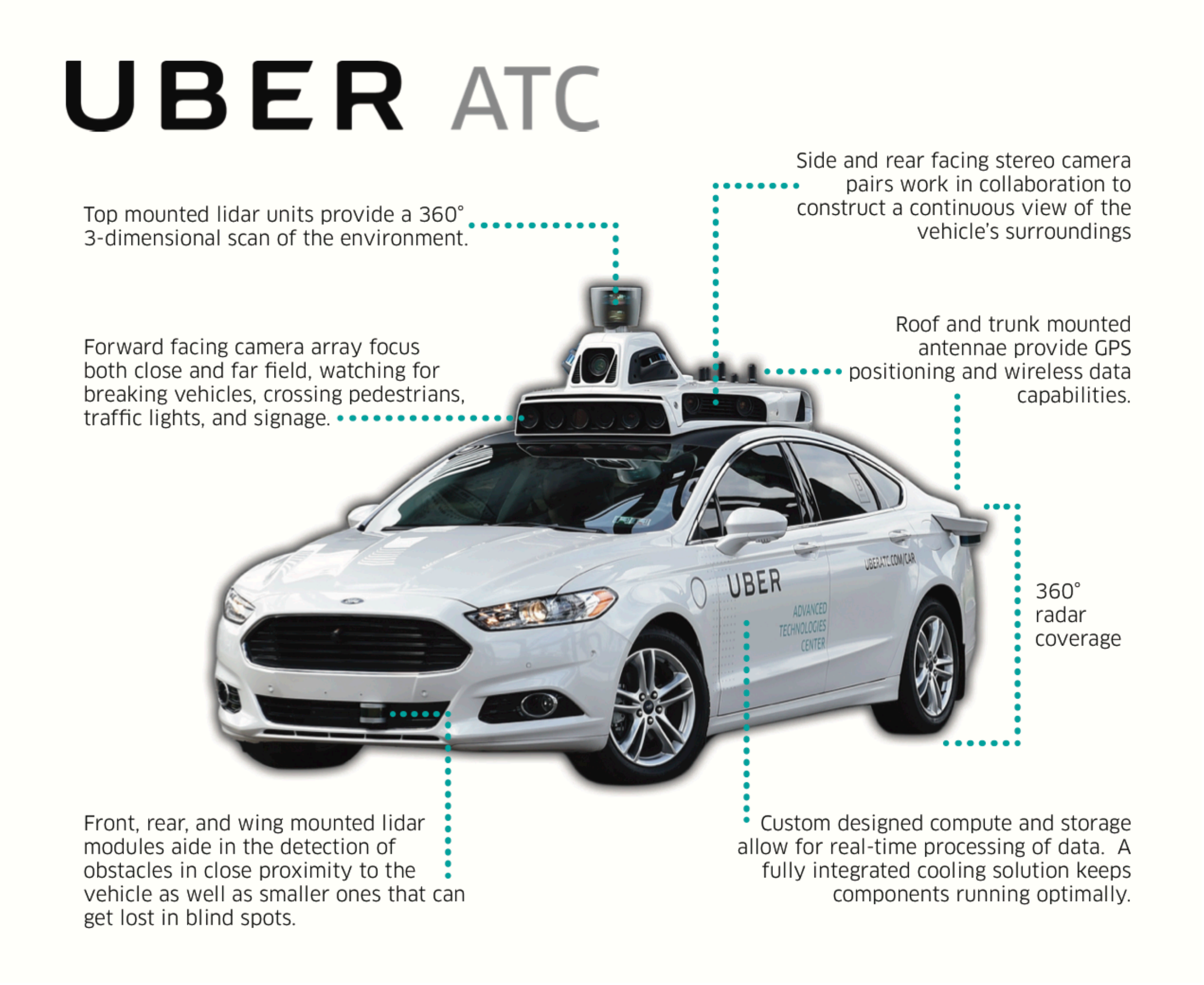


Sensors for mobile robots

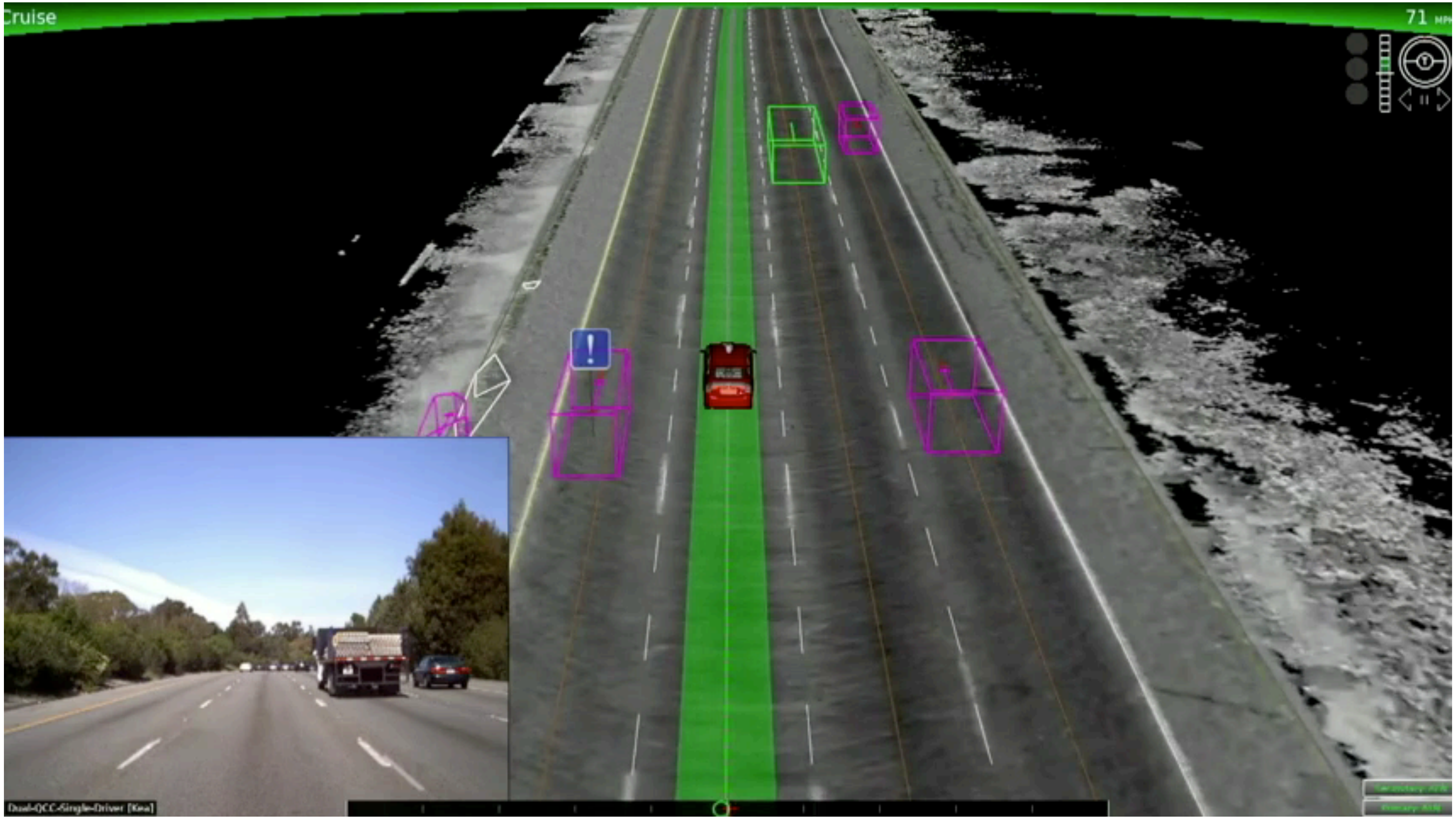
- Aim
  - Learn about key performance characteristics for robotic sensors
  - Learn about a full spectrum of sensors, e.g. proprioceptive / exteroceptive, passive / active

- Readings
  - Siegwart, Nourbakhsh, Scaramuzza. Introduction to Autonomous Mobile Robots. Section 4.1.

Example: self-driving cars



A self-driving car in action



Classification of sensors

- Proprioceptive: measure values internal to the robot
  - E.g.: motor speed, robot arm joint angles, and battery voltage
- Exteroceptive: acquire information from the robot's environment
  - E.g.: distance measurements and light intensity

- Passive: measure ambient environmental energy entering the sensor
  - Challenge: performance heavily depends on the environment
  - E.g.: temperature probes and cameras
- Active: emit energy into the environment and measure the reaction
  - Challenge: might affect the environment
  - E.g.: ultrasonic sensors and laser rangefinders

Sensor performance: design specs

- Dynamic range: ratio between the maximum and minimum input values (for normal sensor operation)
- Resolution: minimum difference between two values that can be detected by a sensor
- Linearity: whether or not the sensor's output response depends linearly on the input
- Bandwidth or frequency: speed at which a sensor provides readings (in Hertz)

Sensor performance: in situ specs

- Sensitivity: ratio of output change to input change
- Cross-sensitivity: sensitivity to quantities that are unrelated to the target quantity
- Error: difference between the sensor output m and the true value v

$$\text{error} := m - v$$

- Accuracy: degree of conformity between the sensor's measurement and the true value

$$\text{accuracy} := 1 - |\text{error}|/v$$

- Precision: reproducibility of the sensor results

Sensor errors

- Systematic errors: caused by factors that can in theory be modeled; they are deterministic
  - E.g.: calibration errors
- Random errors: cannot be predicted with sophisticated models; they are stochastic
  - E.g.: spurious range-finding errors
- Error analysis: performed via a probabilistic analysis
  - Common assumption: symmetric, unimodal (and often Gaussian) distributions; convenient, but often a coarse simplification
  - Error propagation characterized by the *error propagation law*

An ecosystem of sensors

- Encoders
- Heading sensors
- Accelerometers and IMU
- Beacons
- Active ranging
- Cameras

Encoders

- Encoder: an electro-mechanical device that converts motion into a sequence of digital pulses, which can be converted to relative or absolute position measurements
  - proprioceptive sensor
  - can be used for robot localization

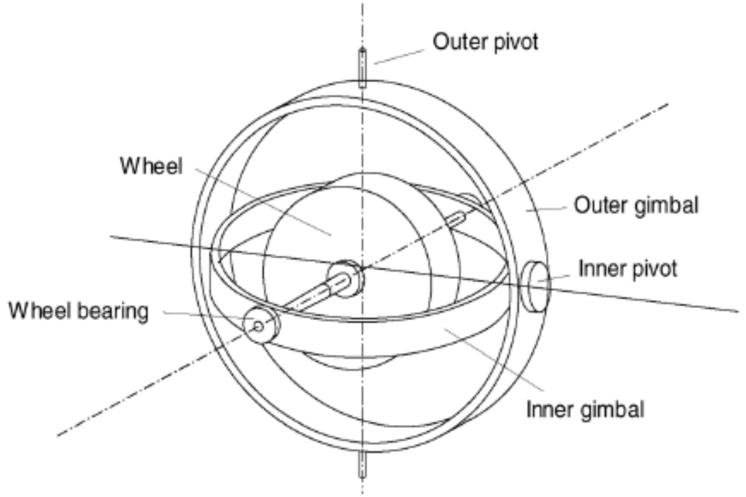
Wheel encoder
Credit: Pololu

- Fundamental principle of optical encoders: use a light shining onto a photodiode through slits in a metal or glass disc

Credit: Honest Sensor

Heading sensors

- Used to determine robot’s orientation, it can be:
  1. Proprioceptive, e.g., gyroscope (heading sensor that preserves its orientation in relation to a fixed reference frame)
  2. Exteroceptive, e.g., compass (shows direction relative to the geographic cardinal directions)
- Fusing measurements with velocity information, one can obtain a position estimate (via integration) -> *dead reckoning*
- Fundamental principle of mechanical gyroscopes: angular momentum associated with spinning wheel keeps the axis of rotation inertially stable



Credit: SNS

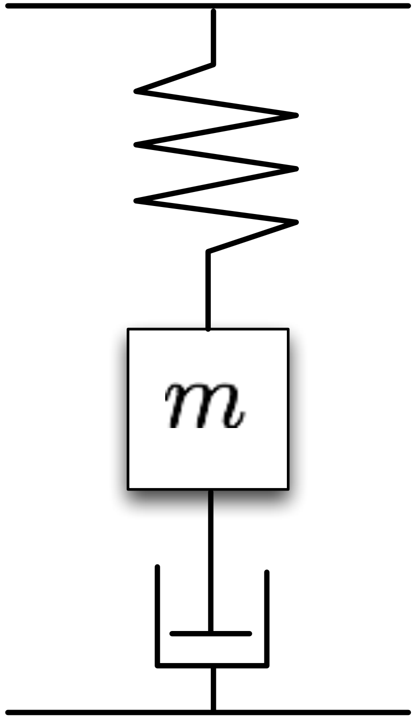
Accelerometer and IMU

- Accelerometer: device that measures all external forces acting upon it
- Mechanical accelerometer: essentially, a spring-mass-damper system

$$F_{\text{applied}} = m\ddot{x} + c\dot{x} + kx$$

with *m* mass of proof mass, *c* damping coefficient, *k* spring constant; in steady state

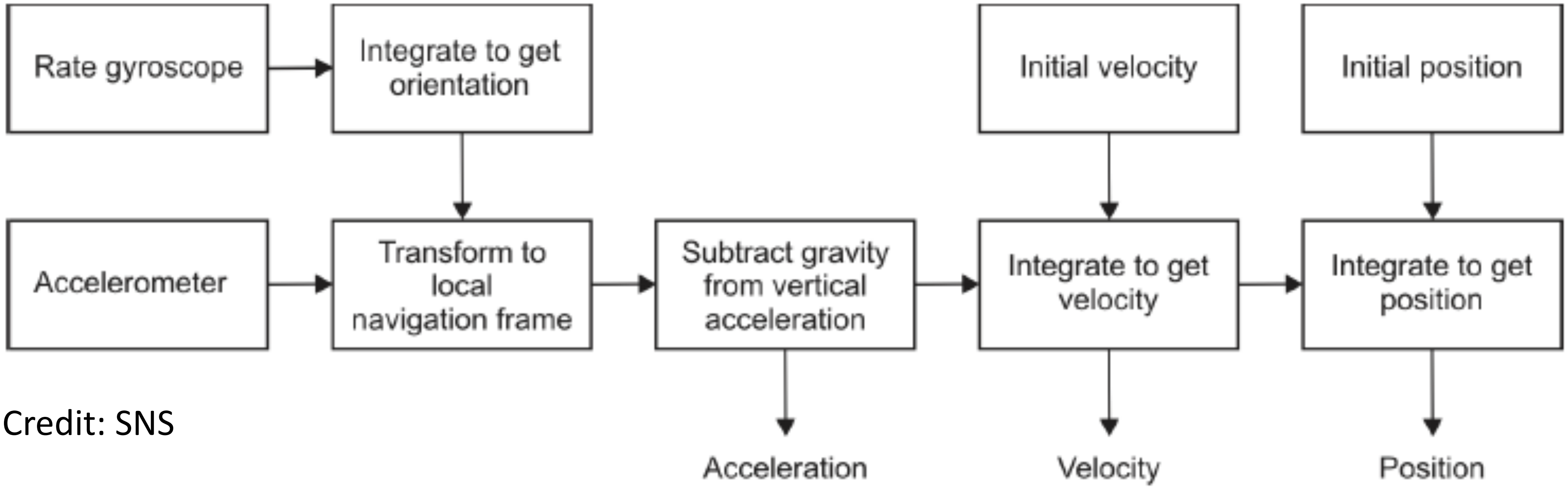
$$a_{\text{applied}} = \frac{kx}{m}$$



- Modern accelerometers use MEMS (cantilevered beam + proof mass); deflection measured via *capacitive* or *piezoelectric* effects

Inertial Measurement Unit (IMU)

- Definition: device that uses gyroscopes and accelerometers to estimate the relative position, orientation, velocity, and acceleration of a moving vehicle with respect to an inertial frame
- *Drift* is a fundamental problem: to cancel drift, periodic references to external measurements are required



Credit: SNS

Beacons

- Definition: signaling devices with precisely known positions
- Early examples: stars, lighthouses
- Modern examples: GPS, motion capture systems

Active ranging

- Provide direct measurements of distance to objects in vicinity
- Key elements for both localization and environment reconstruction
- Main types:
  1. Time-of-flight active ranging sensors (e.g., ultrasonic and laser rangefinder)

Credit: https://electrosome.com/hc-sr04-ultrasonic-sensor-pic/

  2. Geometric active ranging sensors (optical triangulation and structured light)

Time-of-flight active ranging

- Fundamental principle: time-of-flight ranging makes use of the propagation of the speed of sound or of an electromagnetic wave
- Travel distance is given by

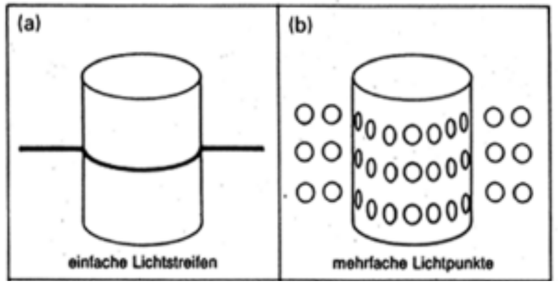
$$d = c\,t$$

where d is the distance traveled, c is the speed of the wave propagation, and t is the time of flight

- Propagation speeds:
  - Sound: 0.3 m/ms
  - Light: 0.3 m/ns
- Performance depends on several factors, e.g., uncertainties in determining the exact time of arrival and interaction with the target

Geometric active ranging

- Fundamental principle: use geometric properties in the measurements to establish distance readings
- The sensor projects a known light pattern (e.g., point, line, or texture); the reflection is captured by a receiver and, together with known geometric values, range is estimated via triangulation
- Examples:
  - Optical triangulation (1D sensor)
  - Structured light (2D and 3D sensor)



Several other sensors are available

- Classical, e.g.:
  - Radar (possibly using Doppler effect to produce velocity data)
  - Tactile sensors
- Emerging technologies:
  - Artificial skins
  - Neuromorphic cameras

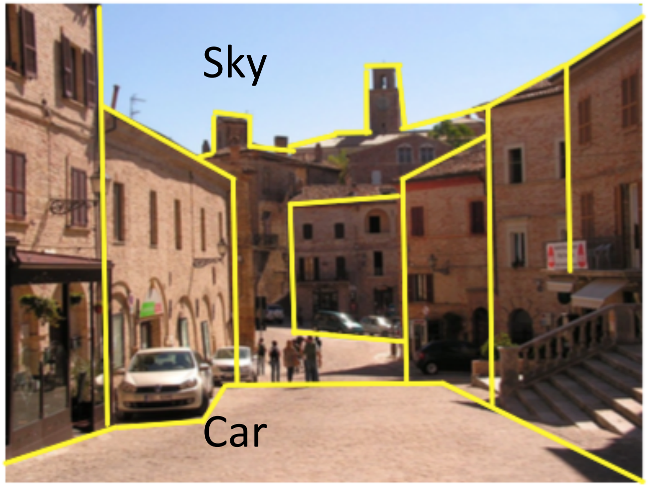
Introduction to computer vision

- Aim
  - Learn about cameras and camera models

- Readings
  - Siegwart, Nourbakhsh, Scaramuzza. Introduction to Autonomous Mobile Robots. Section 4.2.3.
  - D. A. Forsyth and J. Ponce [FP]. Computer Vision: A Modern Approach (2nd Edition). Prentice Hall, 2011. Chapter 1.

Vision

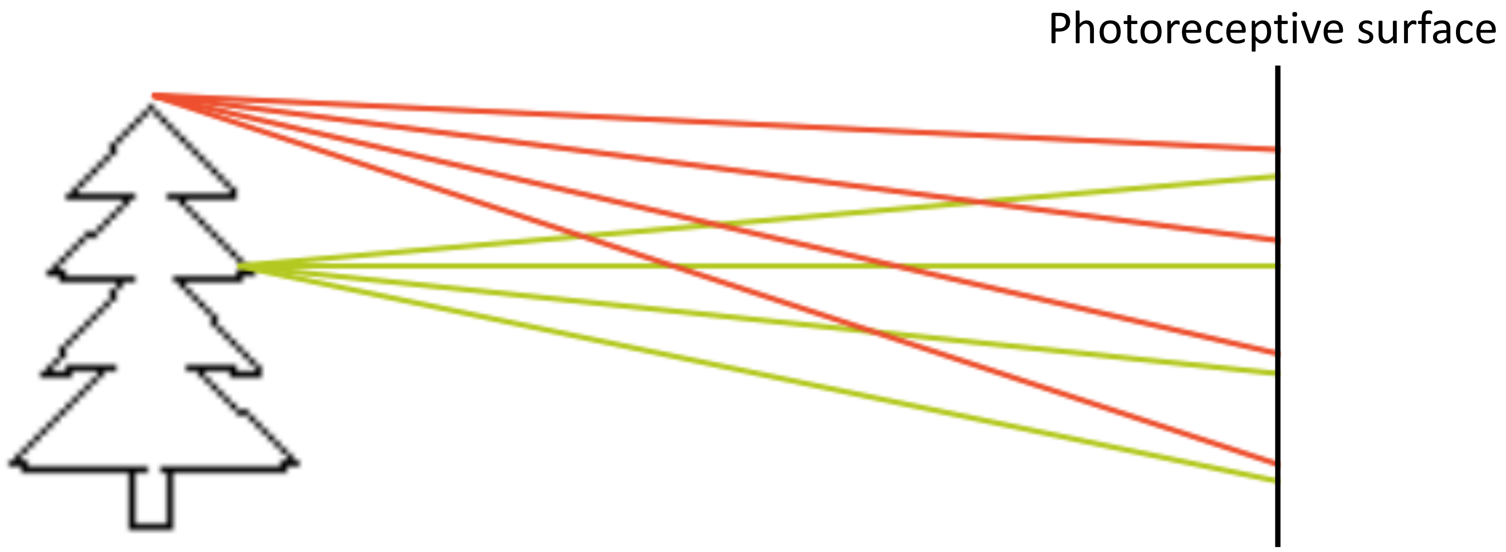
- Vision: ability to interpret the surrounding environment using light in the visible spectrum reflected by objects in the environment
- Human eye: provides enormous amount of information, ~millions of bits per second
- Cameras (e.g., CCD, CMOS): capture light -> convert to digital image -> process to get relevant information (from geometric to semantic)



1. Information extraction
2. Interpretation

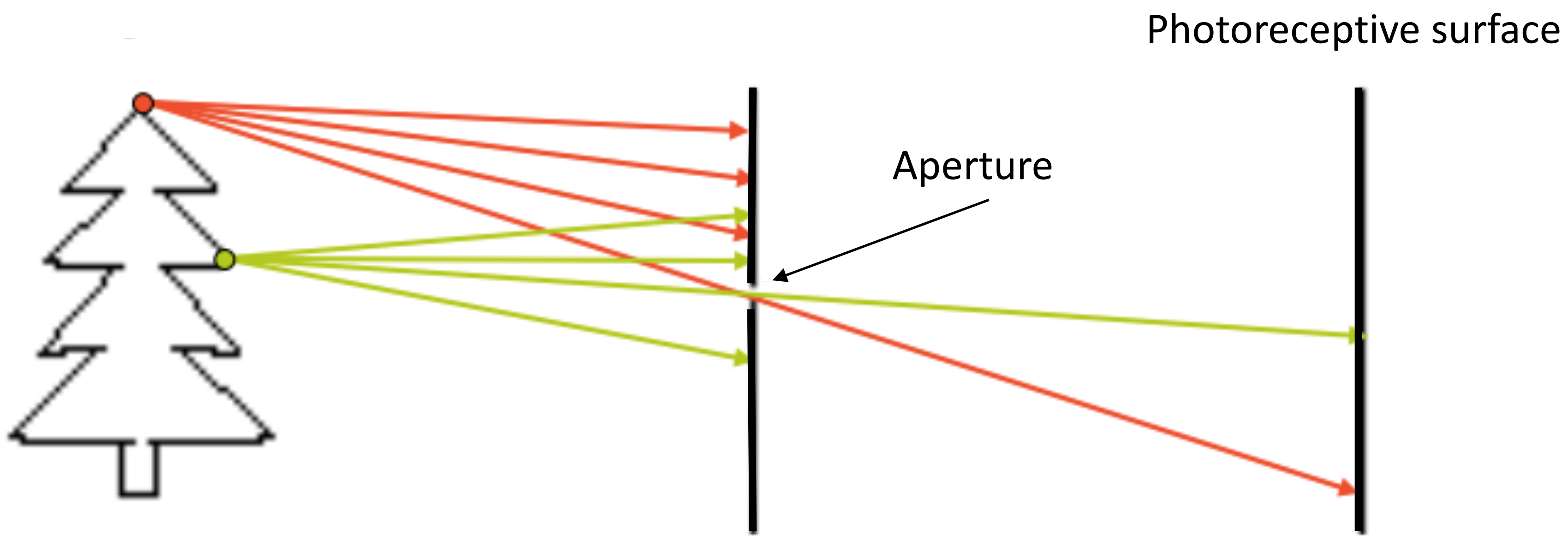
How to capture an image of the world?

- Light is reflected by the object and scattered in all directions
- If we simply add a photoreceptive surface, the captured image will be extremely blurred



Pinhole camera

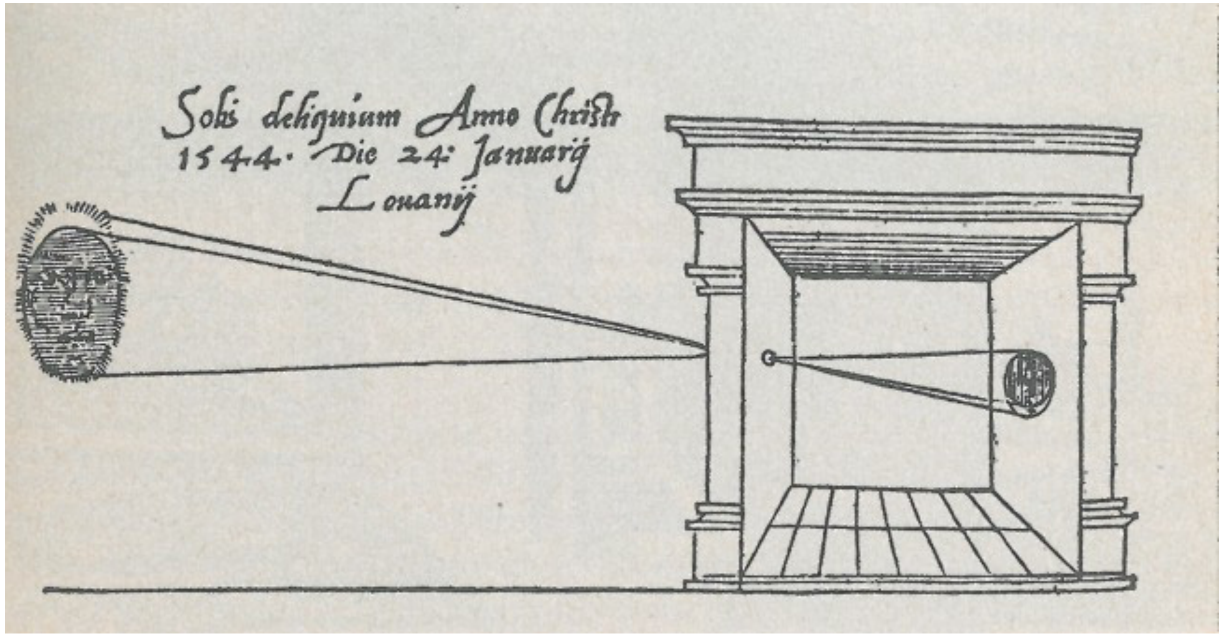
- Idea: add a barrier to block off most of the rays



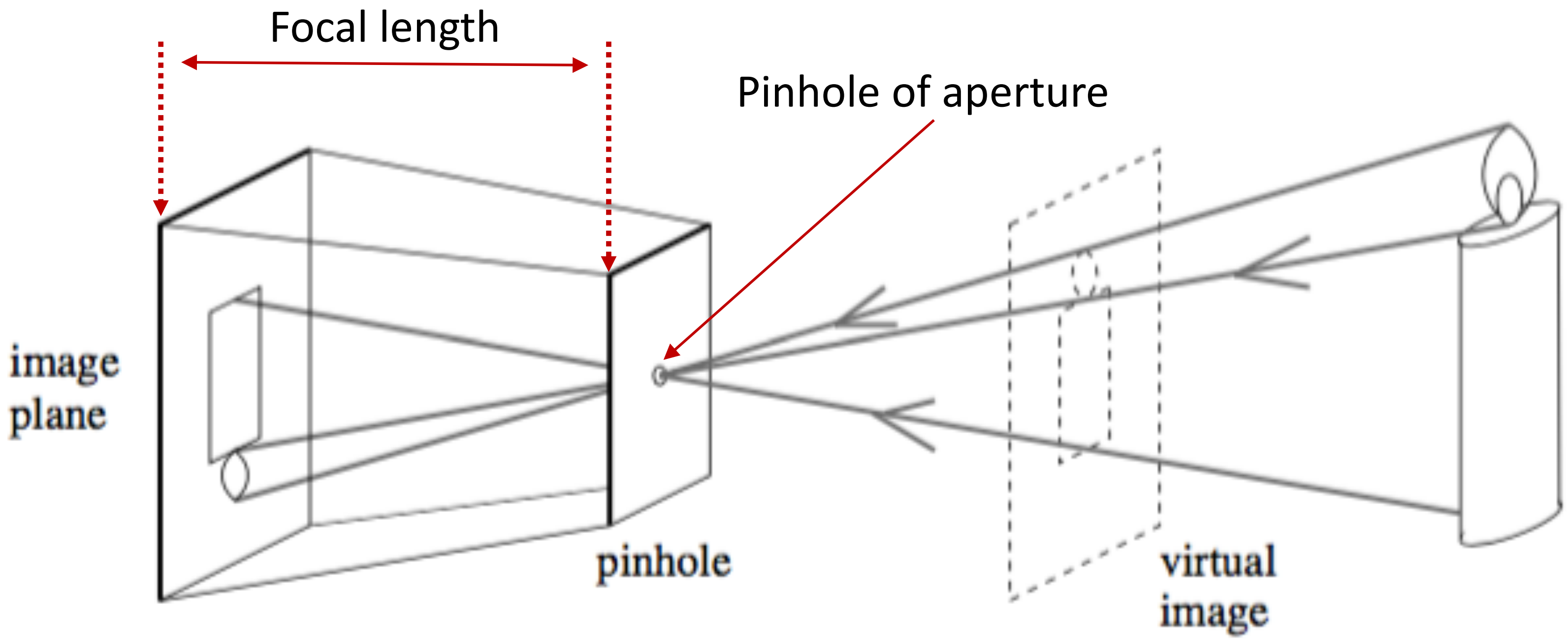
- Pinhole camera: a camera *without a lens* but with a tiny aperture, a *pinhole*

A long history

- Very old idea (several thousands of years BC)
- First clear description from Leonardo Da Vinci (1502)
- Oldest known published drawing of a camera obscura by Gemma Frisius (1544)



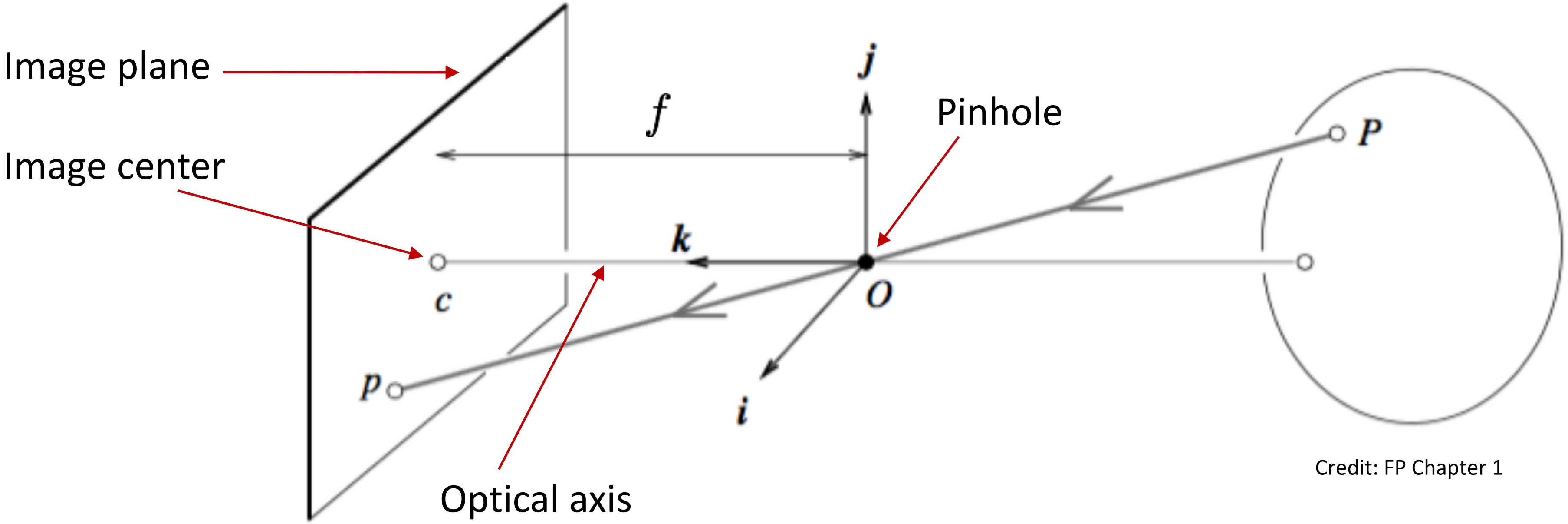
Pinhole camera



Credit: FP Chapter 1

- Perspective projection creates inverted images
- Sometimes it is convenient to consider a *virtual image* associated with a plane lying in front of the pinhole
- Virtual image not inverted but otherwise equivalent to the actual one

Pinhole perspective



Credit: FP Chapter 1

$$P = (X, Y, Z)$$

Perspective

$$p = (x, y, z)$$

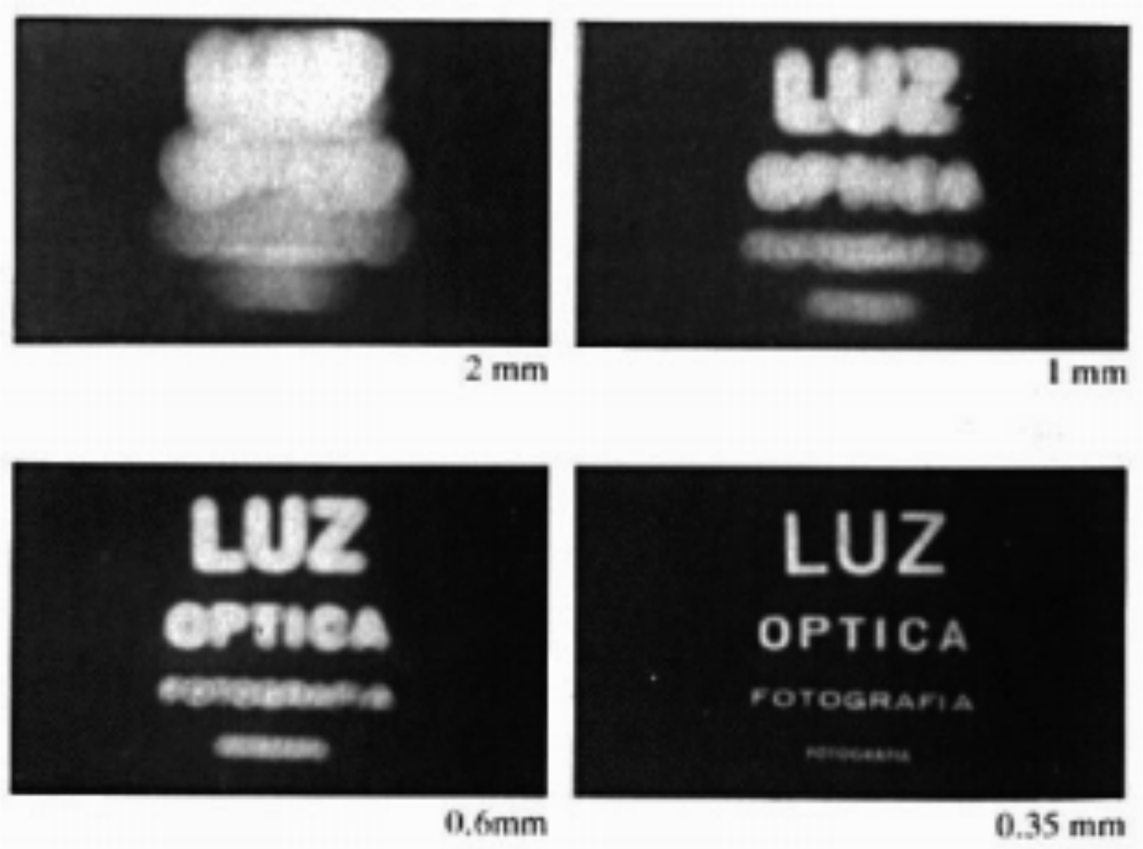
- Since P, O, and p are collinear: $\overline{Op} = \lambda \overline{OP}$ for some $\lambda \in R$
- Also, $z=f$, hence

$$\begin{cases} x = \lambda X \\ y = \lambda Y \\ z = \lambda Z \end{cases} \Leftrightarrow \lambda = \frac{x}{X} = \frac{y}{Y} = \frac{z}{Z} \quad \Rightarrow \quad \begin{cases} x = f\,\frac{X}{Z} \\ y = f\,\frac{Y}{Z} \end{cases}$$

Issues with pinhole camera

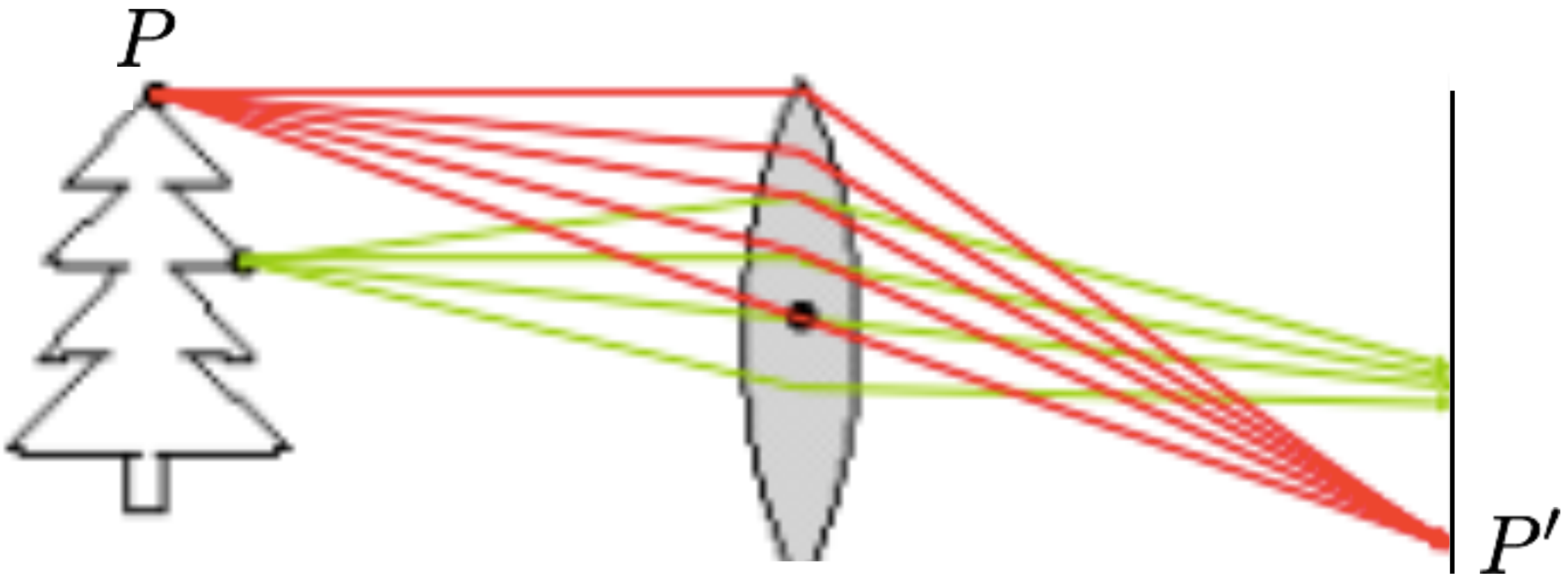
- Larger aperture -> greater number of light rays that pass through the aperture -> blur
- Smaller aperture -> fewer number of light rays that pass through the aperture -> darkness (+ diffraction)

- Solution: add a lens to replace the aperture!

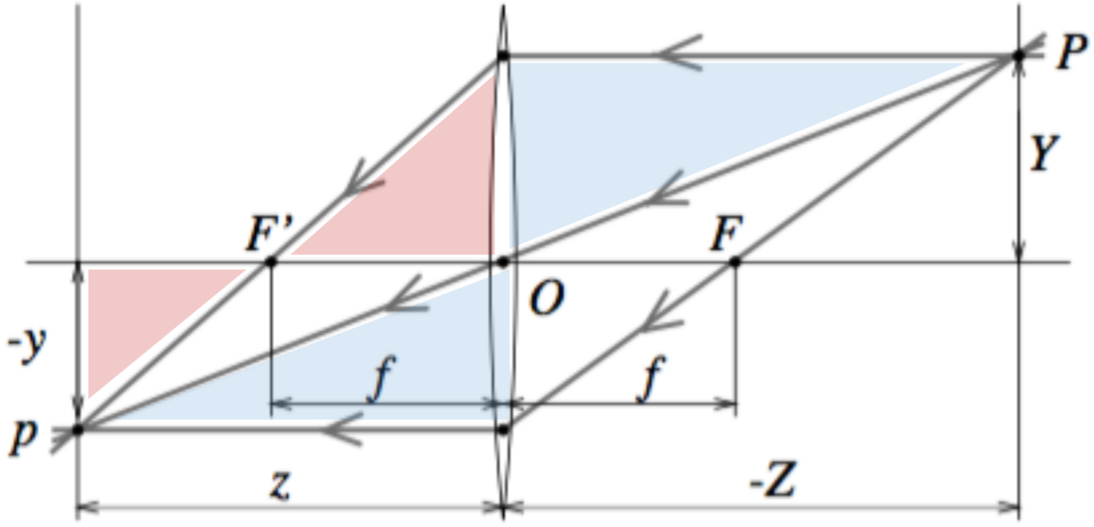


Lenses

- Lens: an optical element that focuses light by means of refraction



Thin lens model



Credit: FP Chapter 1

Key properties (follows from Snell's law) :

1. Rays passing through *O* are not refracted
2. Rays parallel to the optical axis are focused on the *focal point F'*
3. *All* rays passing through *P* are focused by the thin lens on the point *p*

- Similar triangles

$$\frac{y}{Y} = \frac{z}{Z}$$ Blue triangles

$$\frac{y}{Y} = \frac{z-f}{f} = \frac{z}{f} - 1$$ Red triangles

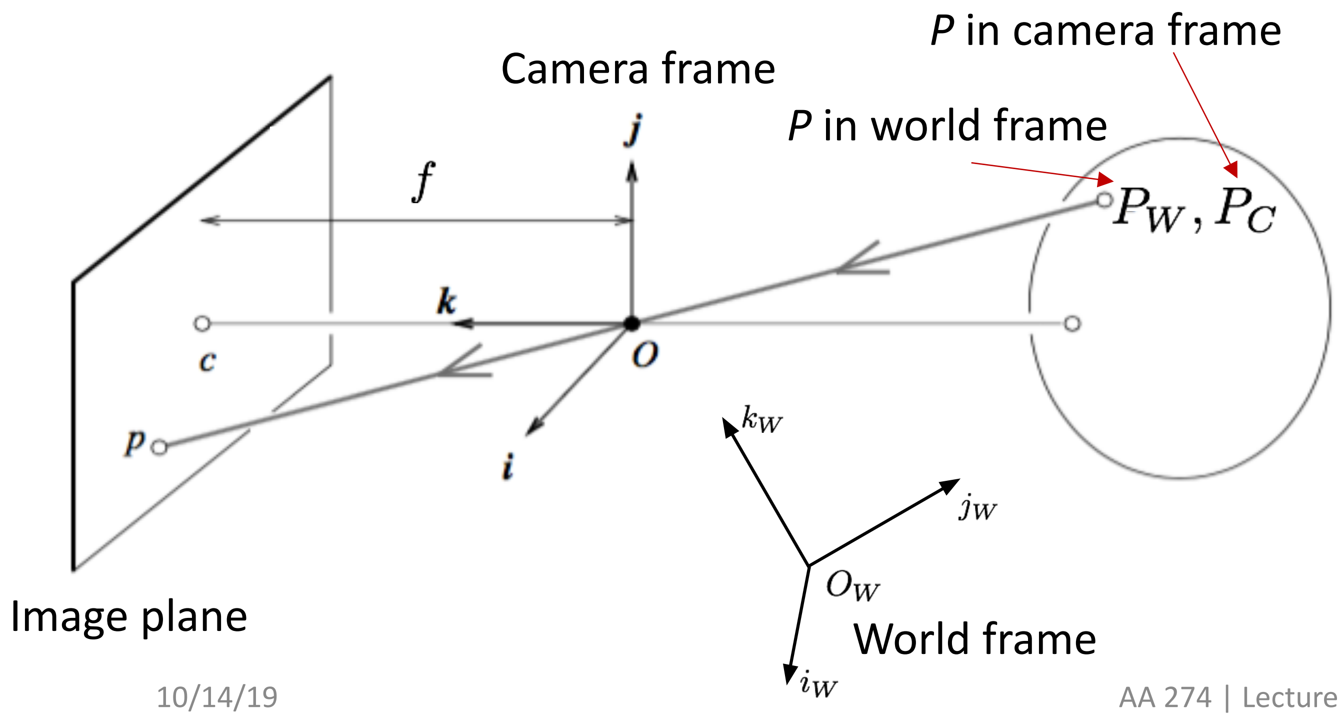
$$\boxed{\Rightarrow \frac{1}{z} + \frac{1}{Z} = \frac{1}{f}}$$ Thin lens equation

Thin lens model

- Key points:
  1. The equations relating the positions of P and p are exactly the same as under pinhole perspective if one considers z as focal length (as opposed to f), since P and p lie on a ray passing through the center of the lens
  2. Points located at a distance $-Z$ from O will be in sharp focus only when the image plane is located at a distance z from O on the other side of the lens that satisfies the thin lens equation
  3. In practice, objects within some range of distances (called depth of field or depth of focus) will be in acceptable focus
  4. Letting $Z \rightarrow \infty$ shows that f is the distance between the center of the lens and the plane where distant objects focus
  5. In reality, lenses suffer from a number of *aberrations*

Perspective projection

- Goal: find how world points map in the camera image
- Assumption: pinhole camera model (*all results also hold under thin lens model, assuming camera is focused at ∞*)



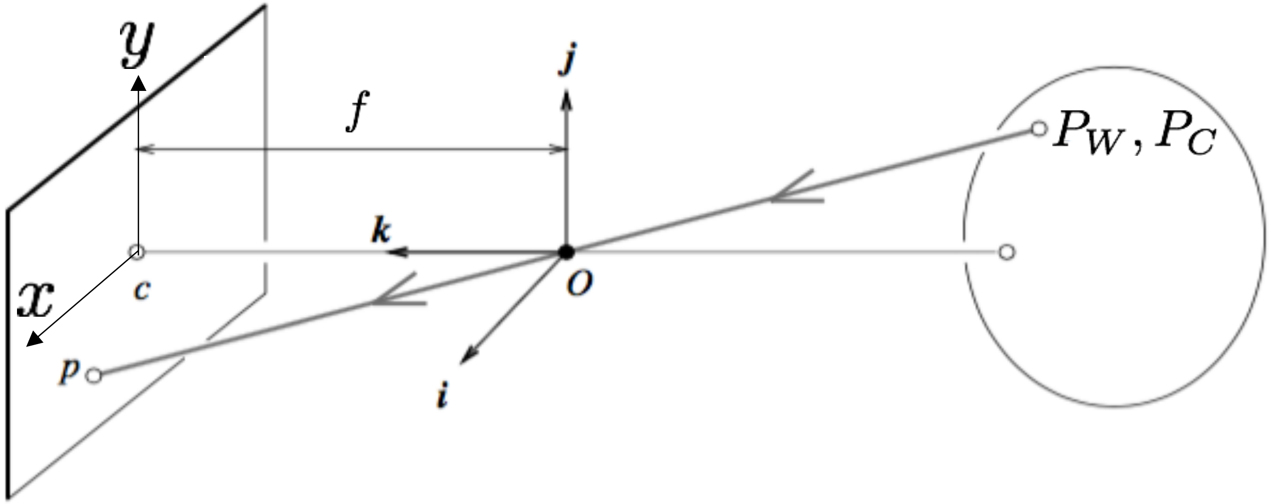
Procedure

1. Map P_c into p (image plane)
2. Map p into (u,v) (pixel coordinates)
3. Transform P_w into P_c

Step 1

- Task: Map $P_c = (X_C, Y_C, Z_C)$ into $p = (x, y)$ (image plane)
- From before

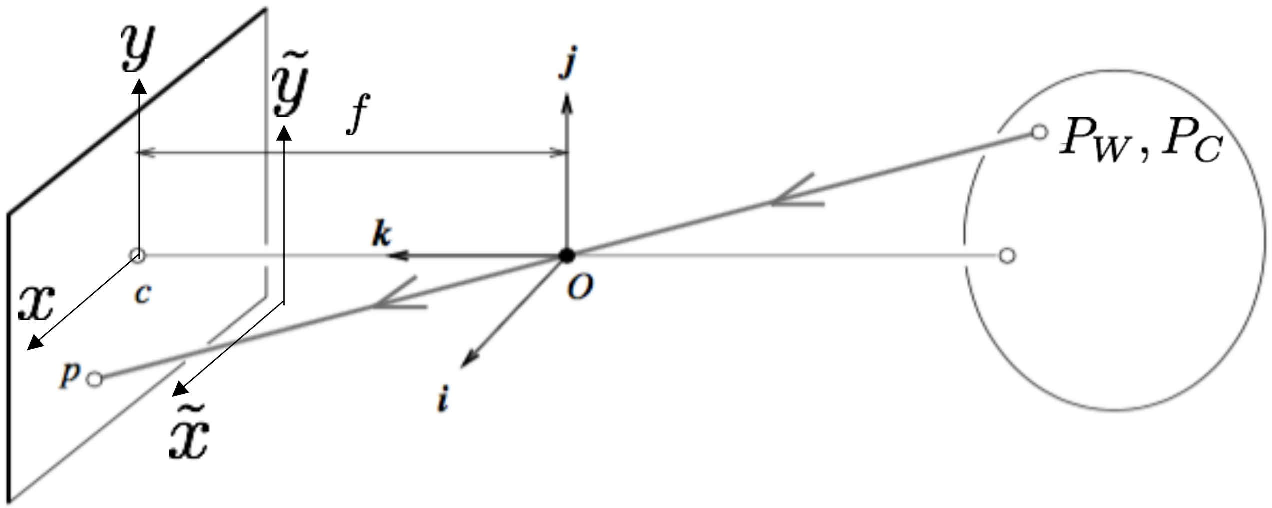
$$\begin{cases} x = f\,\frac{X_C}{Z_C} \\ y = f\,\frac{Y_C}{Z_C} \end{cases}$$

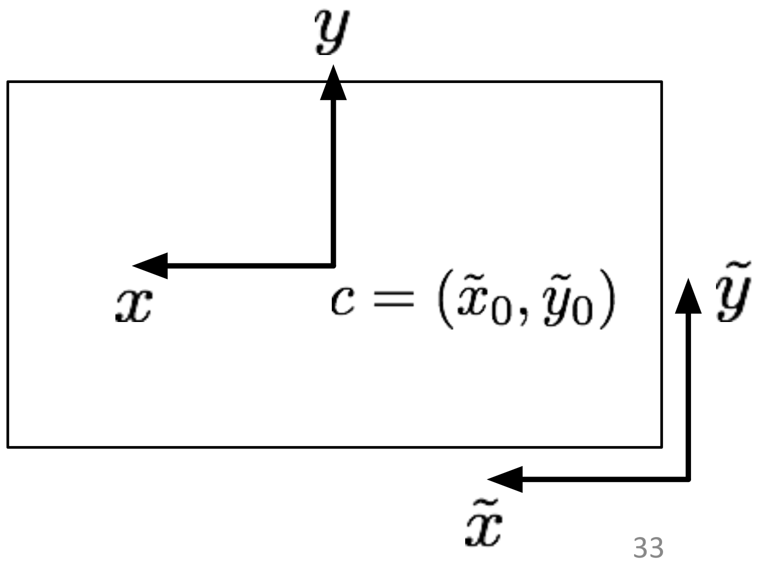


Step 2.a

- Fact: actual origin of the camera coordinate system is usually at a corner (lower left)

$$\tilde{x} = f\,\frac{X_C}{Z_C} + \tilde{x}_0, \qquad \tilde{y} = f\,\frac{Y_C}{Z_C} + \tilde{y}_0,$$





Step 2.b

- Task: convert from image coordinates $(\tilde{x}, \tilde{y})$ to pixel coordinates (u, v)
- Let k_x and k_y be the number of pixels per unit distance in image coordinates in the *x* and *y* directions, respectively

$$u = k_x \tilde{x} = \overbrace{k_x\, f}^{\alpha} \frac{X_C}{Z_C} + \overbrace{k_x \tilde{x}_0}^{u_0}$$

$$v = k_y \tilde{y} = \underbrace{k_y f}_{\beta} \frac{Y_C}{Z_C} + \underbrace{k_y \tilde{y}_0}_{v_0}$$

$$\Rightarrow \quad \boxed{\begin{aligned} u &= \alpha \frac{X_C}{Z_C} + u_0 \\ v &= \beta \frac{Y_C}{Z_C} + v_0 \end{aligned}}$$

Nonlinear transformation

Homogeneous coordinates

- Goal: represent the transformation as a linear mapping
- Key idea: introduce homogeneous coordinates

Inhomogenous -> homogeneous

$$\begin{pmatrix} x \\ y \end{pmatrix} \Rightarrow \lambda \begin{pmatrix} x \\ y \\ 1 \end{pmatrix} \qquad \begin{pmatrix} x \\ y \\ z \end{pmatrix} \Rightarrow \lambda \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix}$$

Homogenous -> inhomogeneous

$$\begin{pmatrix} x \\ y \\ w \end{pmatrix} \Rightarrow \begin{pmatrix} x/w \\ y/w \end{pmatrix} \qquad \begin{pmatrix} x \\ y \\ z \\ w \end{pmatrix} \Rightarrow \begin{pmatrix} x/w \\ y/w \\ z/w \end{pmatrix}$$

Perspective projection in homogeneous coordinates

- Projection can be equivalently written in homogeneous coordinates

$$\left[\begin{array}{cc} \overbrace{\boxed{\begin{matrix}\alpha & 0 & u_0 \\ 0 & \beta & v_0 \\ 0 & 0 & 1\end{matrix}}}^{K} & \begin{matrix}0\\0\\0\end{matrix}\end{array}\right] \begin{pmatrix} X_c \\ Y_c \\ Z_c \\ 1 \end{pmatrix} = \begin{pmatrix} \alpha X_c + u_0 Z_c \\ \beta Y_c + v_0 Z_c \\ Z_c \end{pmatrix}$$

Camera matrix/
Matrix of intrinsic parameters

P_c in homogeneous coordinates

Homogeneous pixel coordinates

- In homogeneous coordinates, the mapping is linear:

Point p in homogeneous pixel coordinates

$$p^h = [K \quad 0_{3\times 1}] P_C^h$$

Point P_c in homogeneous camera coordinates

Skewness

- In some (rare) cases

Skew parameter

$$K = \begin{bmatrix} \alpha & \gamma & u_0 \\ 0 & \beta & v_0 \\ 0 & 0 & 1 \end{bmatrix}$$

- When is $\gamma \neq 0$?
  - x- and y-axis of the camera are not perpendicular (unlikely)
  - For example, as a result of taking an image of an image
- Five parameters in total!

Next time: computer vision